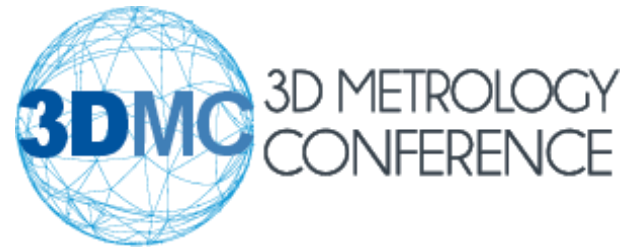


Radio Telescope Inspection by Terrestrial Laser Scanner

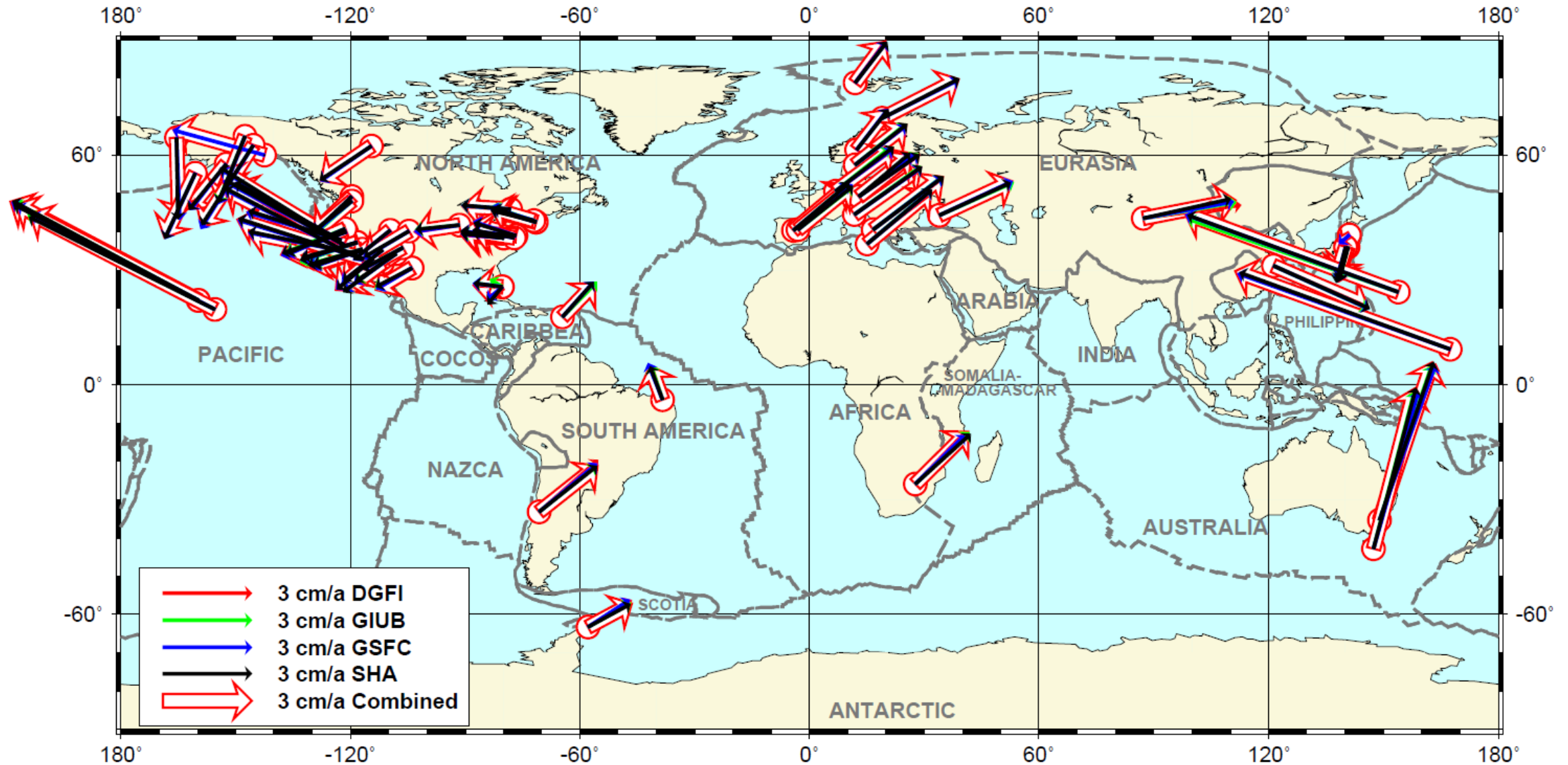


10./11. October 2017, Aachen, Germany

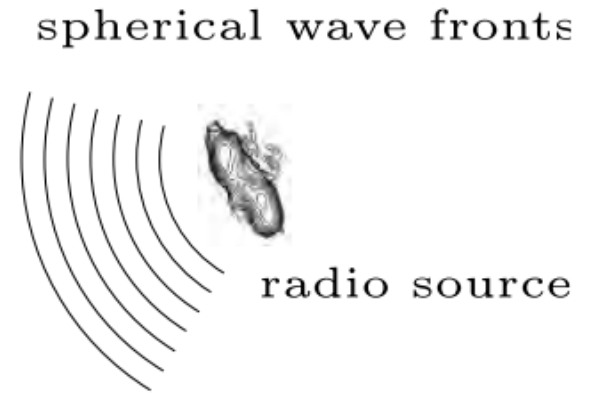
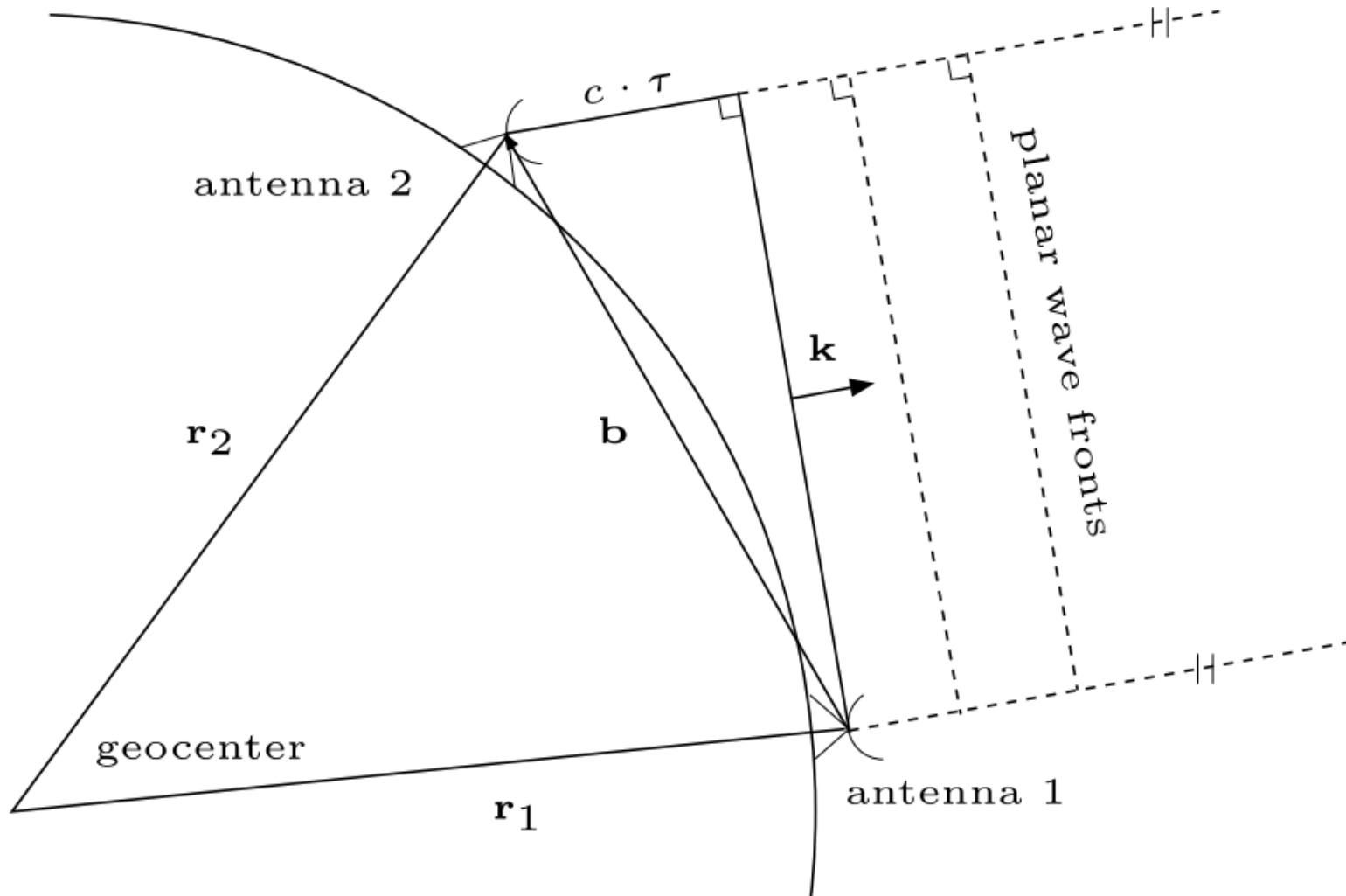
Dr.-Ing. Christoph Holst
University of Bonn, Germany

- **Institute of Geodesy and Geoinformation**
- B.Sc. / M.Sc. Geodesy and Geoinformation (German)
- M.Sc. Geodetic Engineering (English)
- Geodetic metrology
- Industrial metrology
- Data processing & accuracy analyses
- **... and also: global geodesy**









