

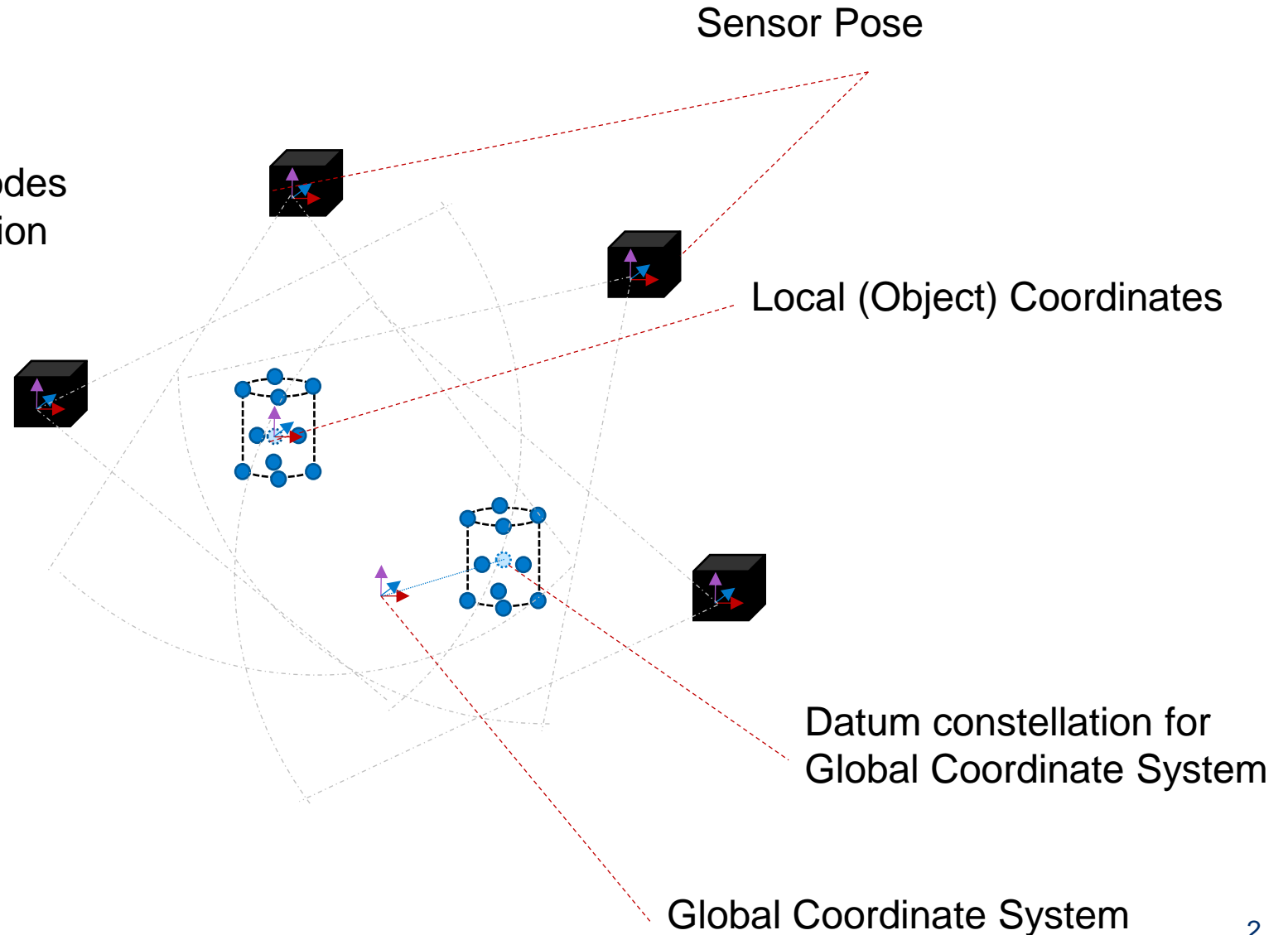
# Generalised Test for the Qualification of Distributed Large Volume Metrology Systems for Dynamic Measurement

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3DMC 2024 Loughborough

# Distributed Large Volume Metrology System

- A distributed LVM system has multiple nodes that work in concert to measure the position and/or orientation of objects
  - are often capable of measuring multiple independent objects simultaneously
  - overcome line of sight limitations
  - can be based on numerous technologies and processing methodologies



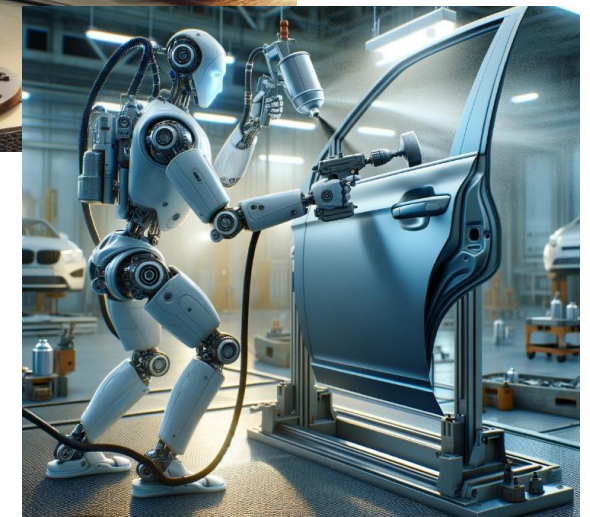
# Introduction: The Motivation

Traditional robotic manipulators excel at repeatable tasks in controlled environments but historically do not accommodate high levels of in-task variability.

Improve operational flexibility and autonomy can be achieved via decoupled guidance systems.

A decoupled guidance system can provide a common coordinate system for the workpiece and manipulator, this;

- create control zones allowing compliant and/or generalist robots to perform high precision tasks.
- promotes interoperability between process actuators.
- simplifies new task deployment.
- allows better handling of in-task variability.



# Introduction: The Challenge

Many different technologies are, or have the potential to be, used for this application.

Evolving requirements as new technologies promise to automate a broader range of tasks.

Intersection of multiple fields/disciplines

- dimensional metrology, motion capture, positioning systems, and robotics and control.

Complex standards landscape.

## *Current/Potential Technologies for Robot Guidance*

*Photogrammetry*

*Laser Trackers*

*Structured Light Scanning*

*Time-of-Flight (ToF) Cameras*

*Ultra-Wideband (UWB)*

*Bluetooth Low Energy (BLE)*

*RFID*

*Laser Radar (LIDAR)*

*Inertial Measurement Units (IMU):*

*Micro-Electro-Mechanical Systems (MEMS)*

*Acoustic Systems*

*Magnetic Systems*

*Kinematic Methods*

*Hybrid multi-sensor or multi-nodal systems*

# Contents

## Aim

To develop a generalised set of standard tests to quantify the performance of a distributed six degrees of freedom, single or multi- target, large volume metrology (LVM) system for *dynamic* (moving) applications

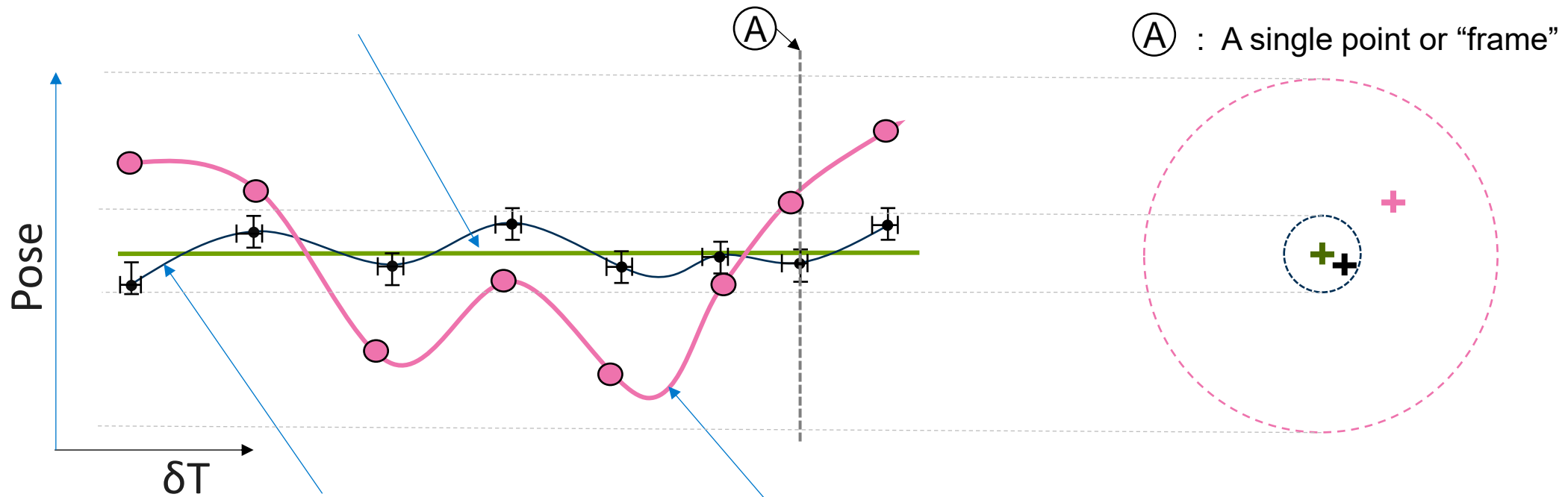
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- Method
  - Overview of a distributed large volume metrology system
  - Methodology Development
- Preliminary Results
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# Method : Principle

**Nominal / Control / Requested Path:** The path requested of the actuator

- Determined through calibration.
- May be quantified relatively opposed to absolute.