$$\tau = t_2 - t_1 = -\frac{1}{c} \cdot \mathbf{b} \cdot \mathbf{k}$$

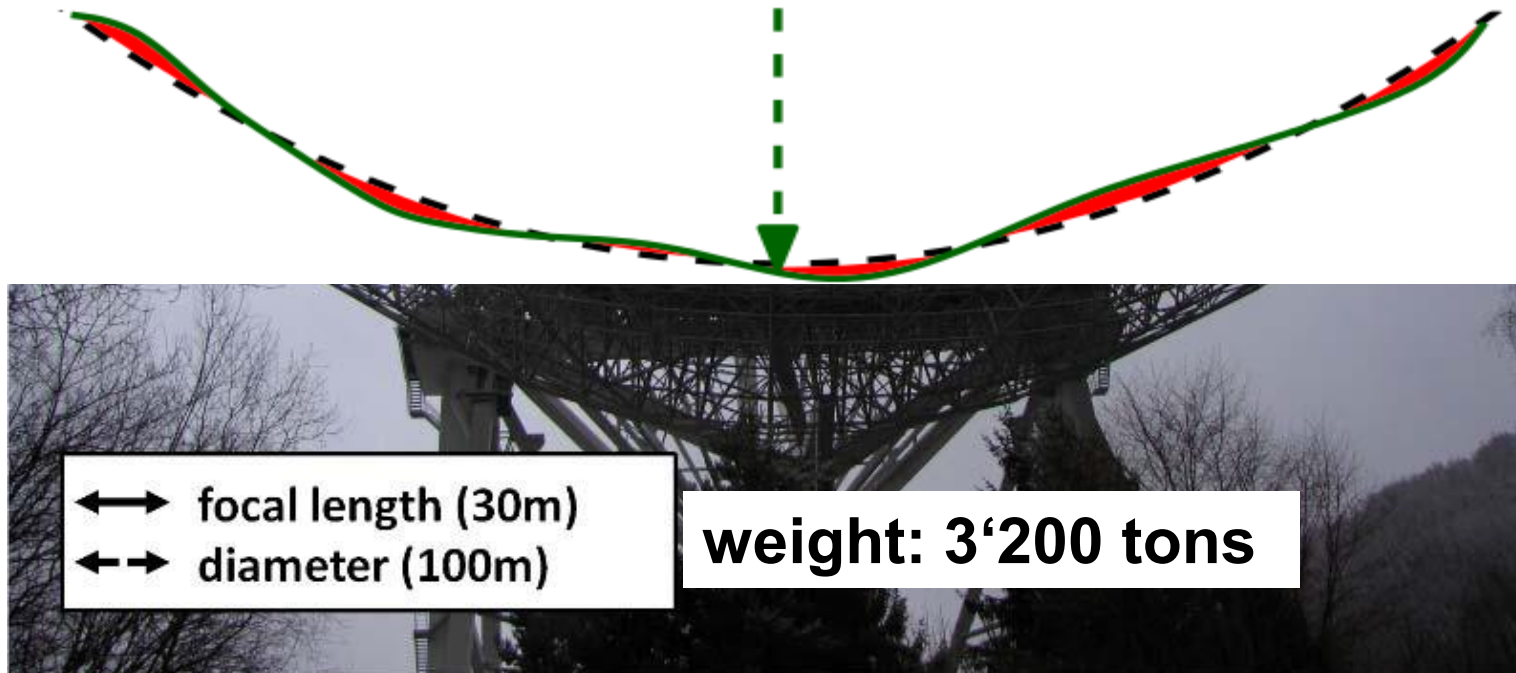
$$\sigma_b \leq 1\text{mm}$$



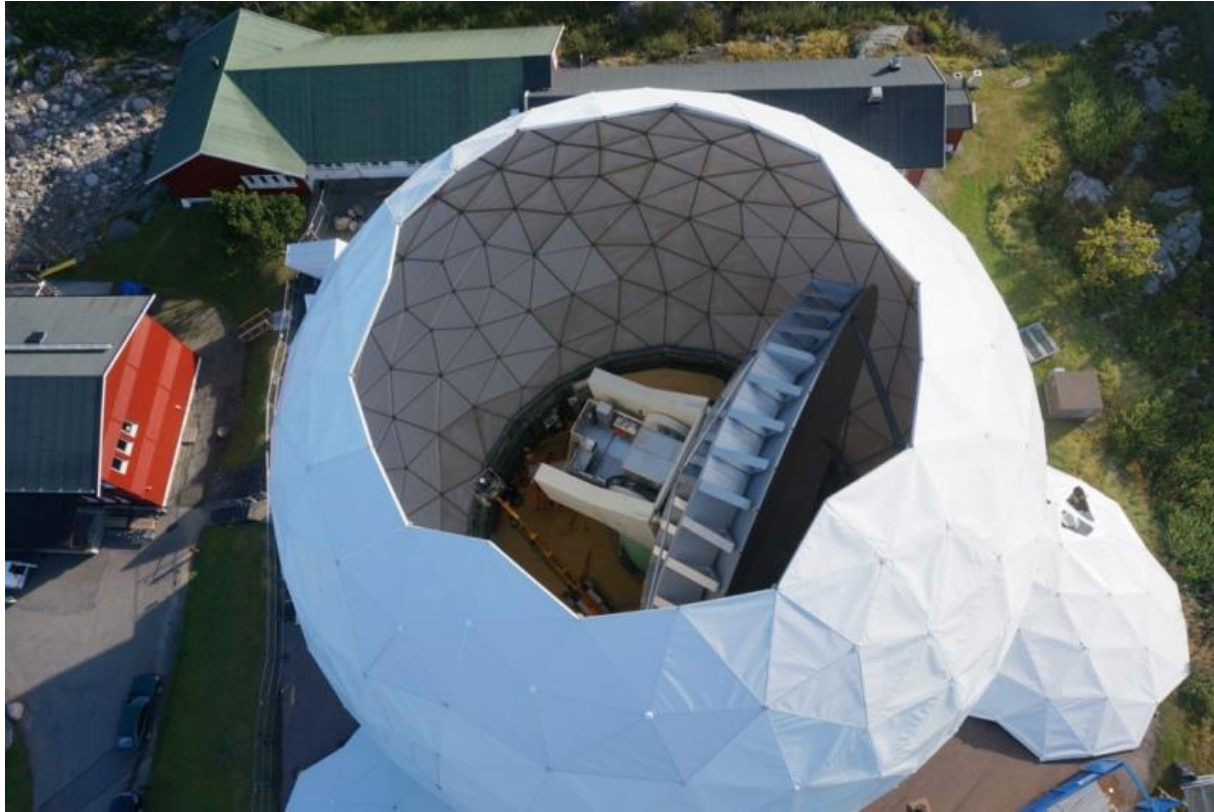
Assumption:
**shape = rotational
paraboloid**

Searched for:
**focal length +
local deformations**

... that depend on
elevation angle





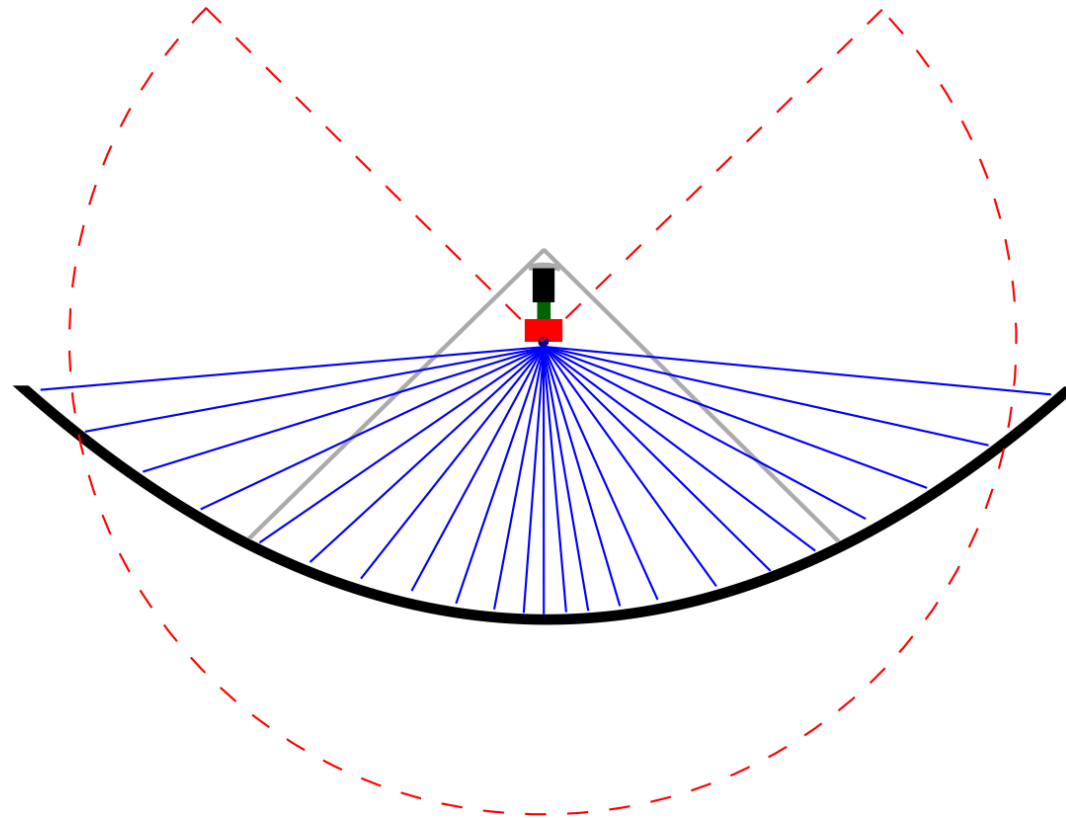


Diameter of 20m
 Enclosed by a radome
 Surface smooth

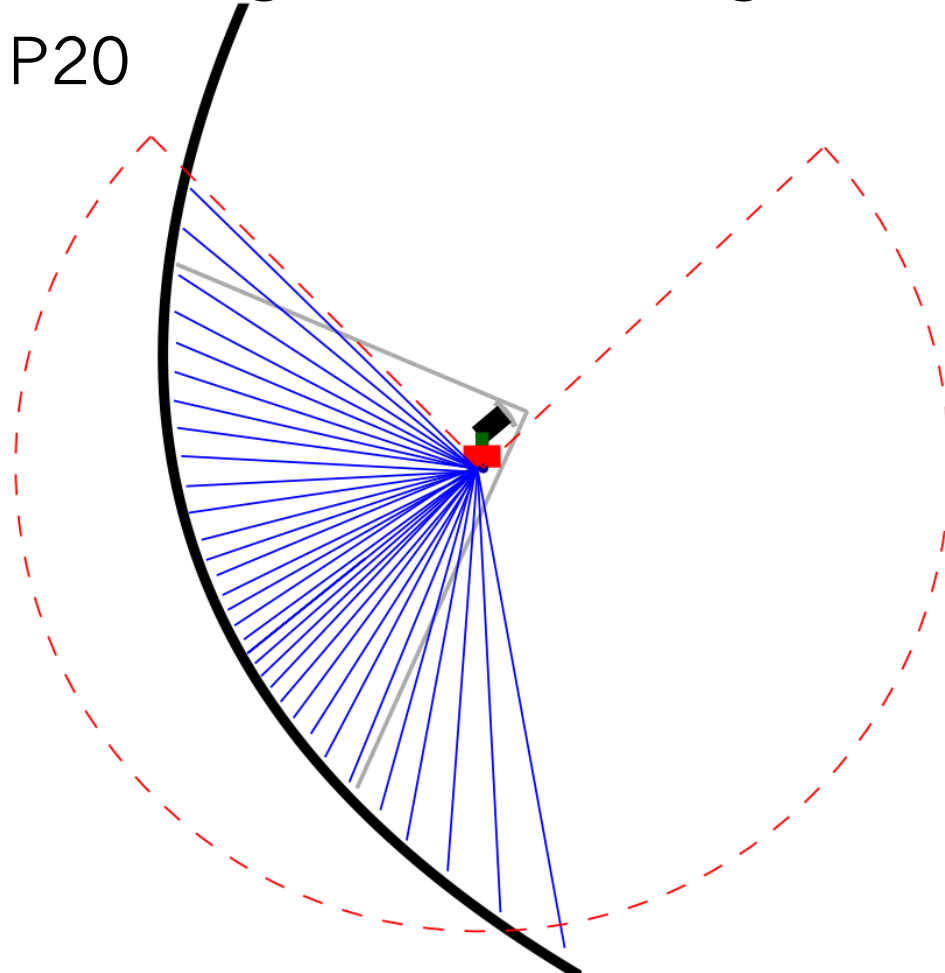
Diameter of 100m
 Subject to wind and weather
 Surface more rough