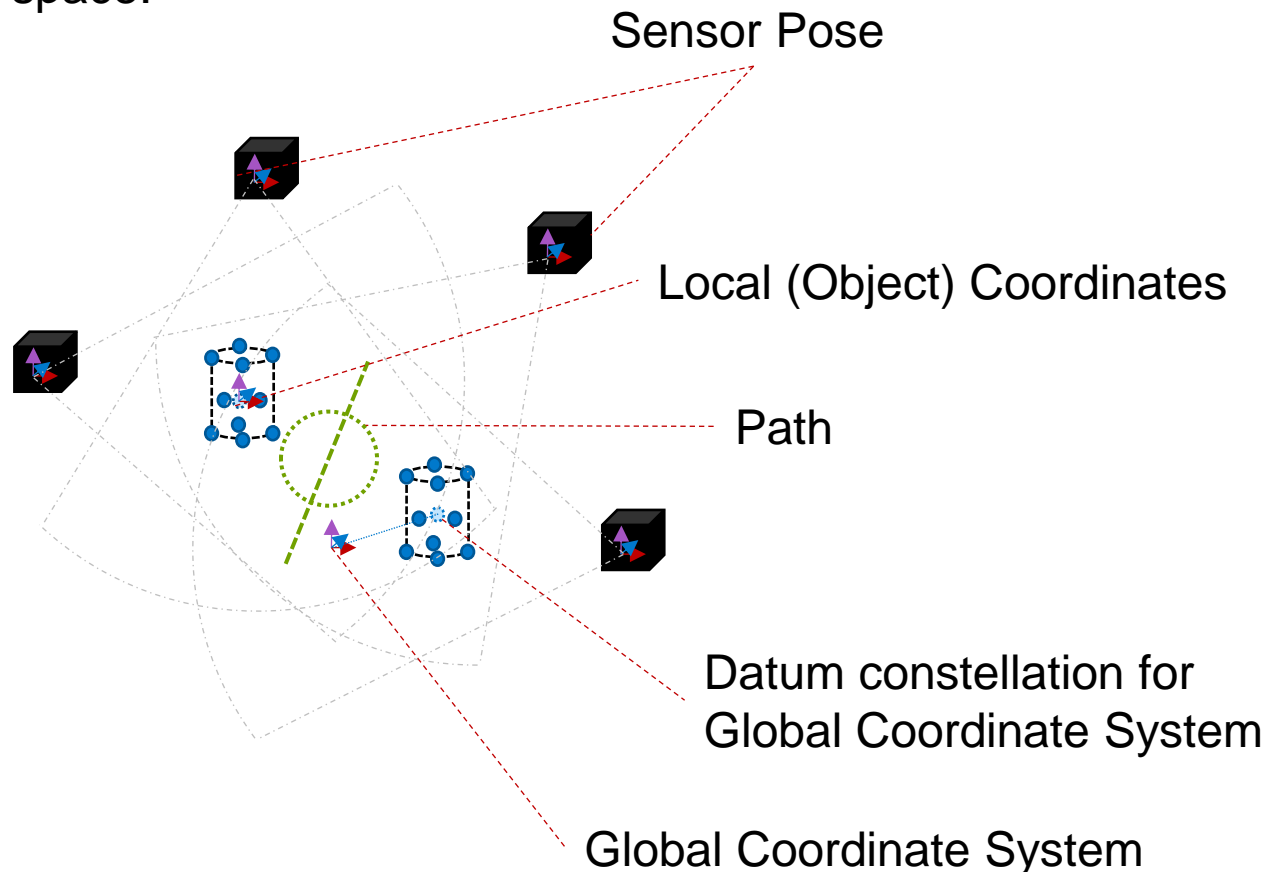
**Actual Path:** in real space

- Dynamic errors,
- Steady state errors,
- Temporal error,
- Kinematic error,
- Environmental error.

**Measured Path:** in measurement space

# Method : Path Selection

A distributed measurement system may not have a convenient set of intrinsic coordinates. The mapping of real space,  $\mathbb{R}^3$ , into measurement space is complex. A linear path in  $\mathbb{R}^3$  is not a linear path through measurement space.



Pros/Cons of Linear vs Circular Path	
Linear Path	Circular Path
Absolute distance can be measured (with calibration).	Absolute distance is fixed around a point.
Additional length is needed for acceleration and damping/decay of oscillation → limits maximum speed.	Can set up continuous rotatory motion - high achievable speed.
Orientation in $\mathbb{R}^3$ is nominally fixed.	Orientation in $\mathbb{R}^3$ is constantly changing.
Large lengths can be impractical and are susceptible to mechanical and thermal effects.	Large radii are impractical and likely less than can be achieved using a linear path.
Calibration of orientation perpendicular to the path can be challenging.	Calibration of circular path should be easier than a linear path.
Gravity is constancy direction.	Gravity is continuously changing direction.

# Reference Artifact Design

\*Please, join us at our poster on artefact design for further discussion

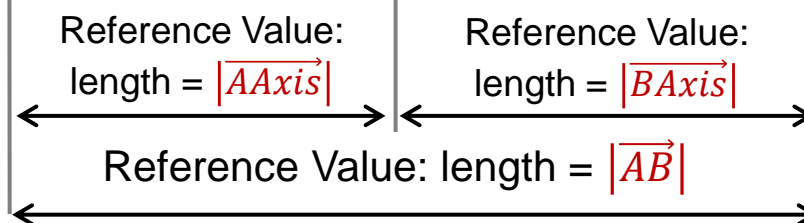
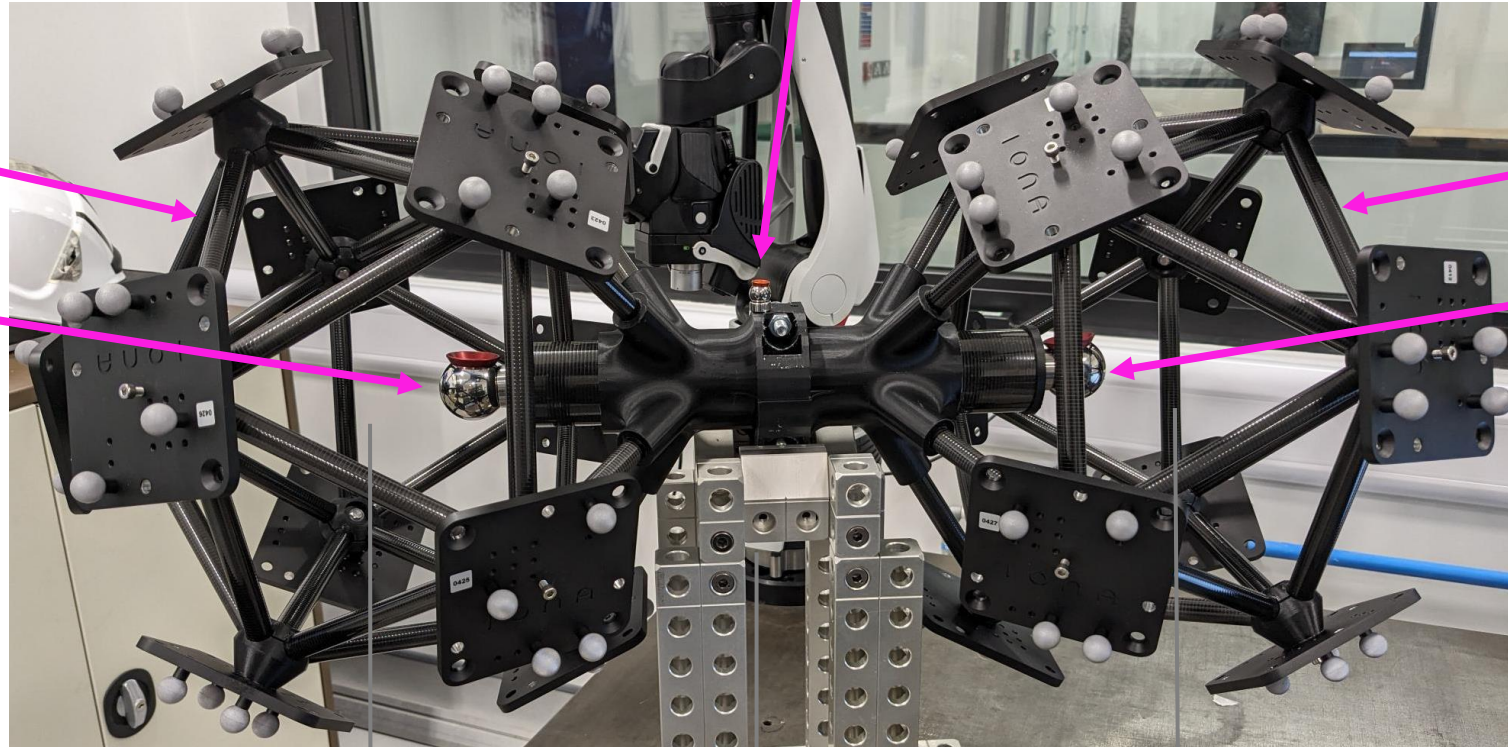
SMR. C

Constellation A

Constellation B

SMR. A

SMR. B

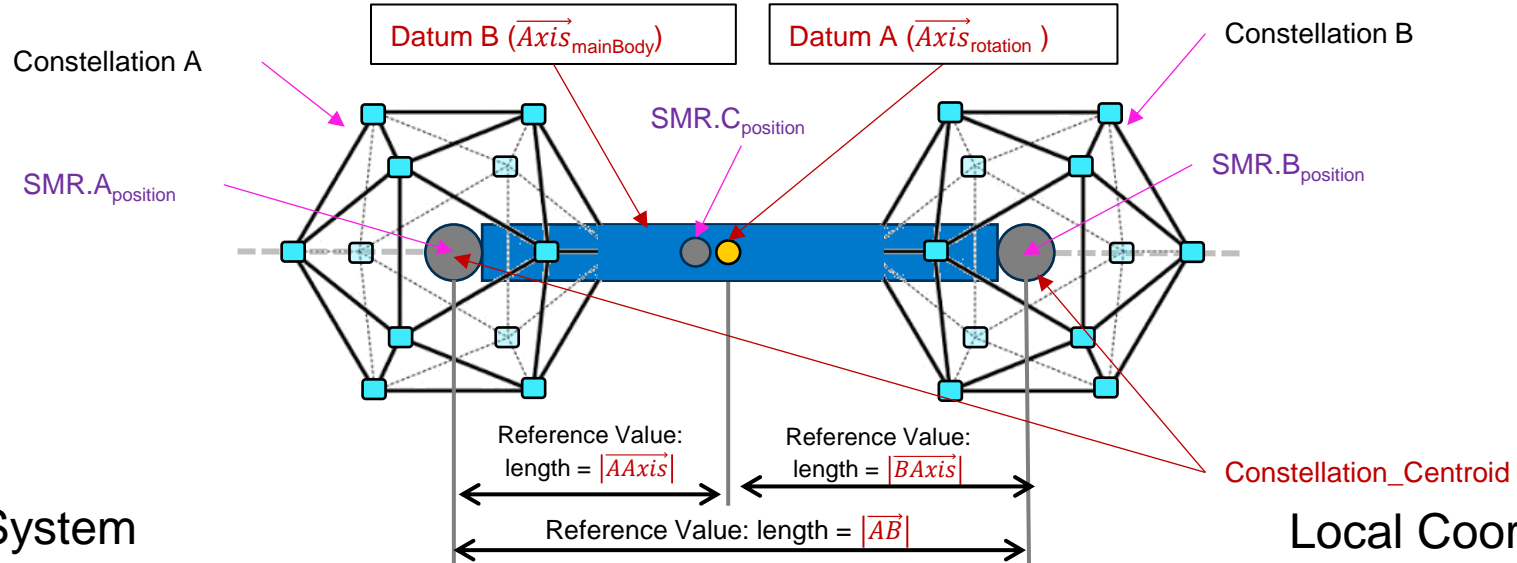


- ❖ Outer targets will be moving faster than inner targets
- ❖ It may be difficult to accurately measure a sensor/constellation centroid for traceable measurement



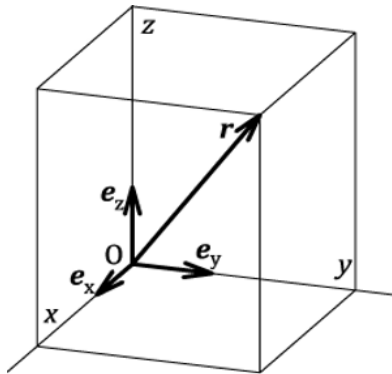
# Reference Artifact Design

## Conversion Between Local coordinate System and Global Coordinate System



### Global Coordinate System

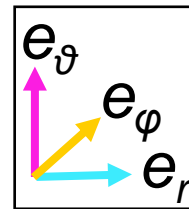
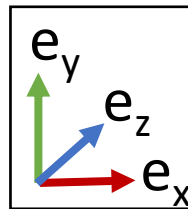
Cartesian Coordinates  
ISO/IEC 80000



Coordinate:  $x, y, z$   
Positional Vector:  $r = x e_x + y e_y + z e_z$   
Differential of Pos. Vector:  $dr = dx e_x + dy e_y + dz e_z$

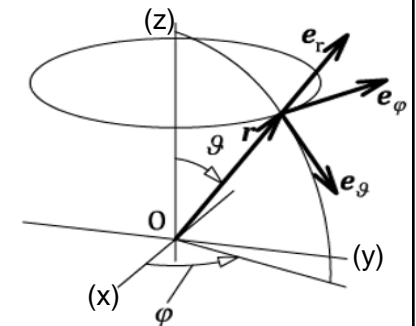
$$\vec{Axis}_{rotation} = P_{AxisGlobal}(x, y, z), \vec{Axis}(x e_x, y e_y, z e_z)$$

$$\vec{Axis}_{rotation} = P_{AxisLocal}(r, \vartheta, \varphi), \vec{Axis}(e_\vartheta)$$



### Local Coordinate System

Spherical Polar Coordinates  
ISO/IEC 80000

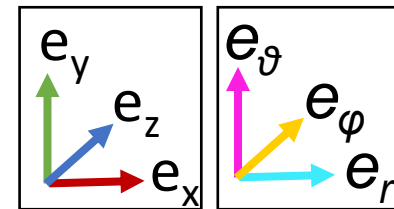
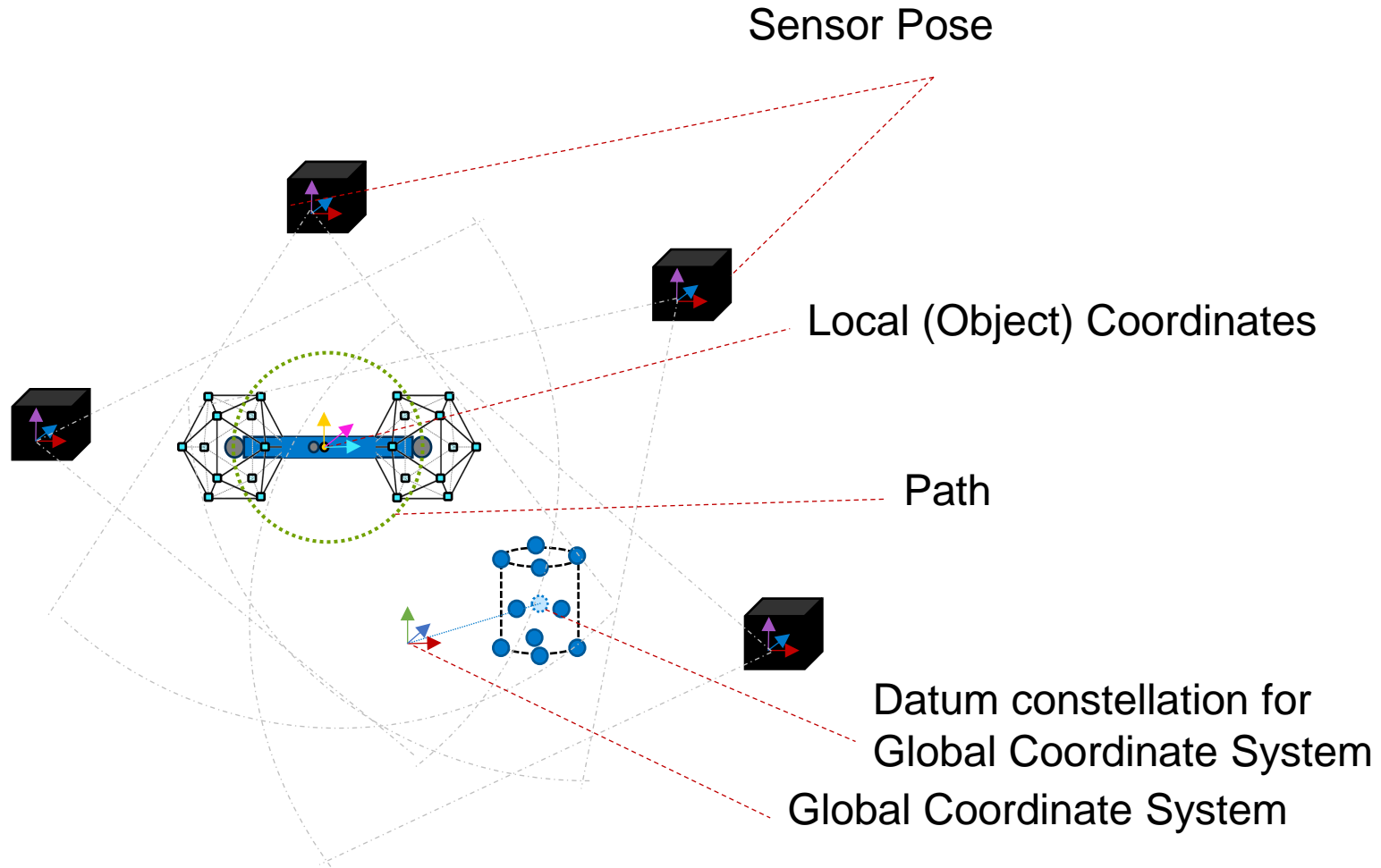


radial distance:  $r \geq 0$ ,  
polar angle:  $0^\circ \leq \vartheta \leq 180^\circ$   
azimuth:  $0^\circ \leq \varphi < 360^\circ$