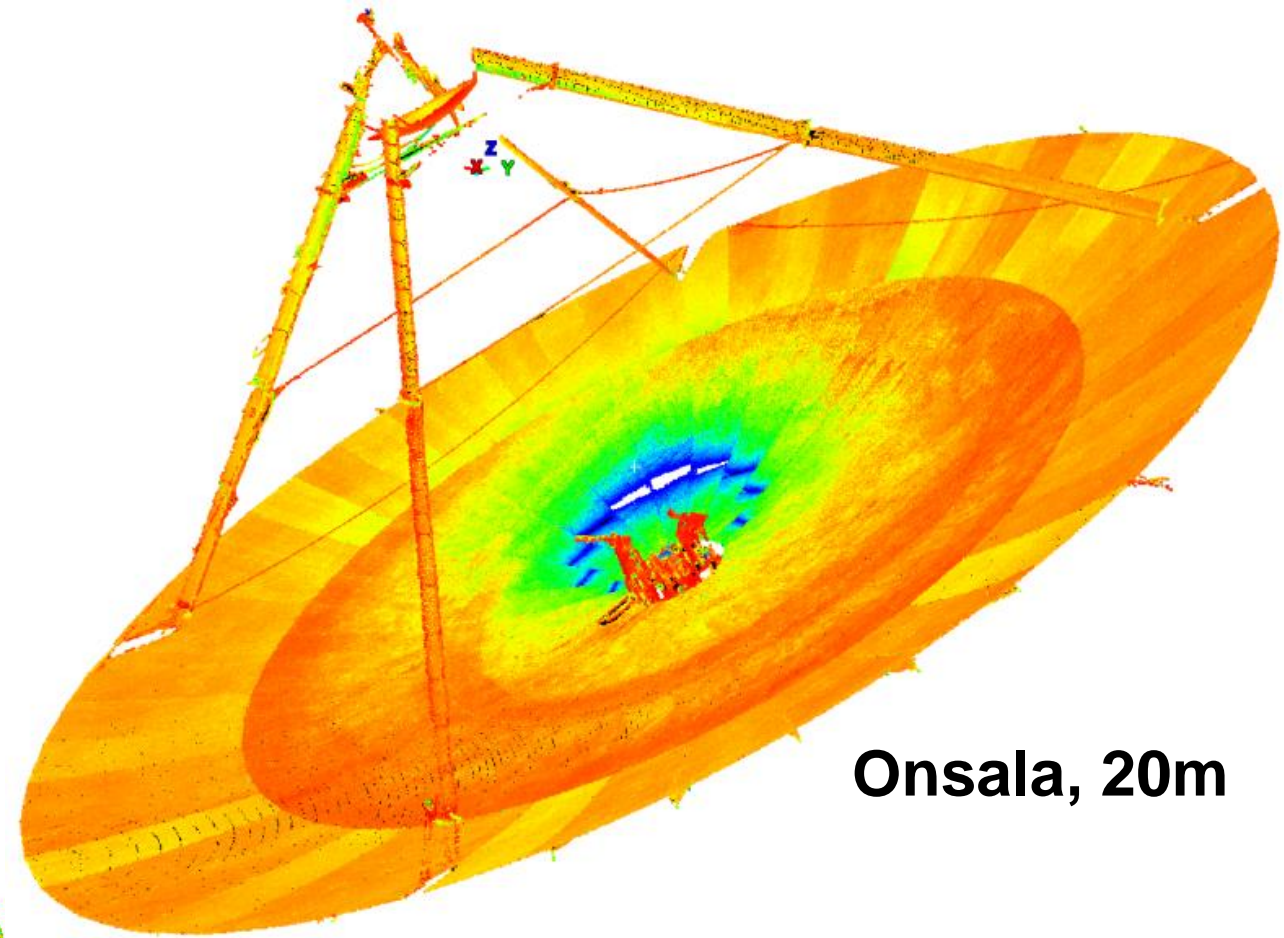
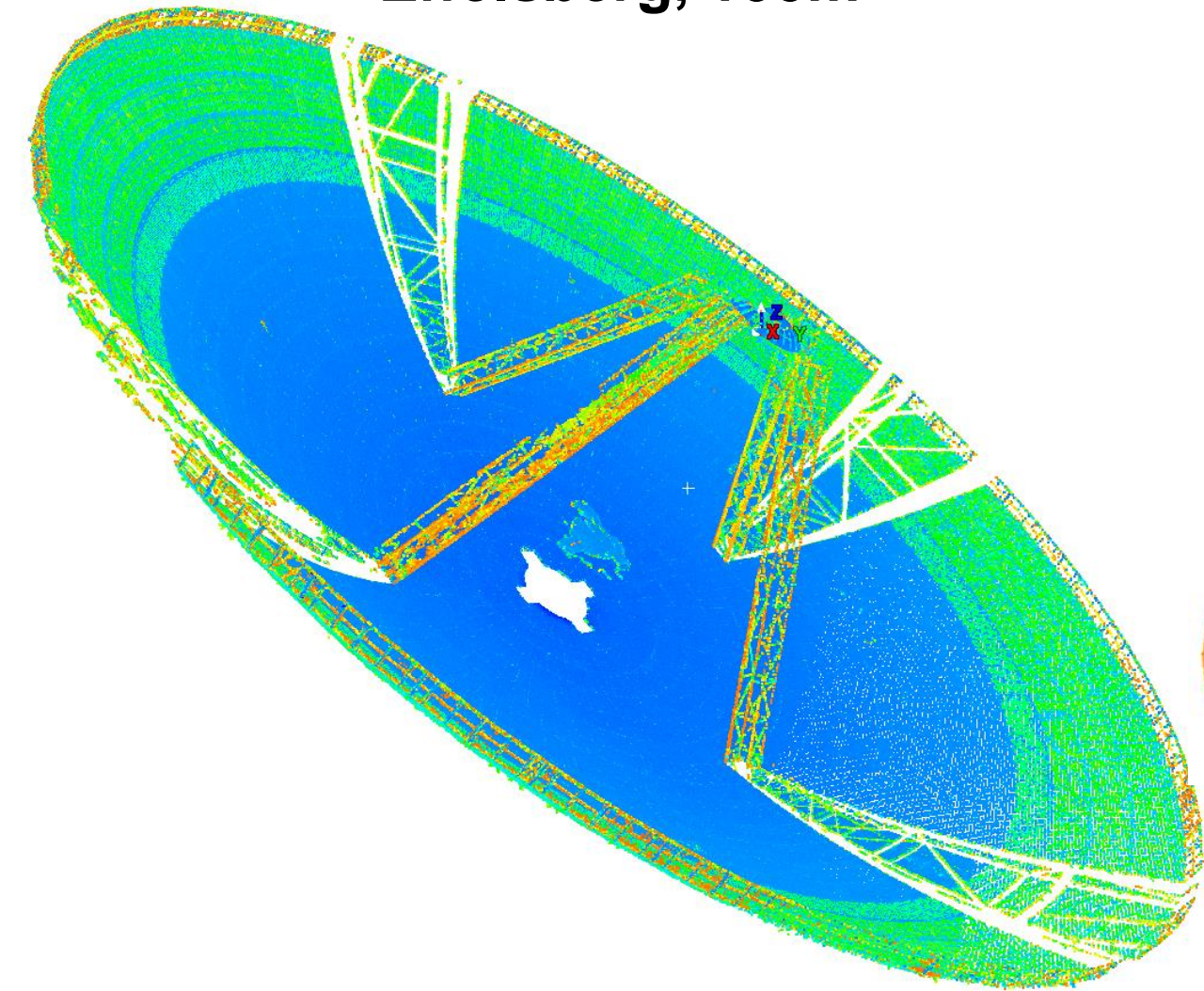
- Overhead station: good incidence angles, no obstruction
- Scanning at 7 elevation angles from 90 deg to 7.5 deg
- Leica ScanStation P20



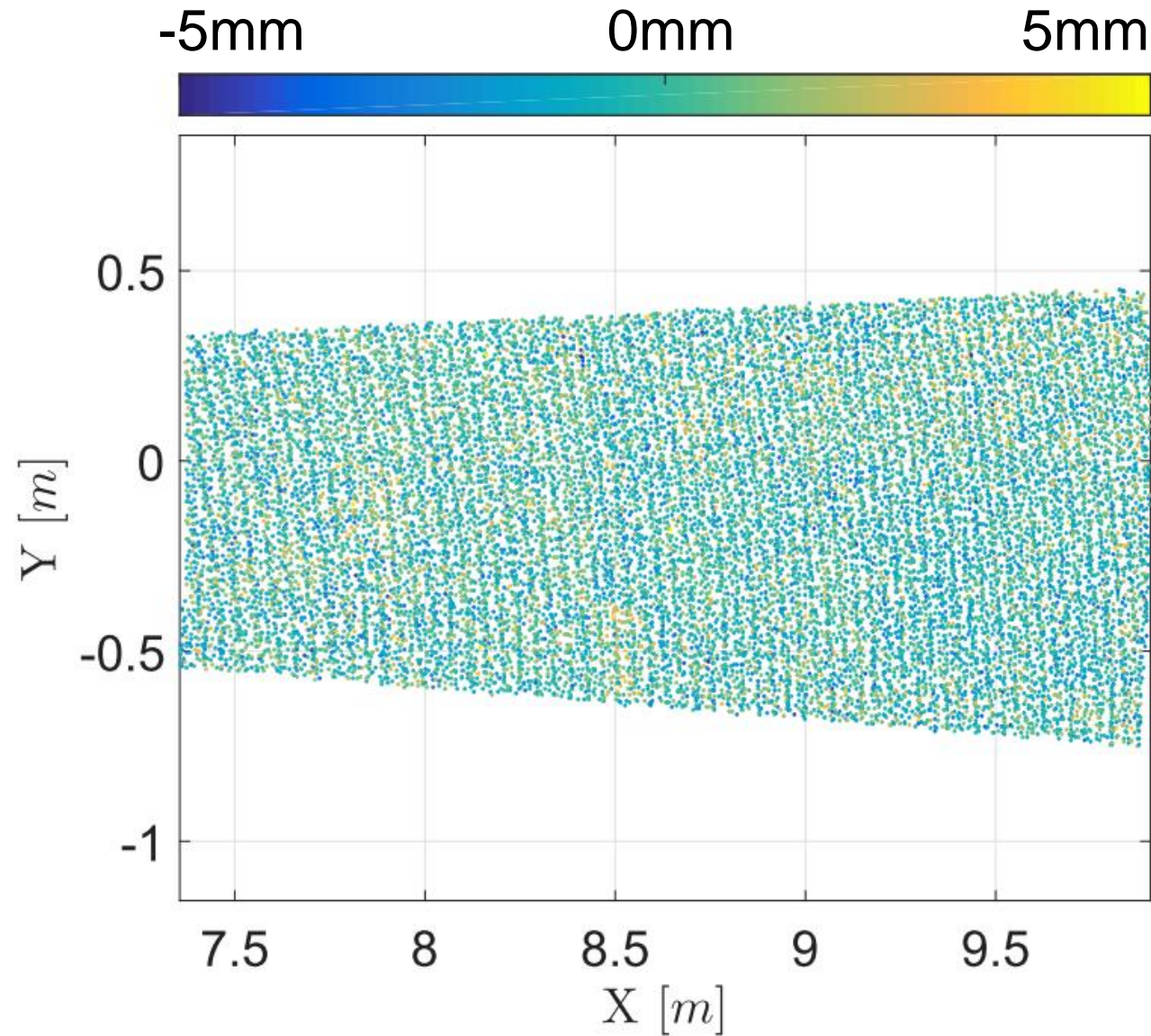
- Overhead station: good incidence angles, no obstruction
- Scanning at 7 elevation angles from 90 deg to 7.5 deg
- Leica ScanStation P20



Effelsberg, 100m



Onsala, 20m



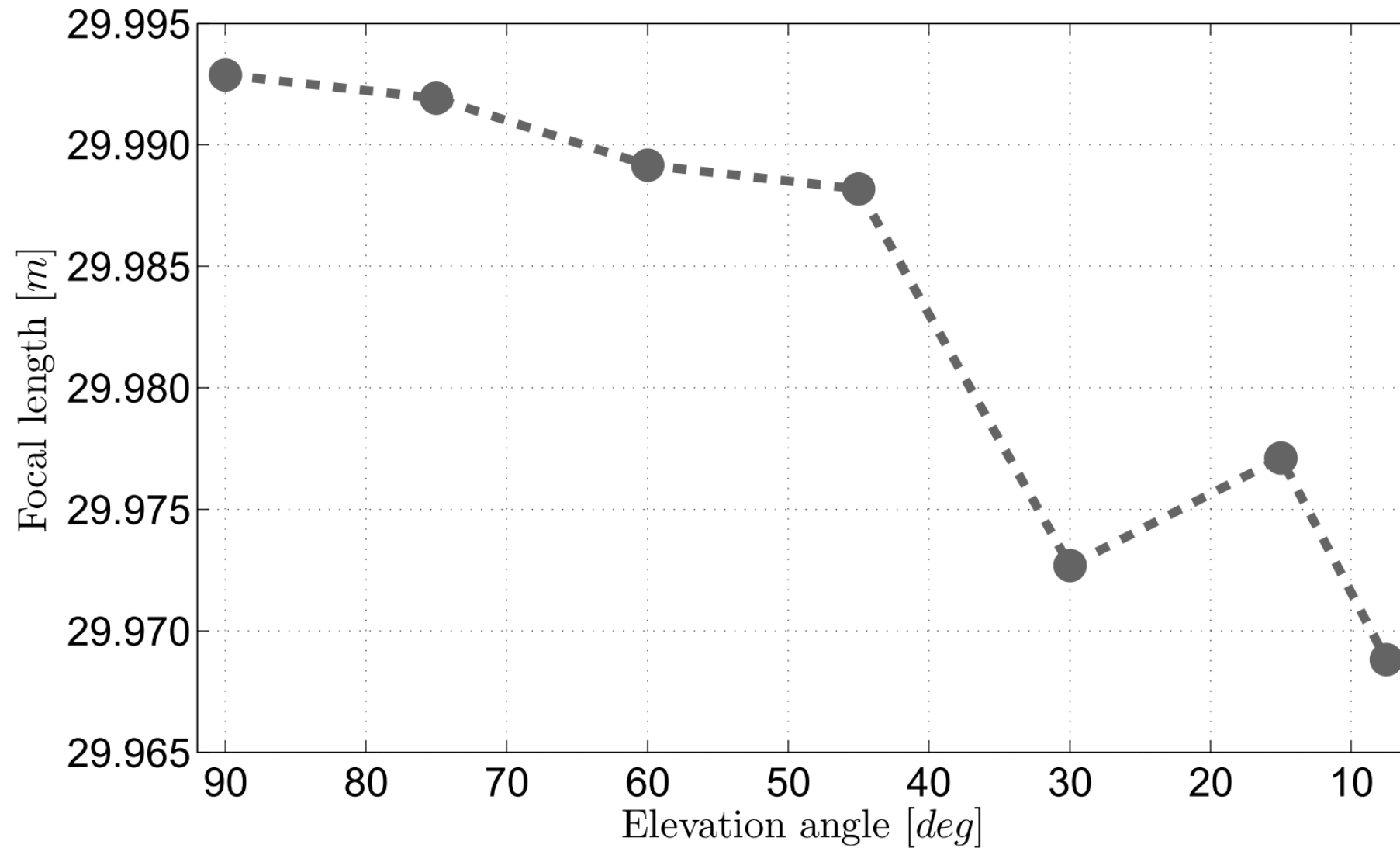
$\sigma < 1.5 \text{ mm}$
@ $r = 7 \dots 15 \text{ m}$