Coordinate:  $r, \vartheta, \varphi$   
Positional Vector:  $r = r e_r$   
Differential of Pos. Vector:  $dr = dr e_r + r d\vartheta e_\vartheta + r \sin\vartheta d\varphi e_\varphi$

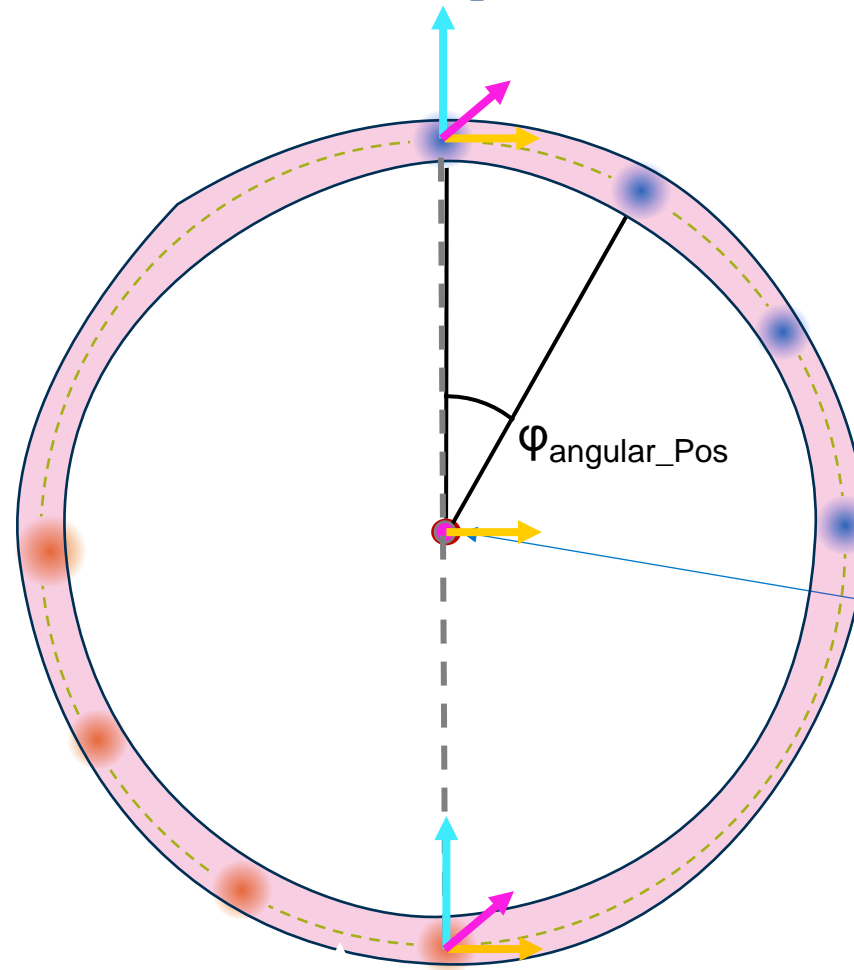
# Reference Artifact Design

## Conversion Between Local coordinate System and Global Coordinate System



# Data Collection Protocol: Stop/Start

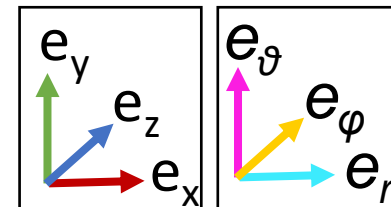
- Actuator provides nominal value for angular position,  $\varphi_{\text{angularPos}}$
- Zero point of  $\varphi_{\text{angularPos}}$ , i.e. when  $x_{\text{const.A}} = x_{\text{const.B}}$
- $\overrightarrow{Axis}$  must be determined in the Global coordinate system to represent results in  $(x, y, z)$ 
  - Can be derived from the measurement data.
  - Can be determined independently using a registered reference measurement system.
- Path can be determined using;
  - Circle fitting: incorporates *a priori* information on the path in  $\mathbb{R}^3$ .



Axis of Rotation

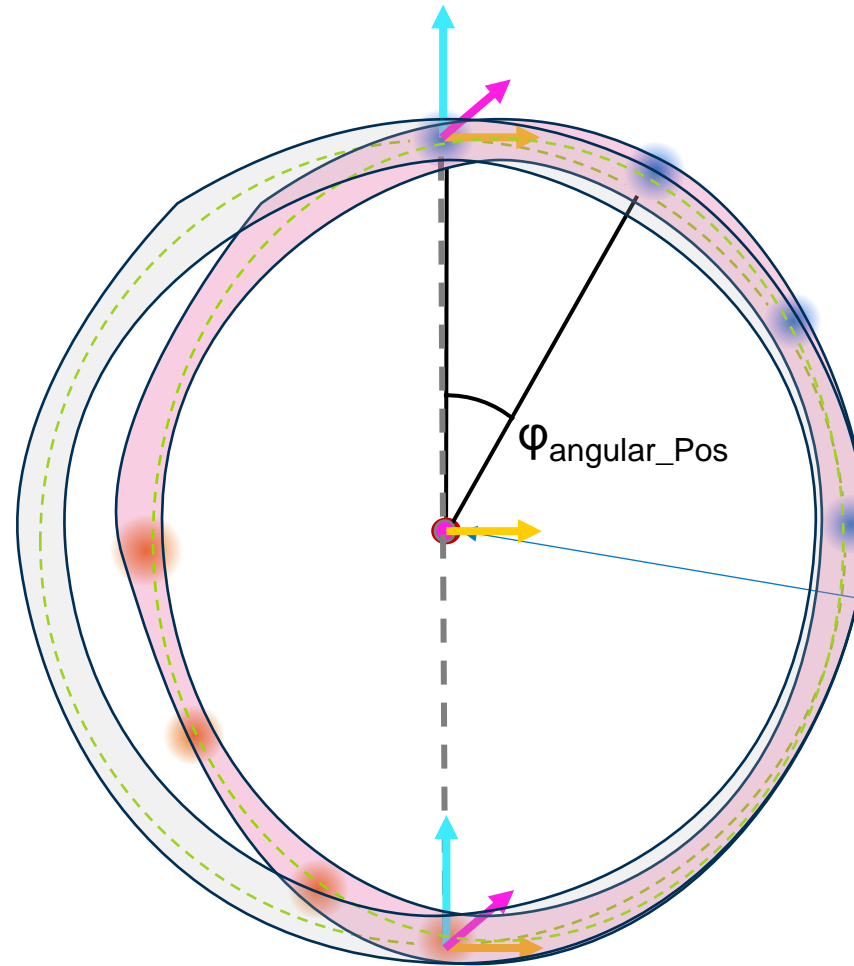
$$= P_{\text{AxisGlobal}}(x, y, z), \overrightarrow{Axis}(x e_x, y e_y, z e_z)$$

$$= P_{\text{AxisLocal}}(r, \theta, \varphi), \overrightarrow{Axis}(e_\theta)$$

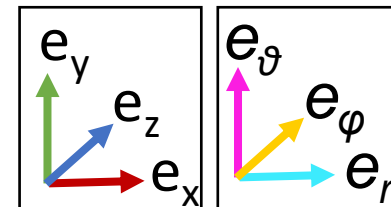


# Data Collection Protocol: Stop/Start

- Path can be determined using;
  - Circle fitting: incorporates *a priori* information on the path in  $\mathbb{R}^3$ .
  - Interpolation: working purely in measurement space.

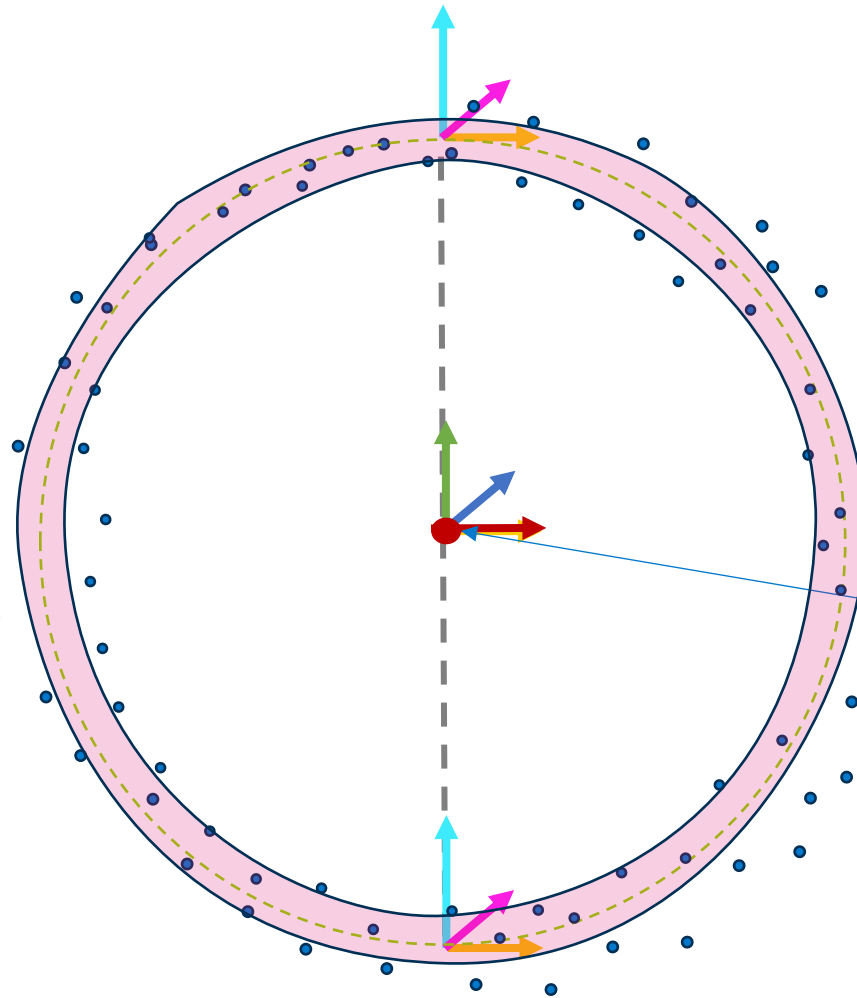


Axis of Rotation  
 $= P_{\text{AxisGlobal}}(x, y, z), \overrightarrow{Axis}(xe_x, ye_y, ze_z)$   
 $= P_{\text{AxisLocal}}(r, \theta, \varphi), \overrightarrow{Axis}(e_\theta)$



# Data Collection Protocol: Continuous

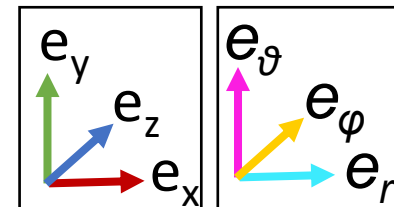
- Continuous measurement requires temporal synchronisation with the system under test.
- Errors are parameterised as deviation from path,
  - $e_r, e_\vartheta, e_\varphi$  are orthonormal basis vectors representing the intrinsic coordinates of the path.
  - Velocity is a scalar multiplied by  $e_\varphi$ .



Axis of Rotation

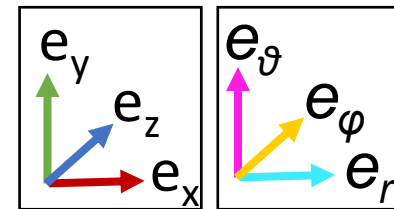
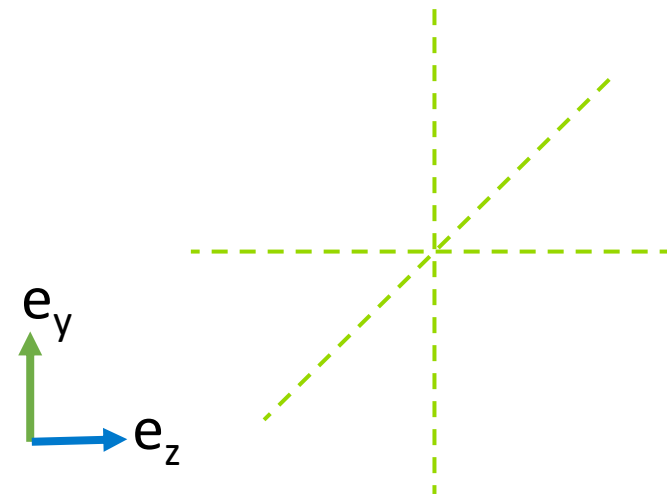
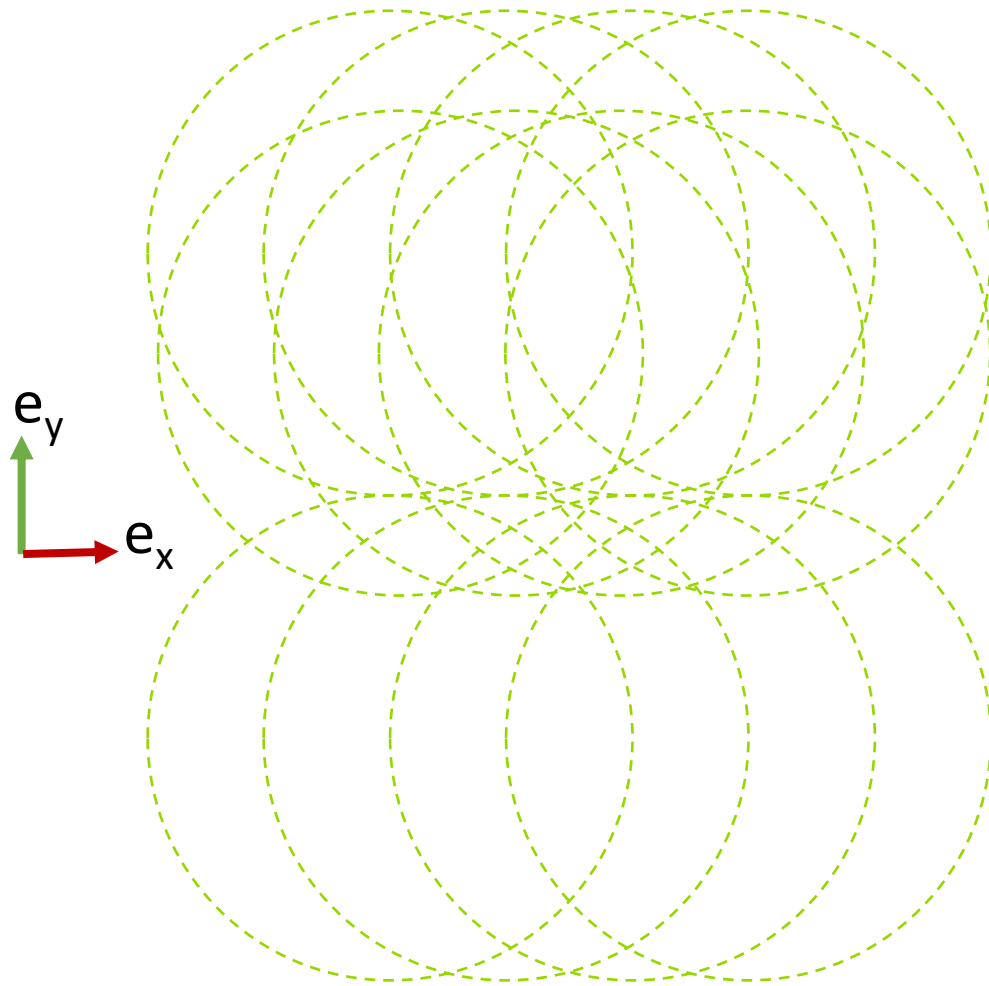
$$= P_{\text{AxisGlobal}}(x, y, z), \overrightarrow{\text{Axis}}(xe_x, ye_y, ze_z)$$

$$= P_{\text{AxisLocal}}(r, \theta, \varphi), \overrightarrow{\text{Axis}}(e_\varphi)$$



- ❖ Method requires an in-situ comparator system to measure absolute position
- ❖ Circular motion may not replicate the intended use case for manufacturing processes
- ❖ The measured performance of a system is not localised as test takes up space.

# Data Collection Protocol: Mapping




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UK Research and Innovation

*'Creating the new machines, technology, and skills needed to manufacture tomorrow's products'*



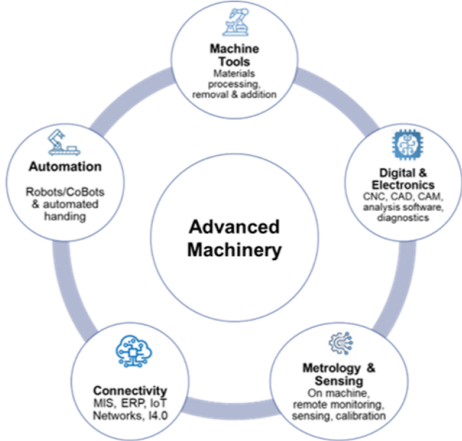
AMPI  
THE ADVANCED MACHINERY & PRODUCTIVITY INSTITUTE

## The Advanced Machinery & Productivity Institute

**AMPI is an industry led initiative** to stimulate and support rapid growth of the UK's machinery manufacturing sector, designed to support a coherent supply chain from research through to implementation.