1. Scanning of main reflector at several elevation angles
2. Parameterization as rotational paraboloid

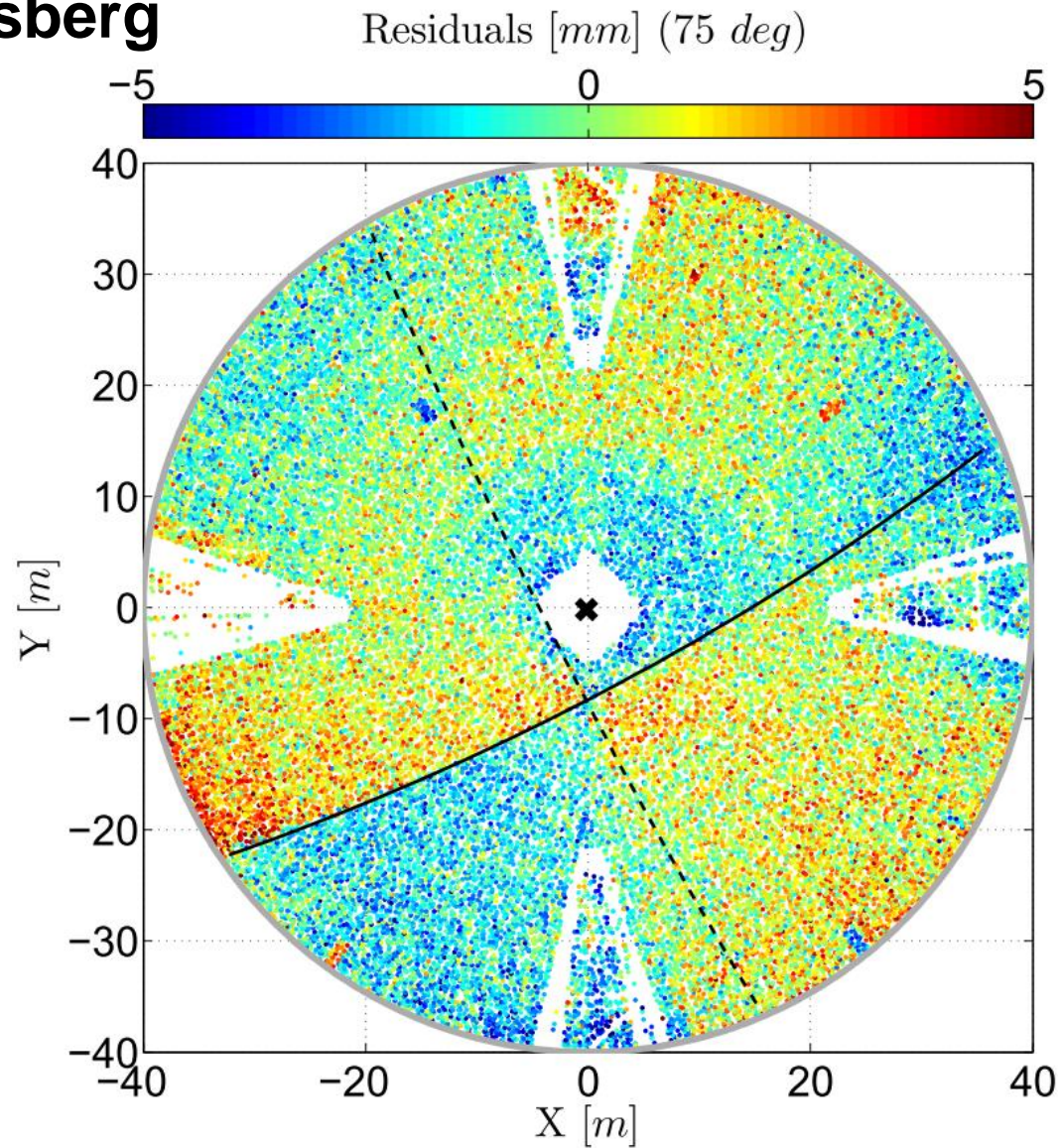
$$\frac{X_i^2 + Y_i^2}{4f} - Z_i = 0$$

$$\mathbf{X}_i = \mathbf{R}_y(\varphi_y) \cdot \mathbf{R}_x(\varphi_x) \cdot \mathbf{x}_i + \mathbf{X}_v$$

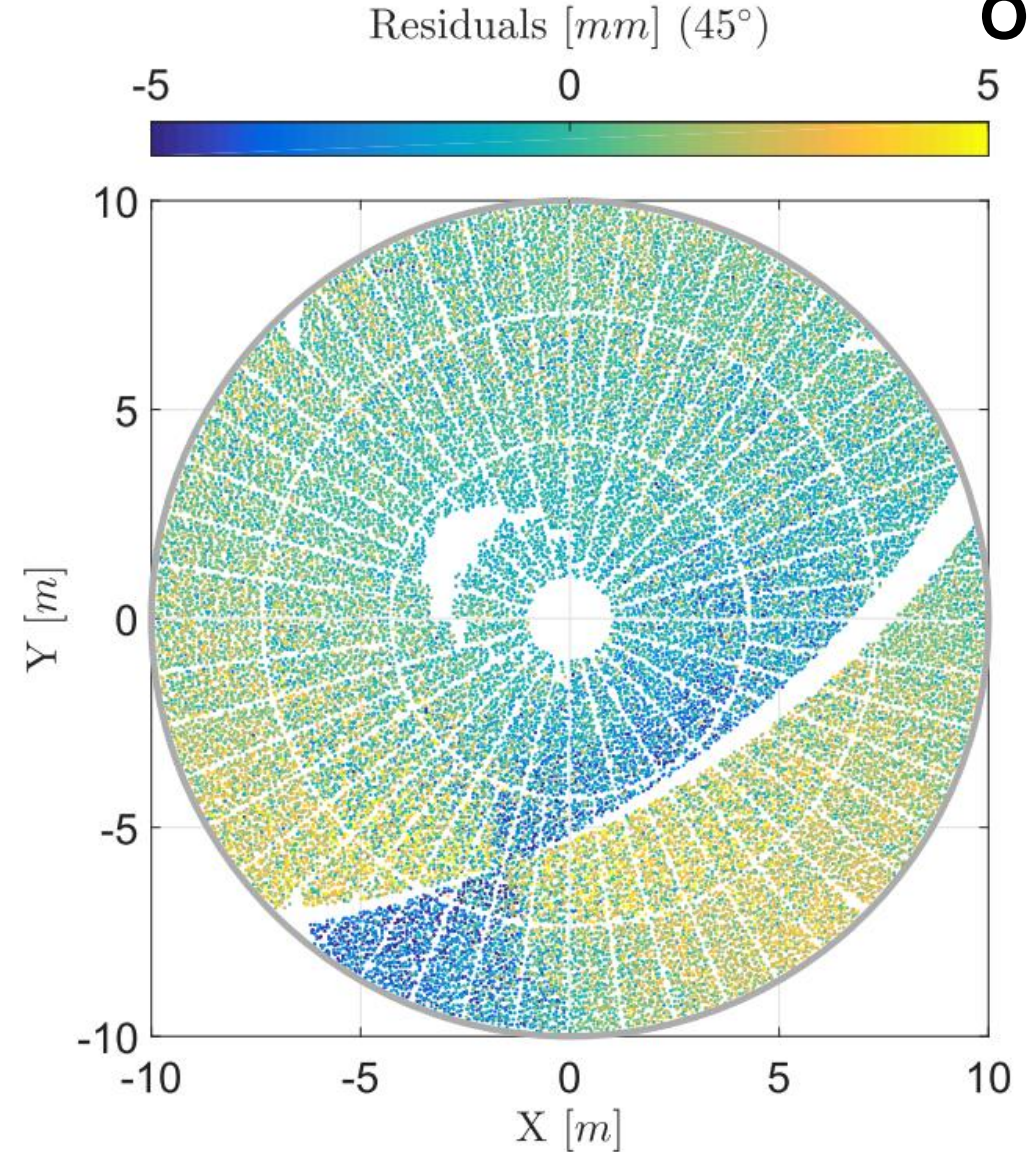
3. Least-squares estimation of the parameters by minimizing $\mathbf{v}^T \boldsymbol{\Sigma}^{-1} \mathbf{v}$
4. Analysis of results
 - **Global deformation**: variations of focal length f at different elevations
 - **Local deformation**: residuals from approximation



Effelsberg

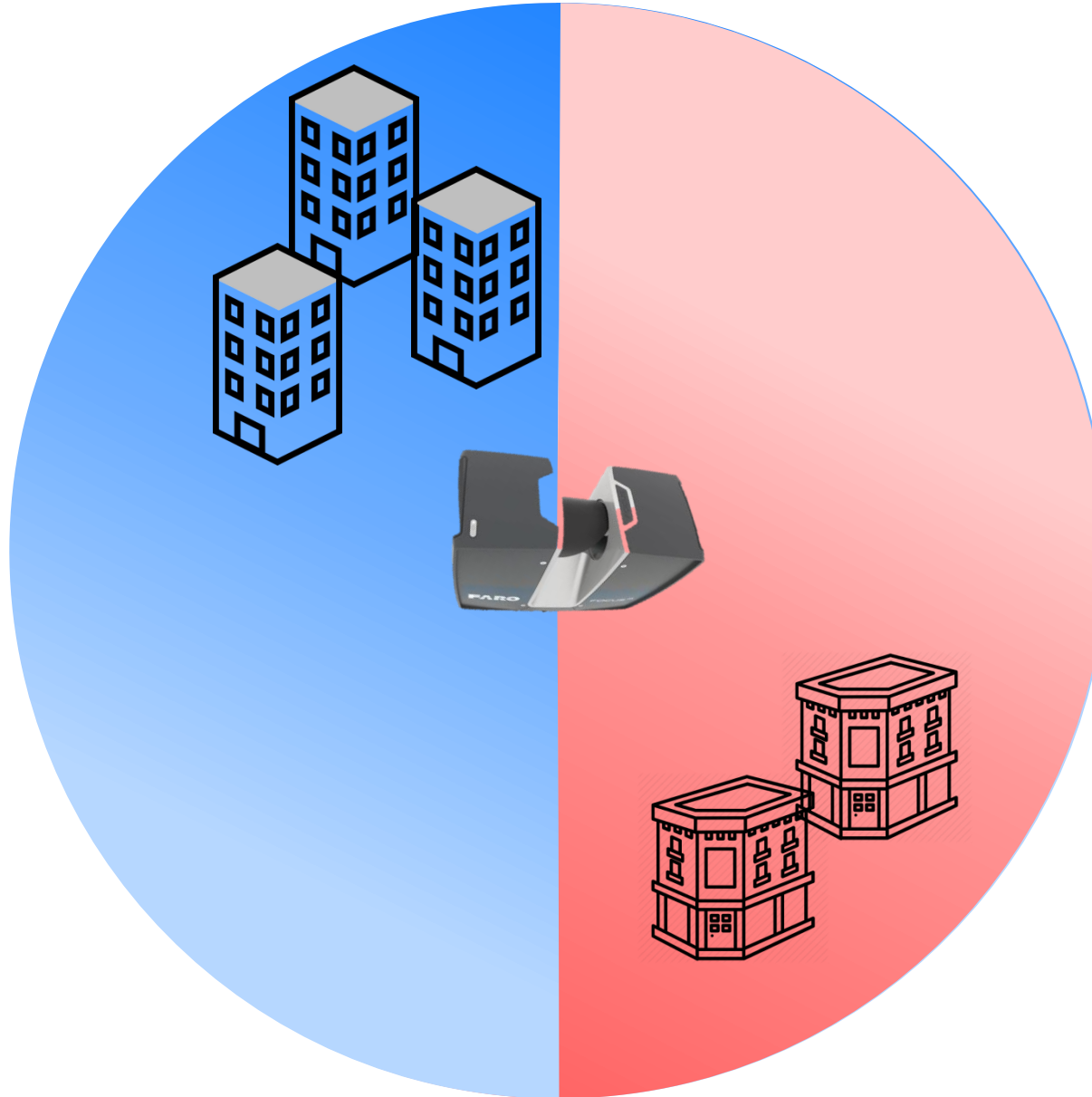


Onsala



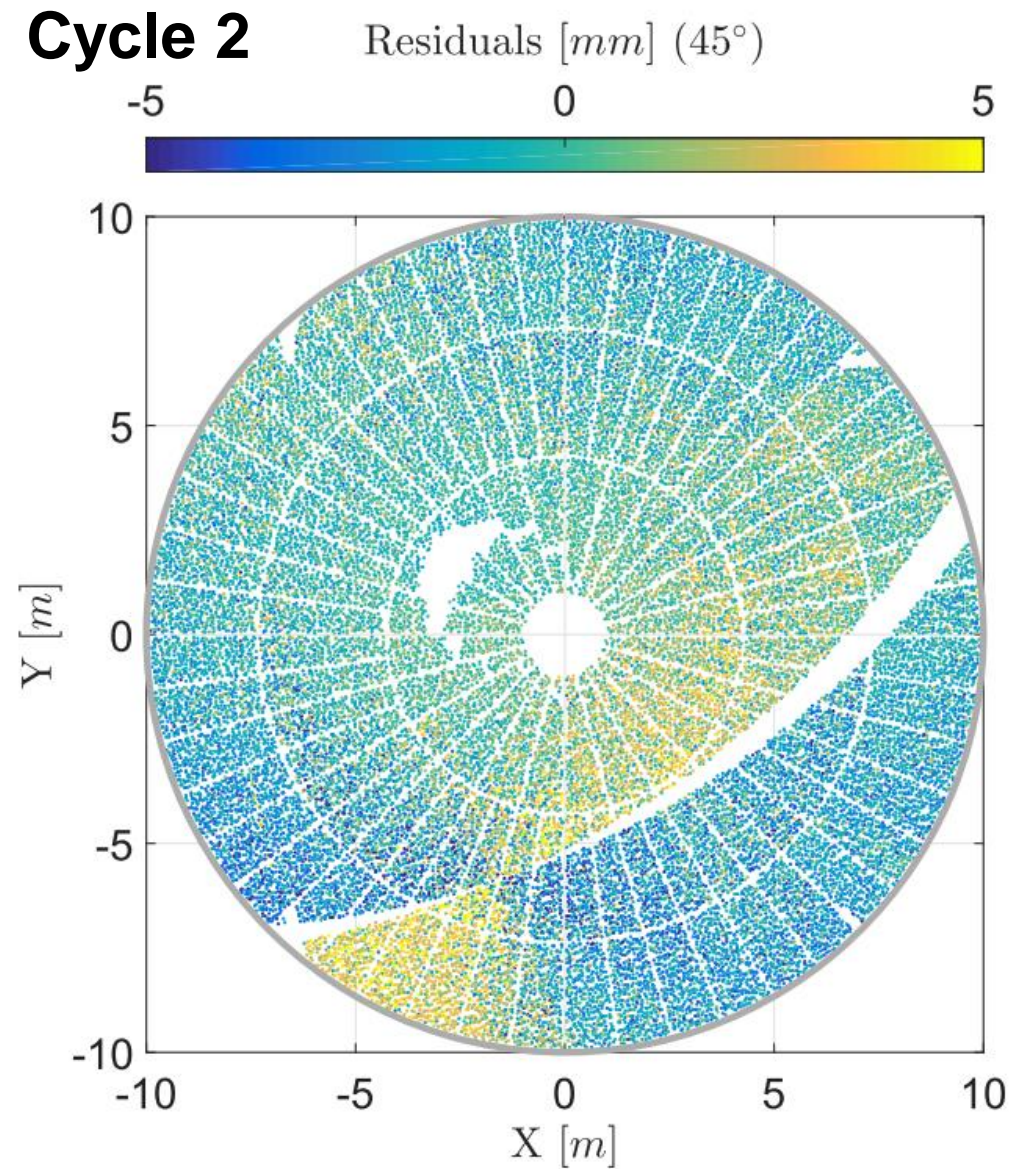
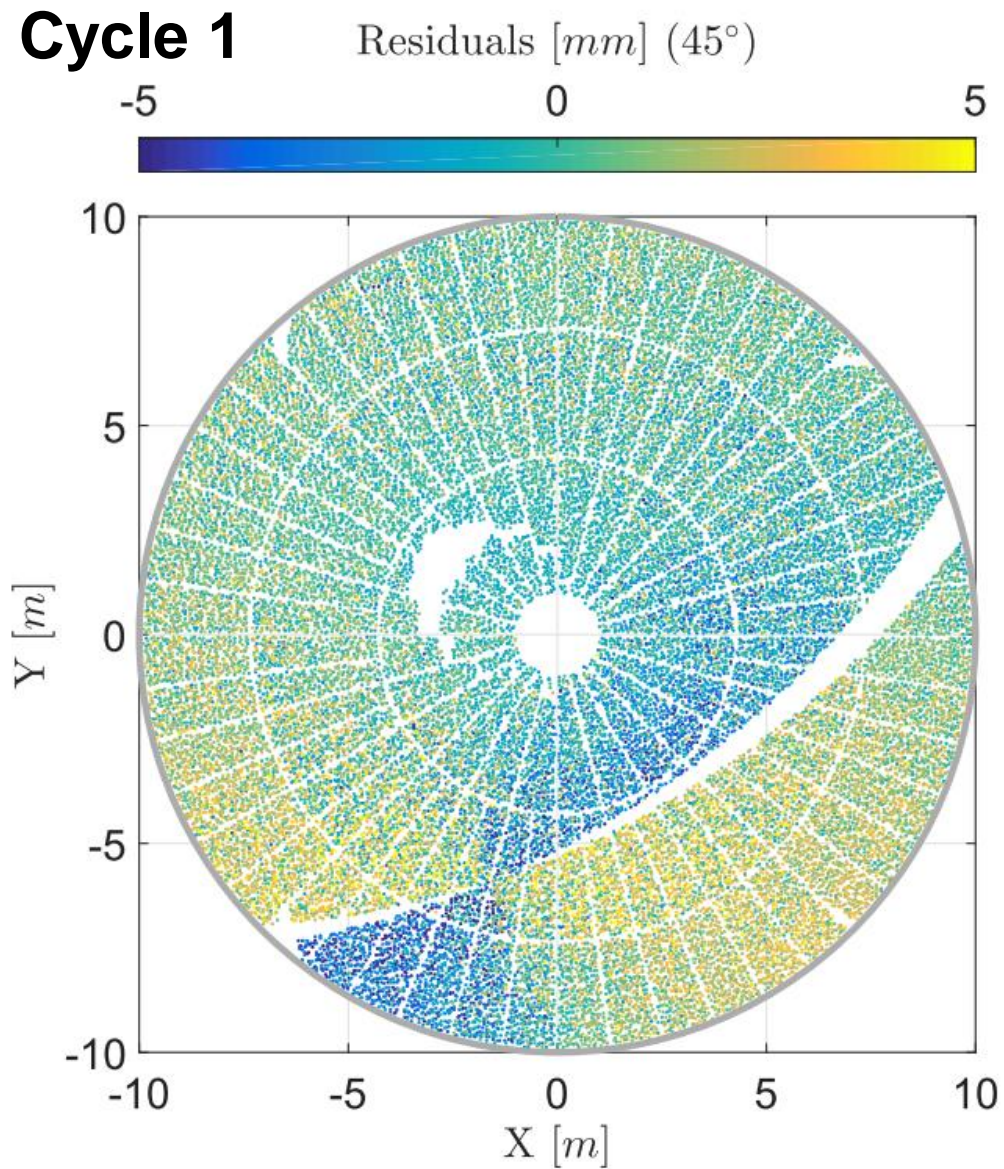
**Face 1 =
FRONT SIDE**

**Face 2 =
BACK SIDE**



1st CYCLE (0° - 180°)

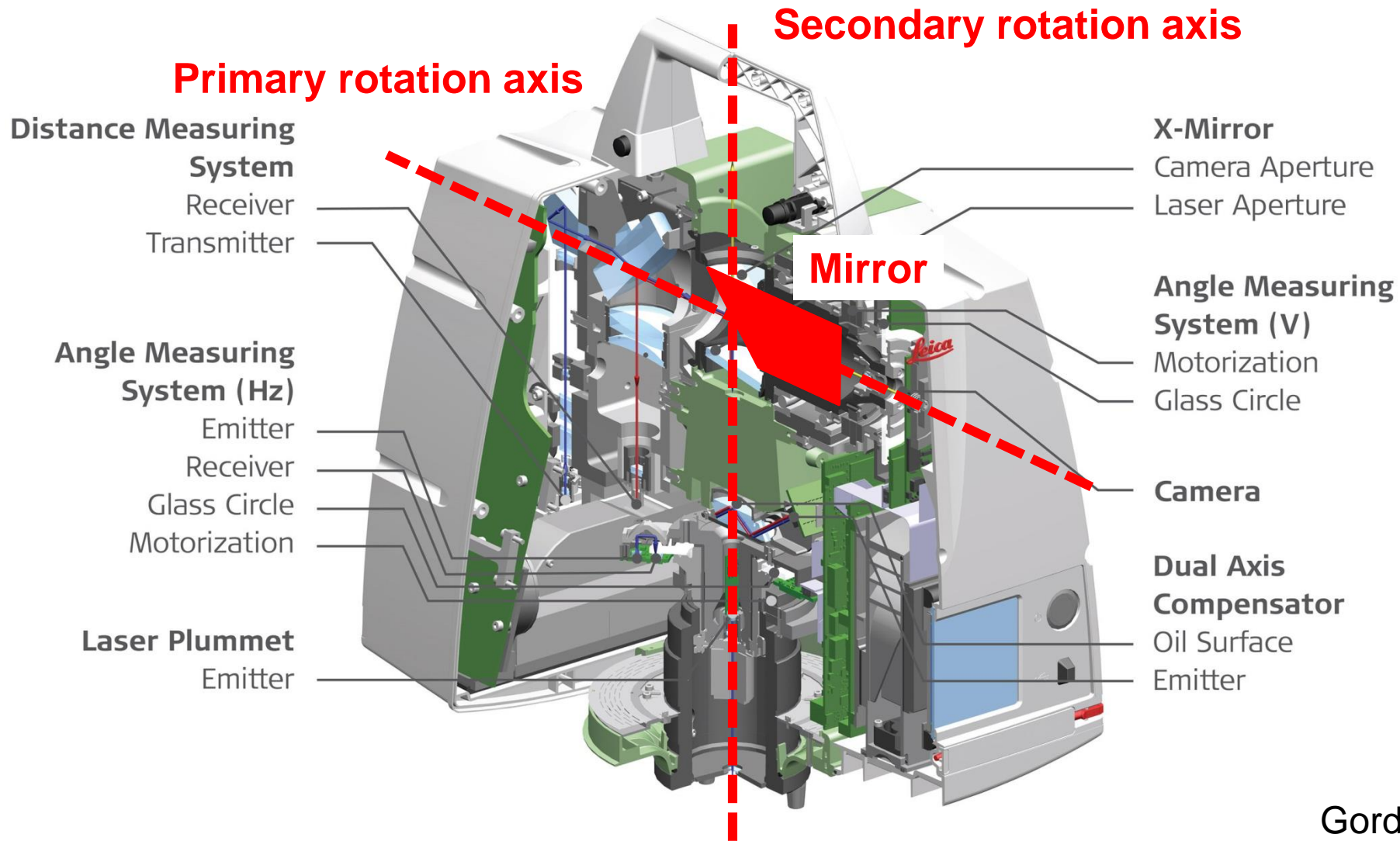
2nd CYCLE (180° - 360°)