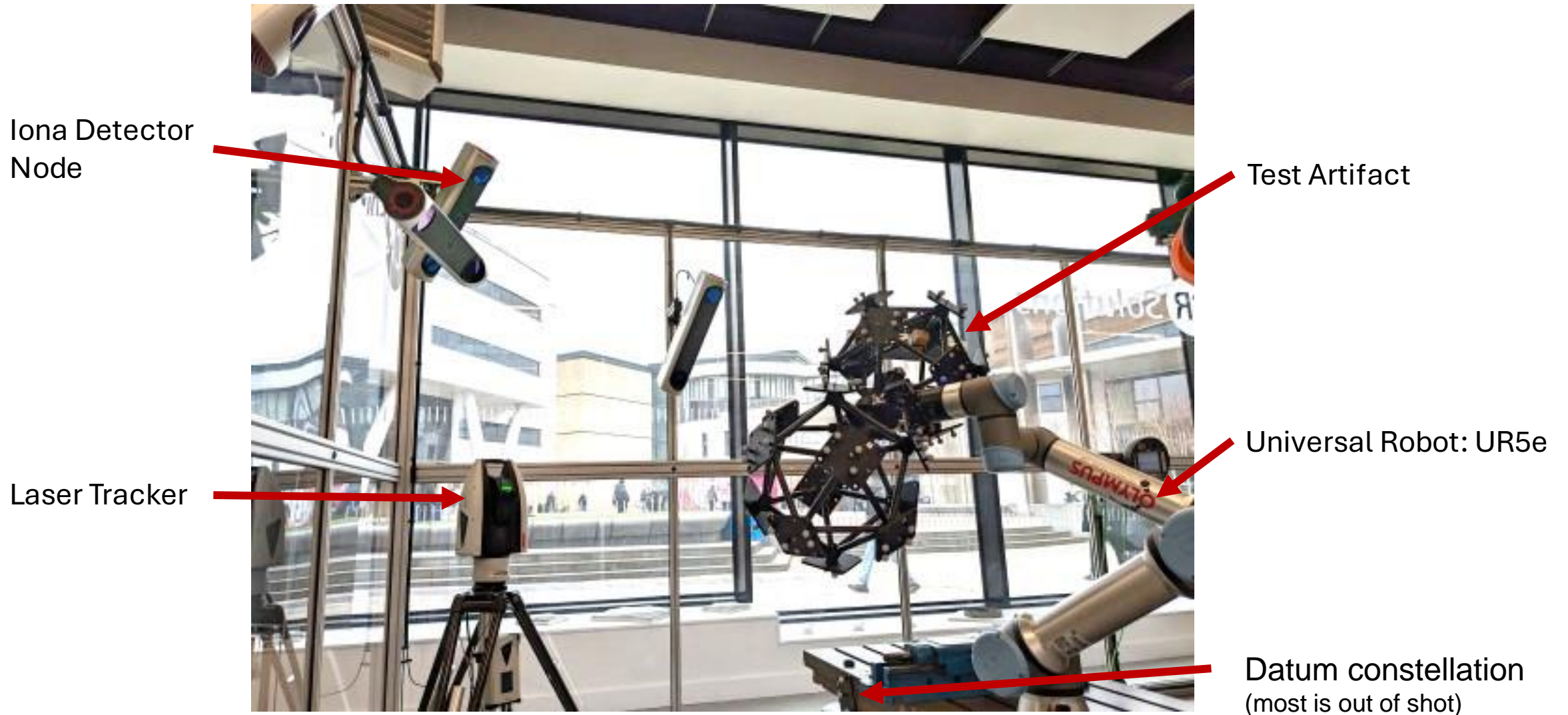
Through partnership between industry, local government, higher education institutions and NPL, AMPI will deliver:

- **Increased competitiveness** and productivity of the machinery sector
- Wider access to **advanced machinery expertise**
- Regional **employment opportunities**, including post doctorates and apprenticeships
- Support for the **commercialisation of new machines**, related technologies and know-how



The diagram illustrates the components of Advanced Machinery. At the center is a circle labeled 'Advanced Machinery'. Surrounding it are five smaller circles, each representing a key area: 'Machine Tools' (Materials processing, removal & addition), 'Digital & Electronics' (CNC, CAD, CAM, analysis software, diagnostics), 'Metrology & Sensing' (On machine, remote monitoring, sensing, calibration), 'Connectivity' (MIS, ERP, IoT Networks, I4.0), and 'Automation' (Robots/CoBots & automated handling).

# Data Collection





# Data Collection Protocol

Time →

Stop/Start Protocol

- 51 positions (1 and 51 were nominally identical)
- Repeat protocol (9 repeats)

Dynamic Protocol

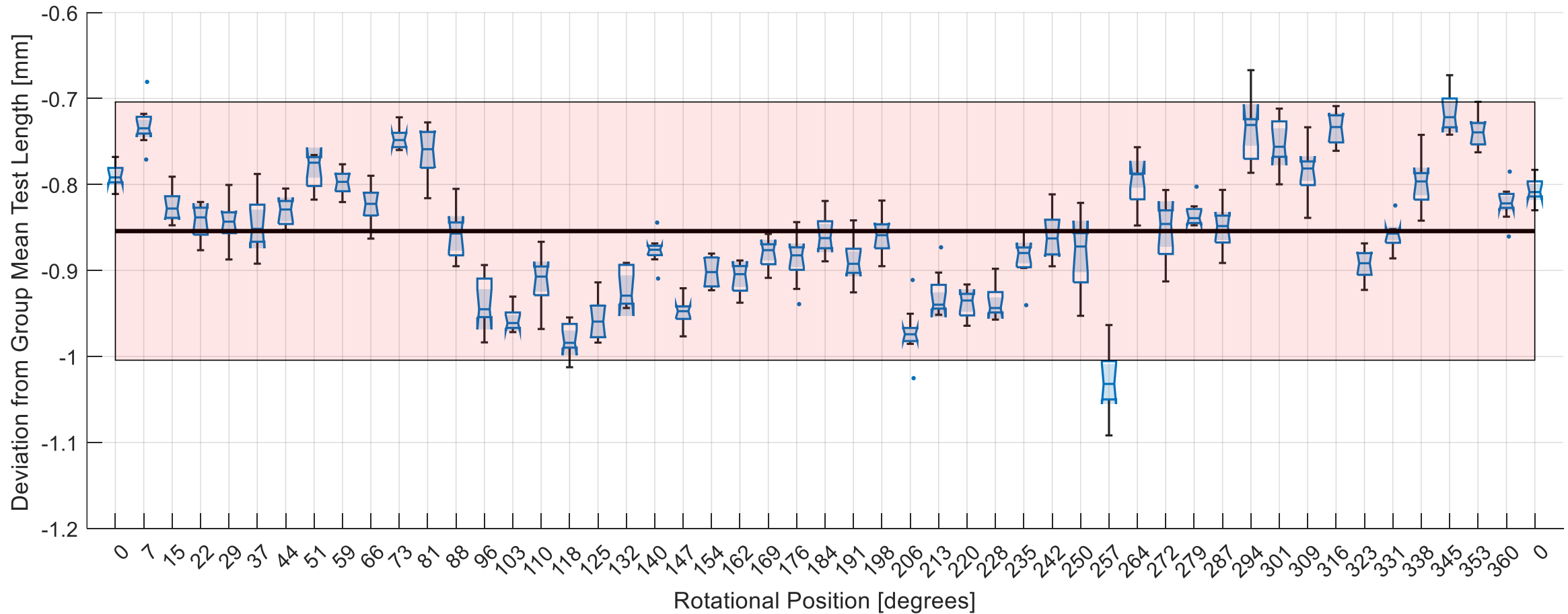
- Data collected over a range of angular speeds.

Test Matrix

Protocol	n	Laser Tracker	Angular Speed (rads s <sup>-1</sup> )	Positions	Samples Per Position
Stop/Start	3	A (Constellation A)	0.0	51	60
Stop/Start	3	B (Constellation B)	0.0	51	60
Stop/Start	3	C	0.0	51	60
Dynamic	5	C	0.2, 0.4, 0.6, 0.8, 1.0	-	1
Return	3	A (Constellation A)	0.4	20	1
Return	3	B (Constellation B)	0.4	20	1
Return	3	C	0.4	20	1

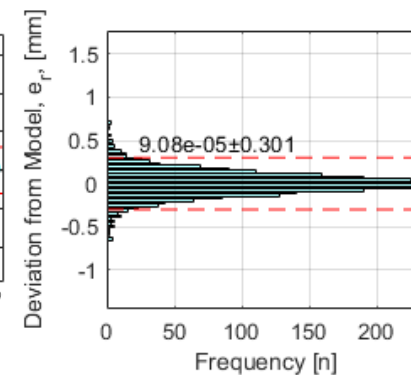
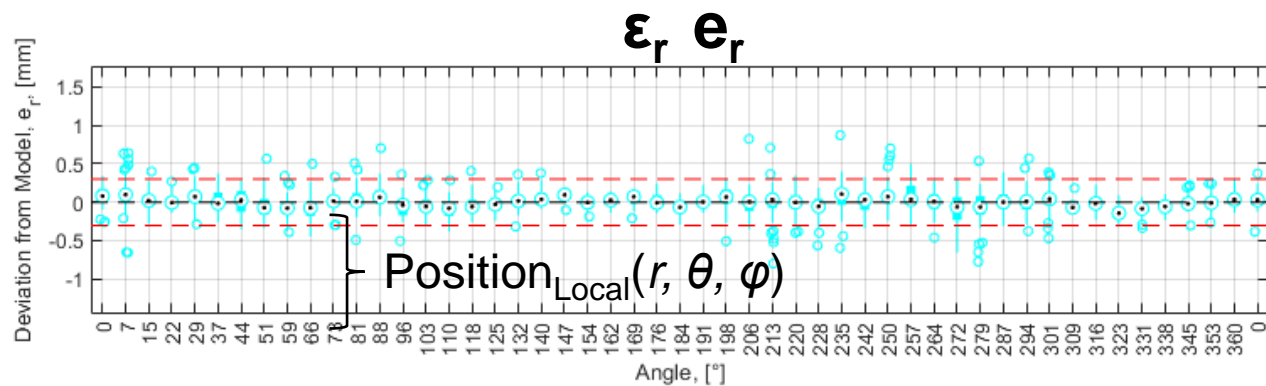
- 9 repeat tests using the stop/start protocol
  - The laser tracker measures 3 different target locations.
- 9 continuous motion tests using the same angular speed
  - These interleaved with the Stop/Start tests as they are taken as the actuator return to its start position.