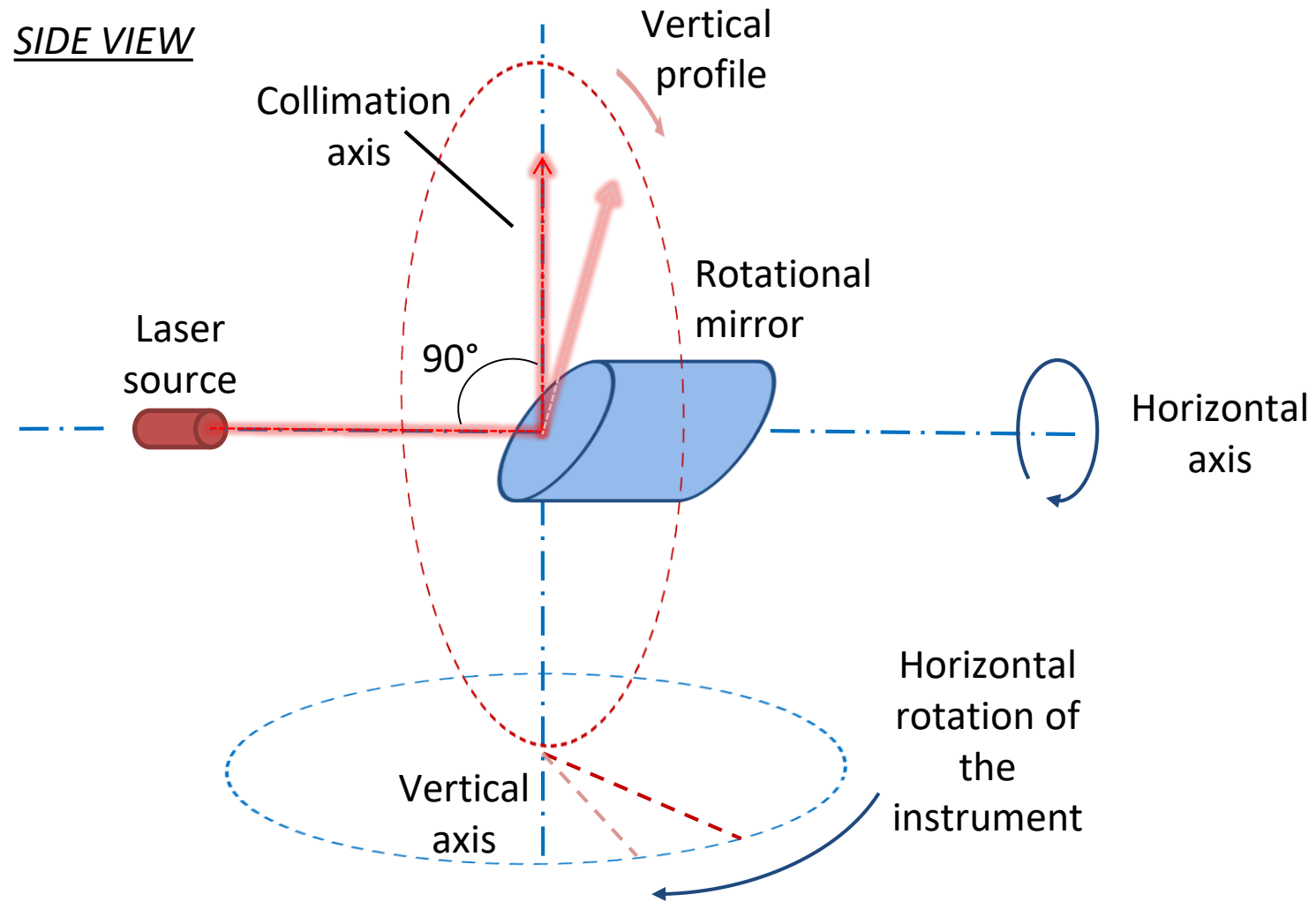
Large systematic errors

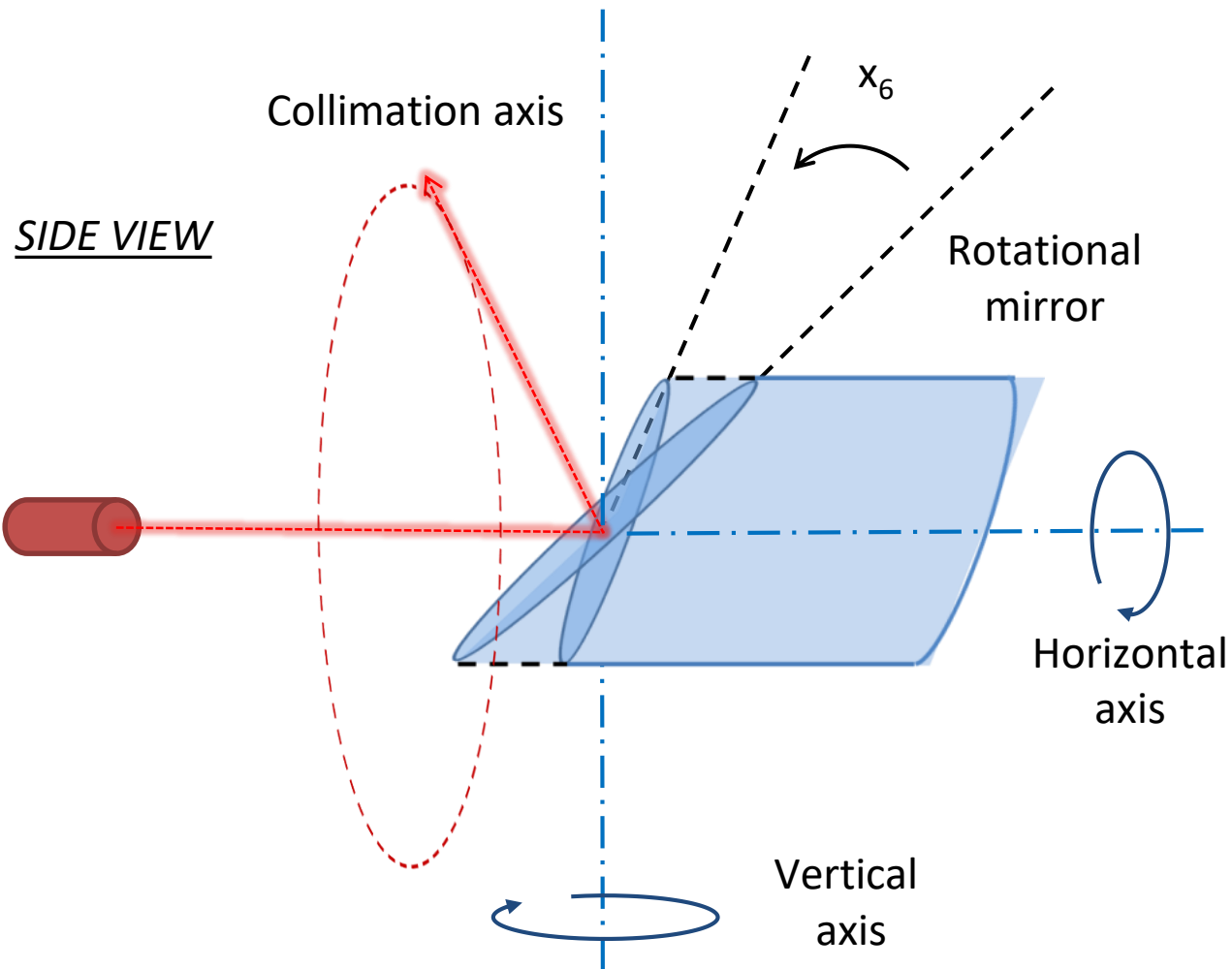
Sign changes between face 1 and face 2

Inspection not meaningful



Gordon
(2012)





Error in horizontal angle in face 1:

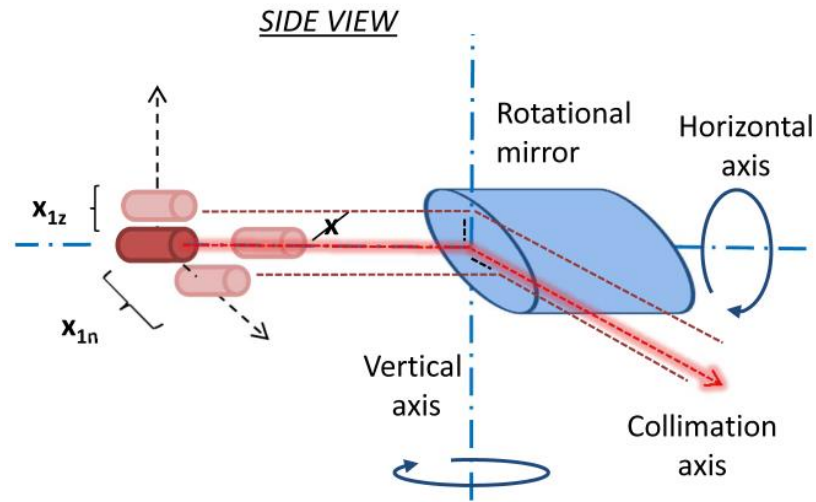
$$\Delta\varphi_j^i = + \frac{2x_6}{\sin(\theta_j^i)}$$

Error in horizontal angle in face 2:

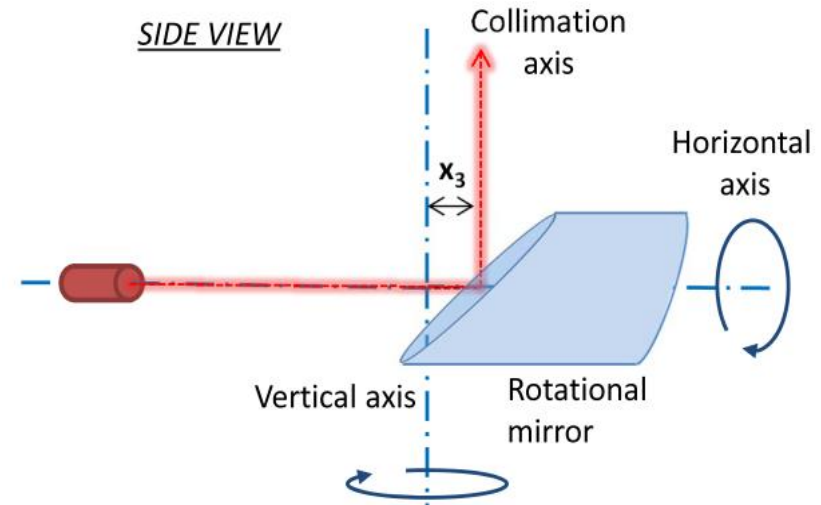
$$\Delta\varphi_j^i = - \frac{2x_6}{\sin(\theta_j^i)}$$

... with θ = vertical angle

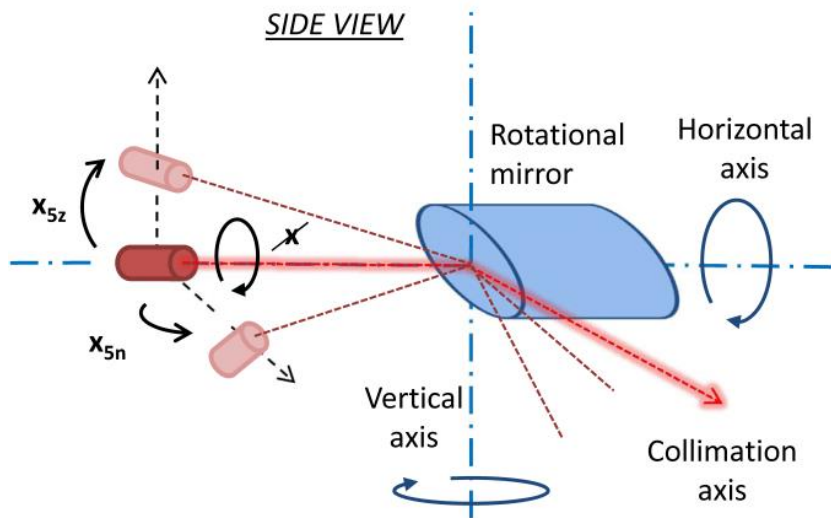
Eccentricity of laser



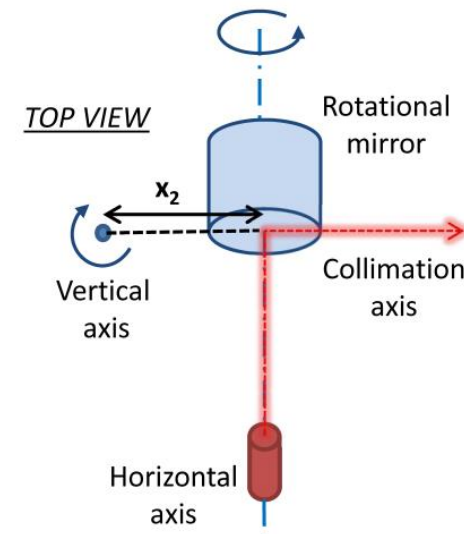
Eccentricity of mirror



Alignment of laser



Alignment of axes



1. Scanning of main reflector at several elevation angles **<= all in two faces**
2. Parameterization as rotational paraboloid

$$\frac{X_i^2 + Y_i^2}{Z_i} - Z_i = 0$$

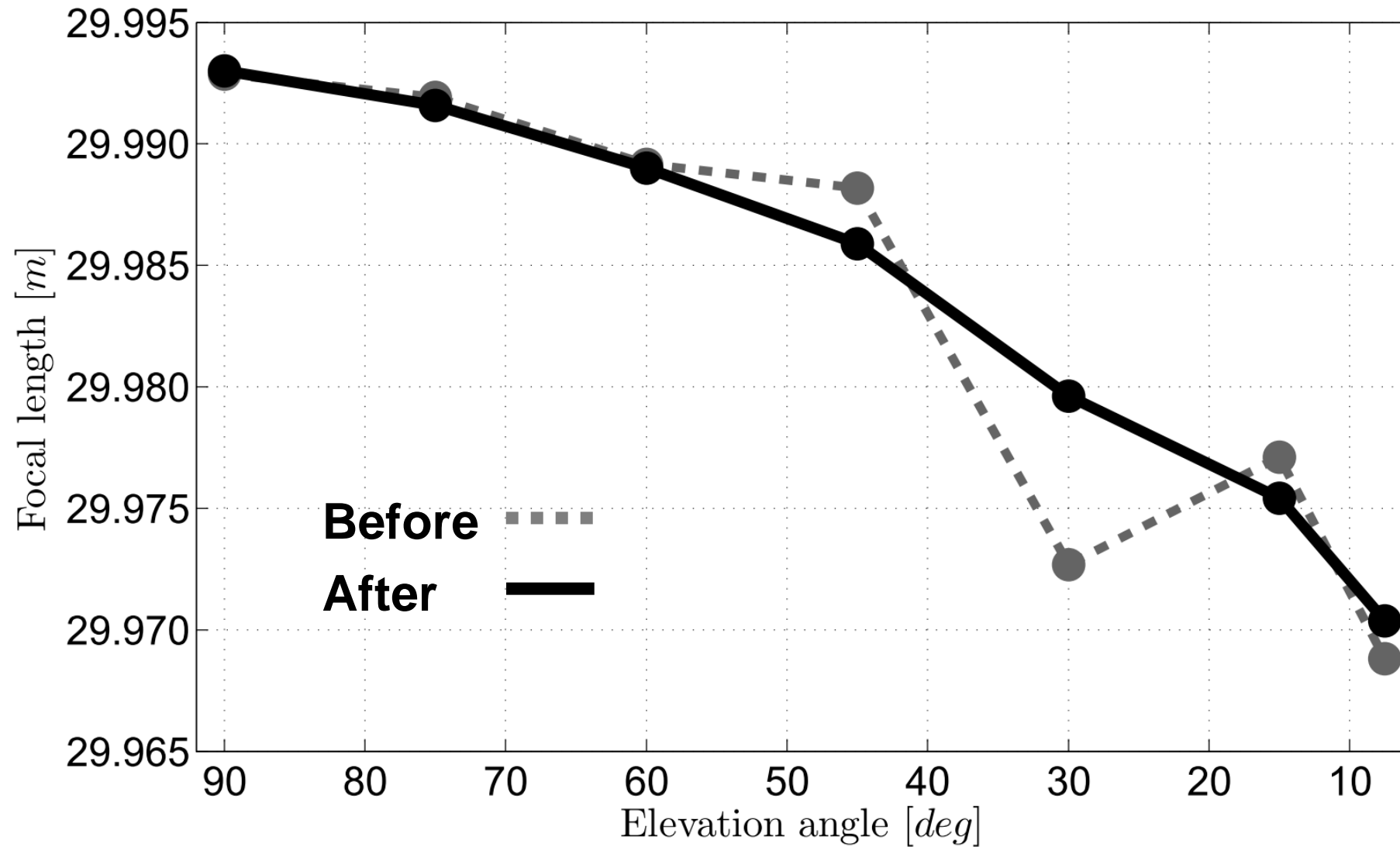
$$\Delta r_j^i = x_2 \sin(\theta_j^i) + x_{10}$$

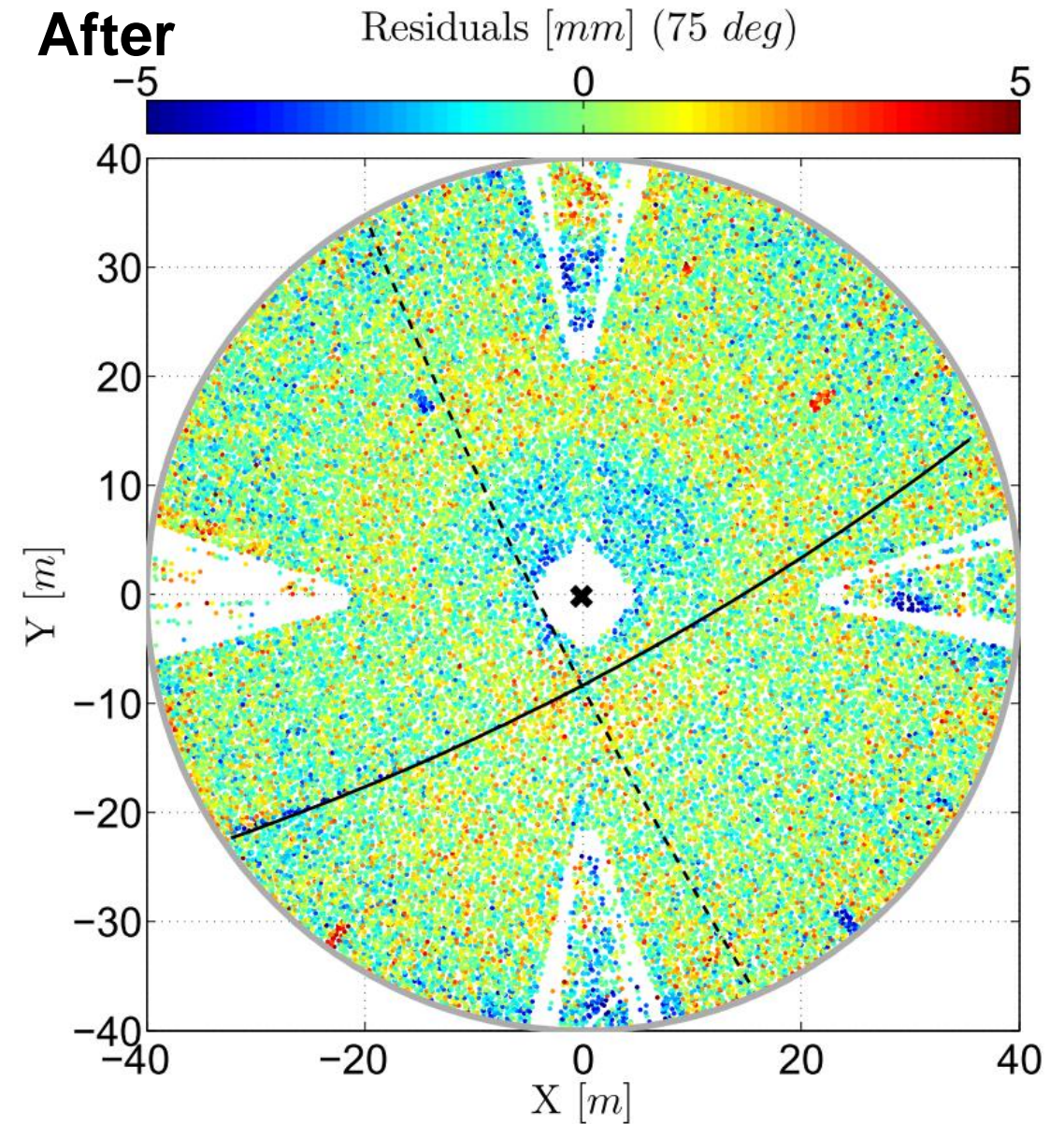
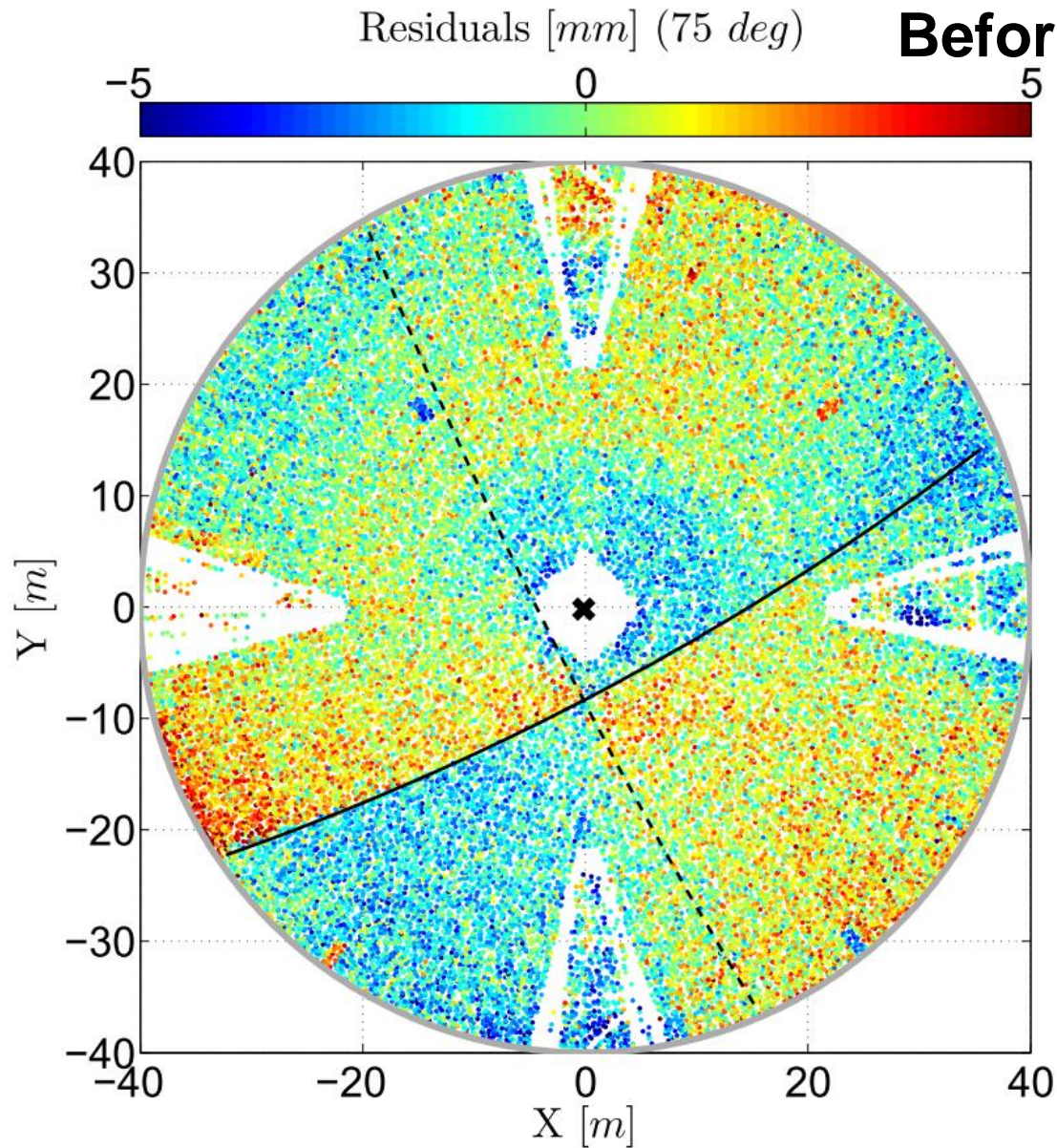
$$\Delta \theta_j^i = \frac{x_{1n+2} \cos(\theta_j^i)}{r_j^i} + x_4 + x_{5n} \cos(\theta_j^i) - \frac{x_{1z} \sin(\theta_j^i)}{r_j^i} - x_{5z} \sin(\theta_j^i)$$