# Comparison to Reference Value: $\text{length} = |\overrightarrow{AB}|$

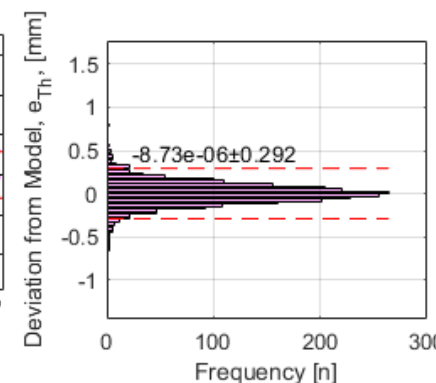
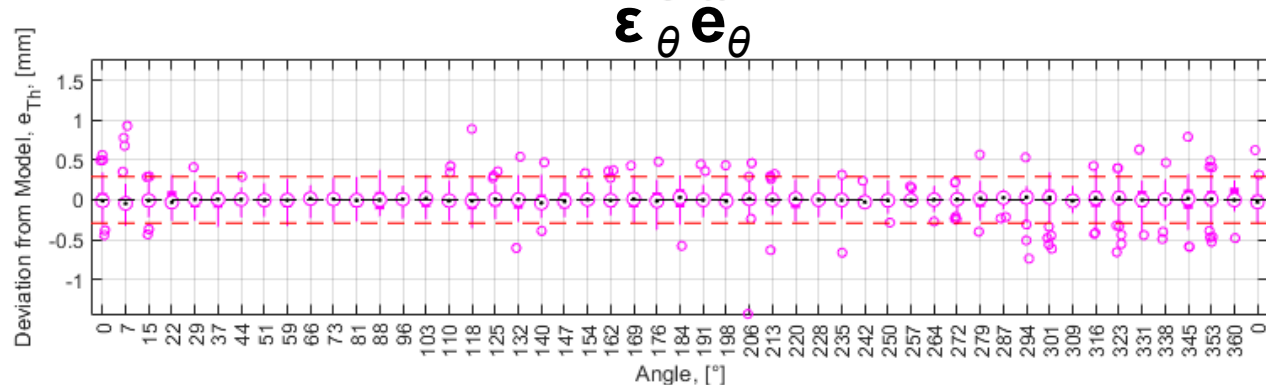


Reference Value:  $\text{length} = |\overrightarrow{AB}|$

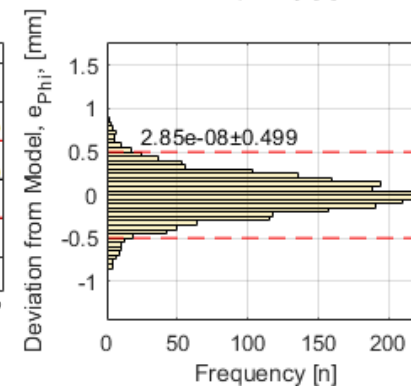
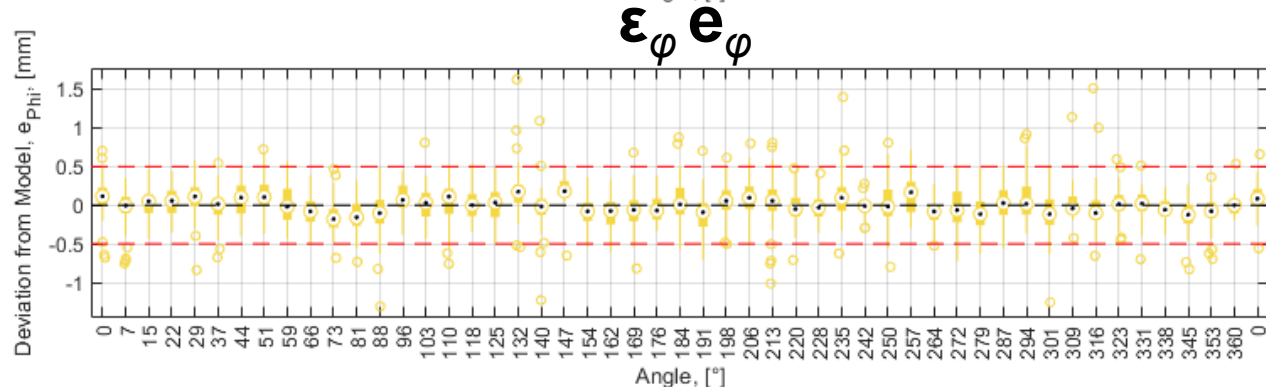
# Position<sub>Local</sub>( $r, \theta, \varphi$ )



$$\epsilon_r = e^{-4} \pm 0.30 \text{ mm, } k=2, \text{ norm}$$



$$\epsilon_\theta = e^{-4} \pm 0.29 \text{ mm, } k=2, \text{ norm}$$

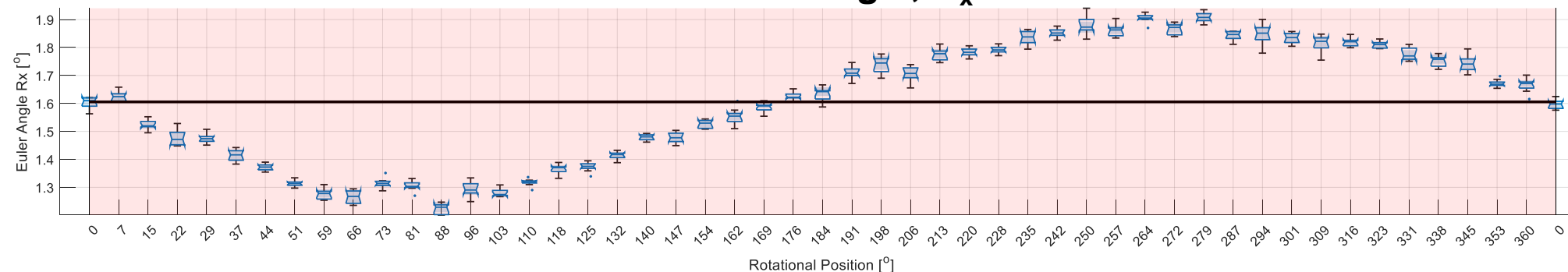


$$\epsilon_\varphi = e^{-8} \pm 0.50 \text{ mm, } k=2, \text{ norm}$$

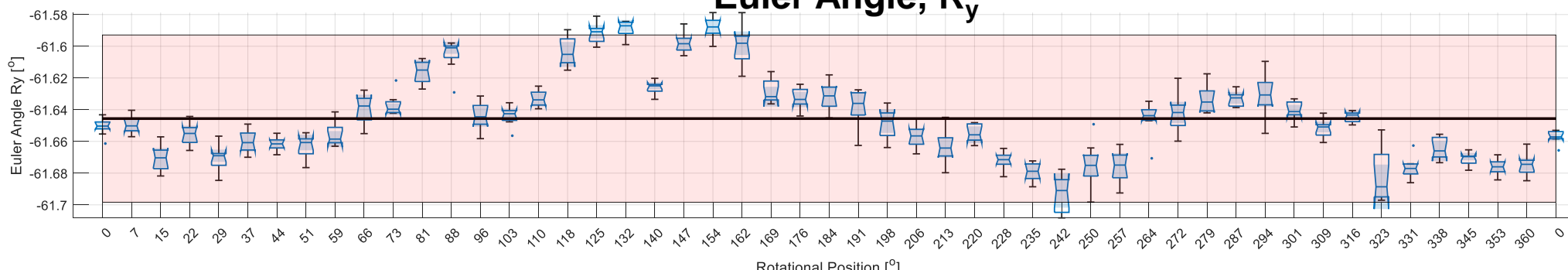
# Orientation<sub>Global</sub> [Rx, Ry, Rz]

## Euler Angle, $R_x$

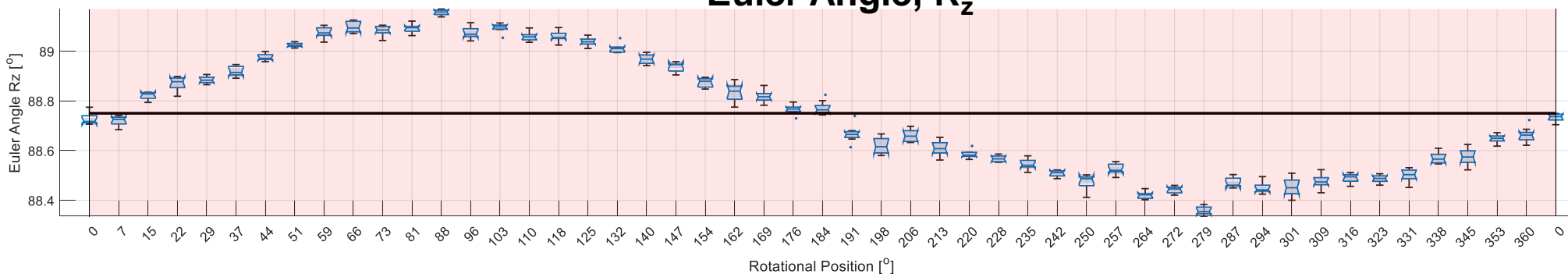
$\epsilon$ , standard error on the mean



## Euler Angle, $R_y$



## Euler Angle, $R_z$



# Summary and Ongoing Work

- A method of quantifying the dynamic performance of a distributed large volume metrology system has been presented aimed at addressing metrological challenges on the horizon of automation.
- The method accommodates multiple levels of comparison;
  - comparison of a systems' static performance against its dynamic performance.
  - comparison against a calibrated length.
  - comparison against an alternative 3 DOF(or more) system.
- Controlled test variables include; position, orientation, velocity, and time
- A prototype artefact has been built for proof of concept with promising results, however;
  - rigidity must be improved.
  - greater velocities need to be achieved (at least 3 ms<sup>-1</sup>).