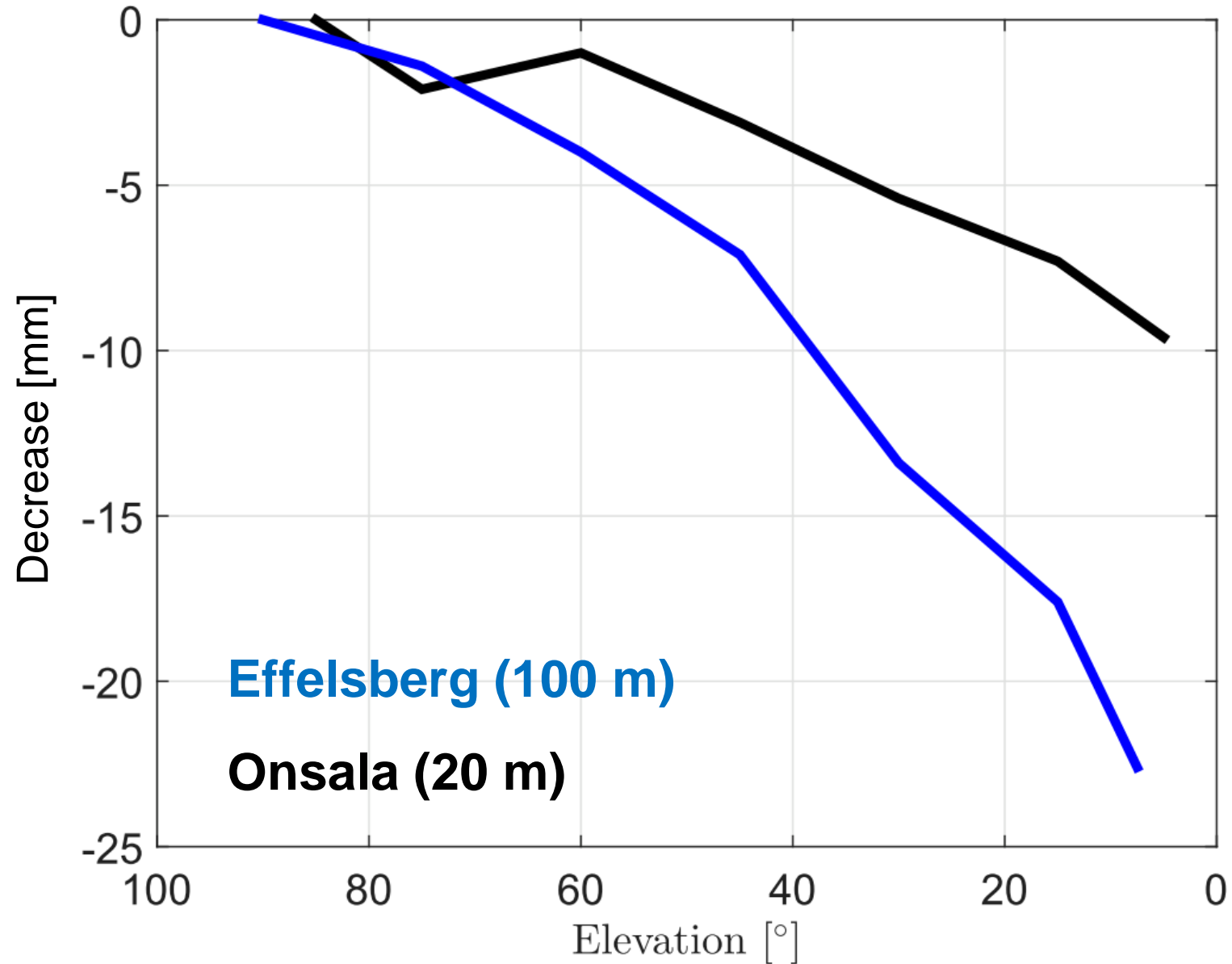
$$\Delta \varphi_j^i = \frac{x_{1z}}{r_j^i \tan(\theta_j^i)} + \frac{x_3}{r_j^i \sin(\theta_j^i)} + \frac{x_{5z-7}}{\tan(\theta_j^i)} + \frac{2x_6}{\sin(\theta_j^i)} + \frac{x_{1n}}{r_j^i}$$

.... in-situ calibration using scans in two faces

- **Local deformation:** residuals from approximation





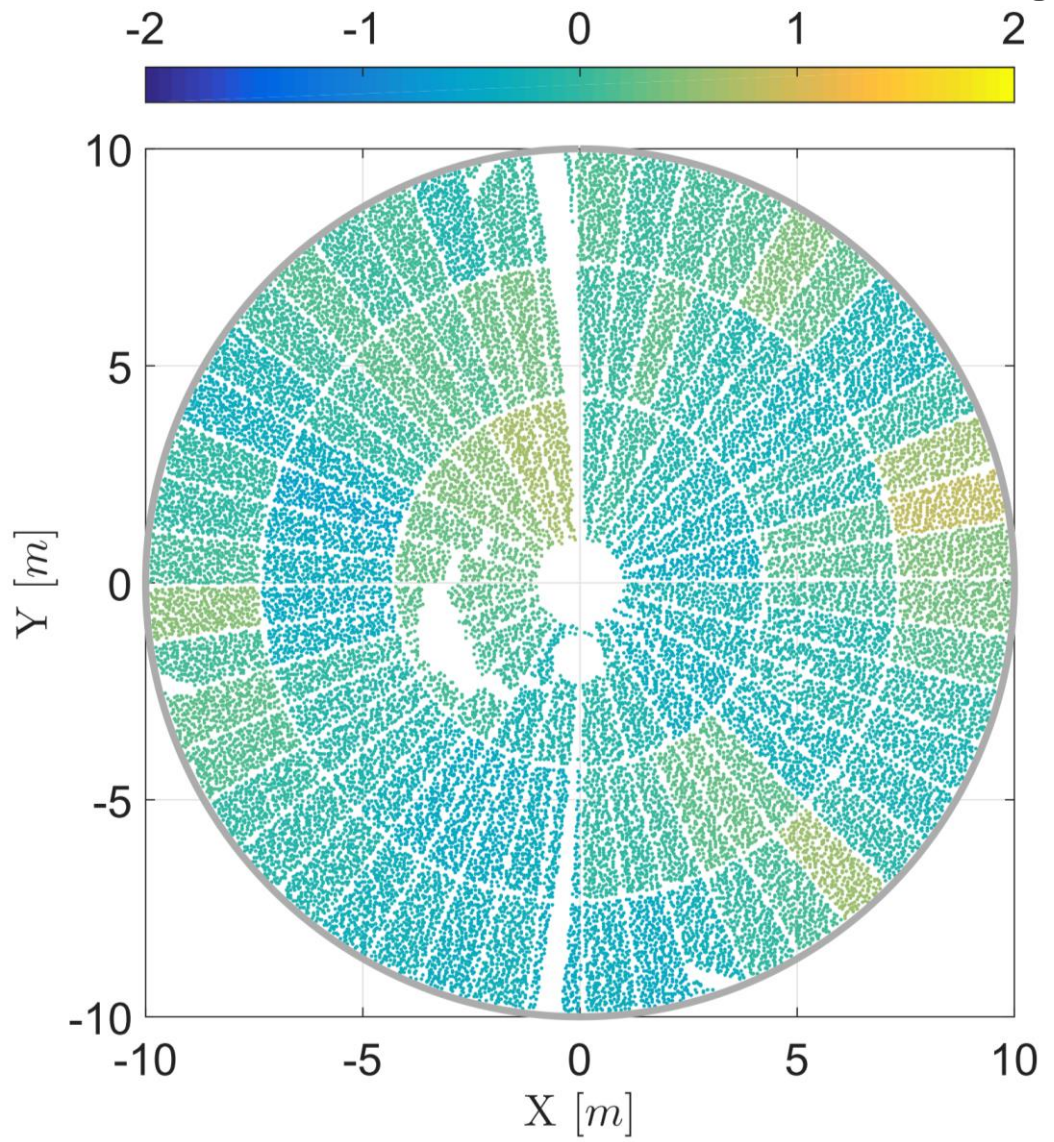
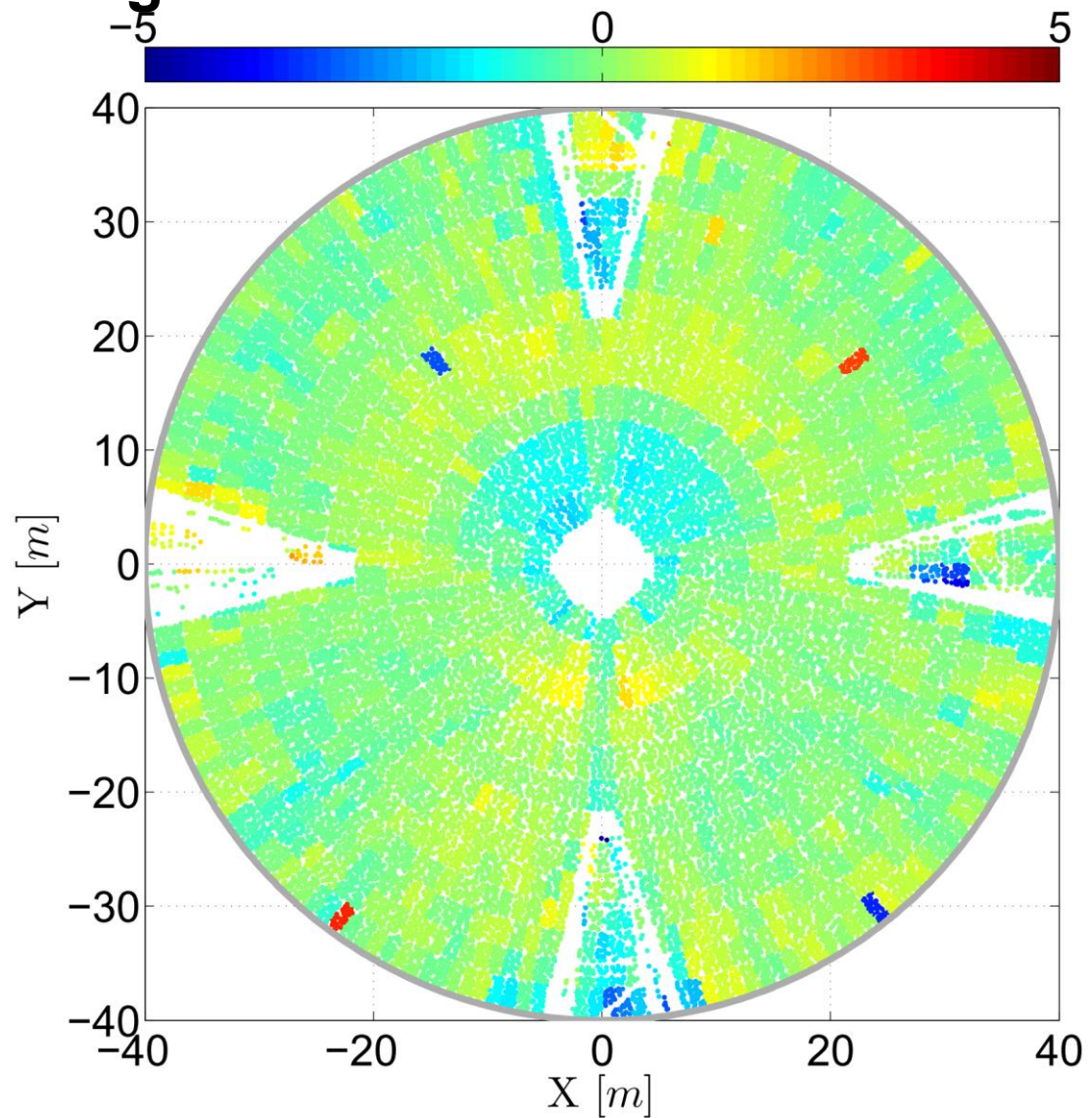


Effelsberg

Mean Residuals of Panels [mm] (75 deg)

Residuals [mm] (75°)

Onsala



- Focal length variations of up to 23 mm
- High-accuracy inspection of large object feasible with terrestrial laser scanner, but
 - **Systematic errors larger than random ones**
 - **Misalignment of laser scanner has to be taken into account**
- **Scanning in two faces + in-situ calibration of scanner improves inspection**
... **Knowledge about sensor needed**
- Transferable to other laser scanners and other objects



Thanks for your attention!

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- Holst, C. et al. (2014): Aiming at self-calibration of terrestrial laser scanners using only one single object and one single scan, J. Appl. Geodesy, 8 (4), S. 295-310
- Holst, C. et al. (2015): Improved area-based deformation analysis of a radio telescope's main reflector based on terrestrial laser scanning, J. Appl. Geodesy, 9 (1), S. 1-14
- Holst, C. et al. (2017): Terrestrial laser scanner two-face measurements for analyzing the elevation-dependent deformation of the Onsala Space Observatory 20-m radio telescope's main reflector in a bundle adjustment, Sensors, 17 (8), 1833