## Work is ongoing

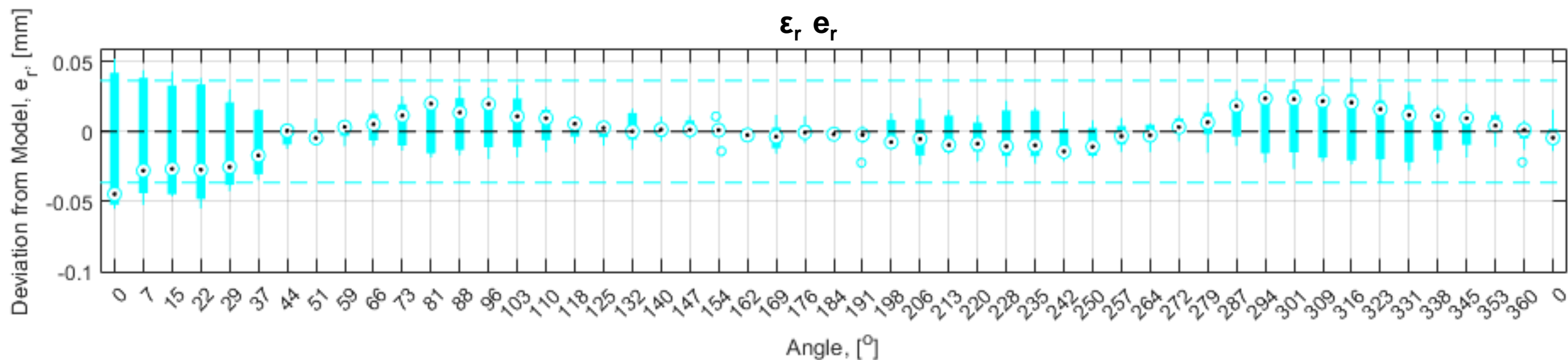
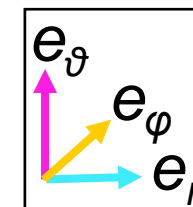
- Iterate the artefact design : increased rigidity, incorporate precision rotational actuator.
- Show system performance as a function of angular velocity.
- Creation of a kinematic model to quantify and potentially correct for errors.
- Robust test uncertainty estimation.
- Sensitisation of the artefact



[npl.co.uk](http://npl.co.uk)

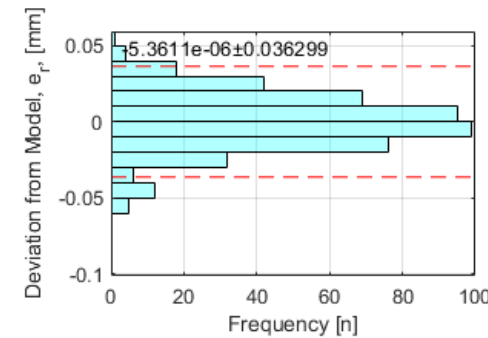
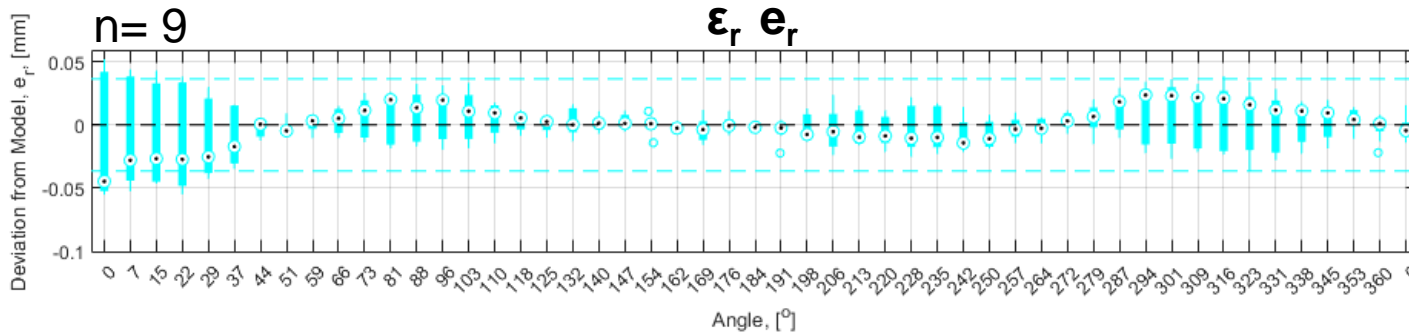
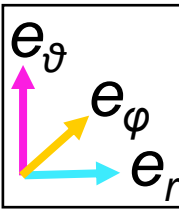
# Deviation from Path: Comparator System

Path : Fit circle

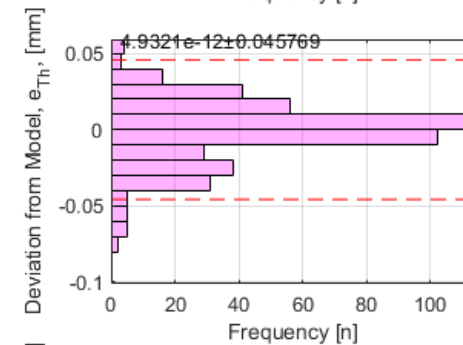
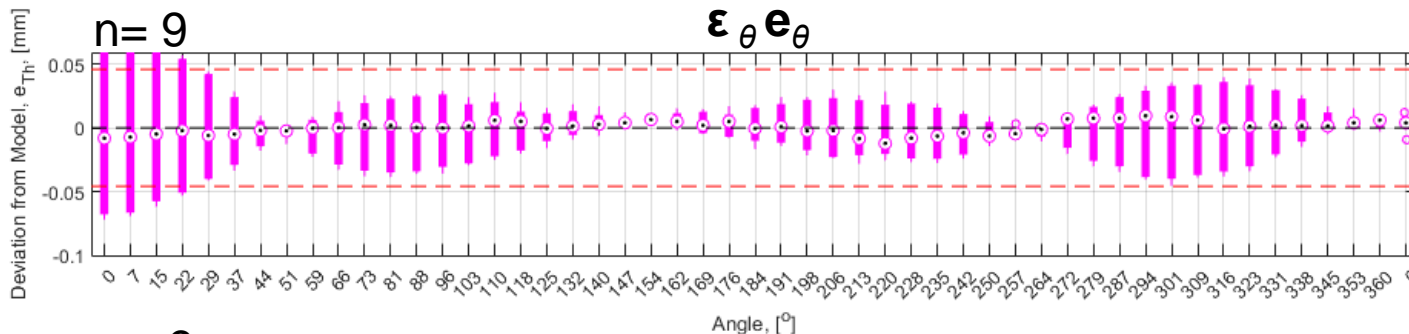


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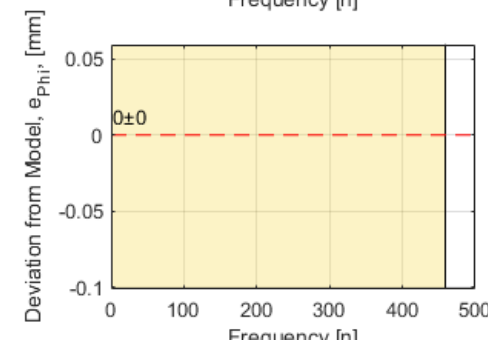
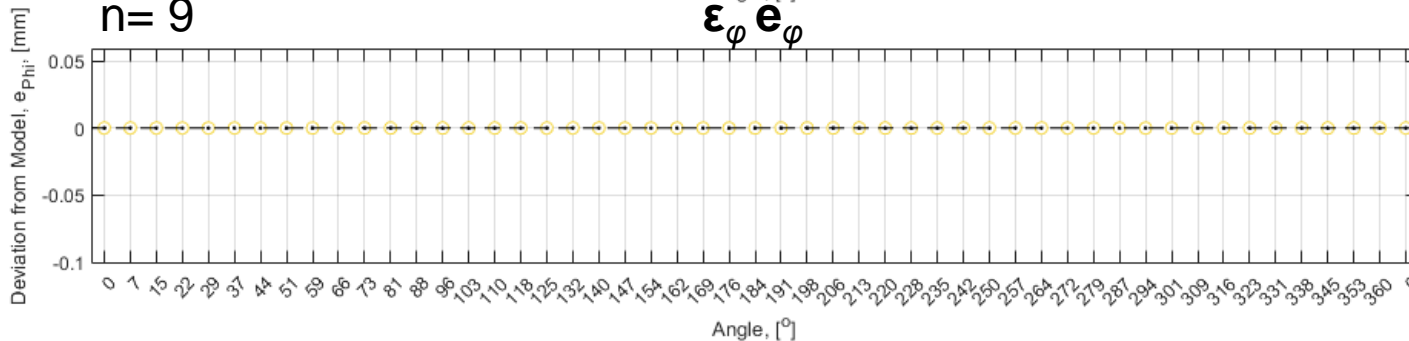
## Path : Fit circle



$e-6 \pm 0.036, k=2, \text{norm}$



$e-12 \pm 0.046, k=2, \text{norm}$



$\theta \pm 0.0, k=2, \text{norm}$

Data from the SMR placed ~coincident with the centroid of Constellation A

Data collection method used: "stable point", hence no distribution for  $\phi$ . Method should not require repeat runs of the stop/start protocol



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