

Investigation and modelling of rolling shutter distortions on photogrammetric single- and multi-image applications

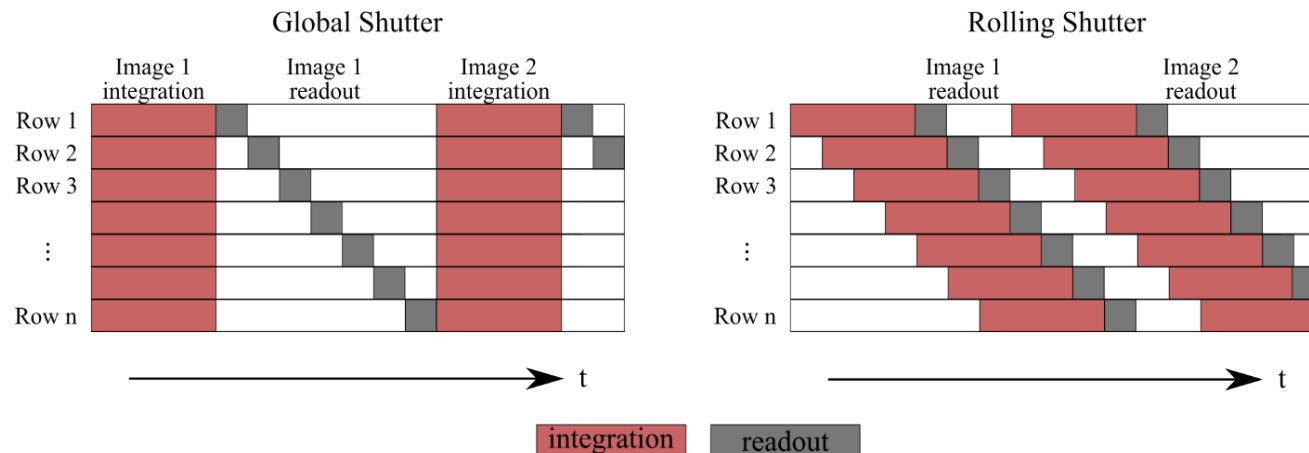
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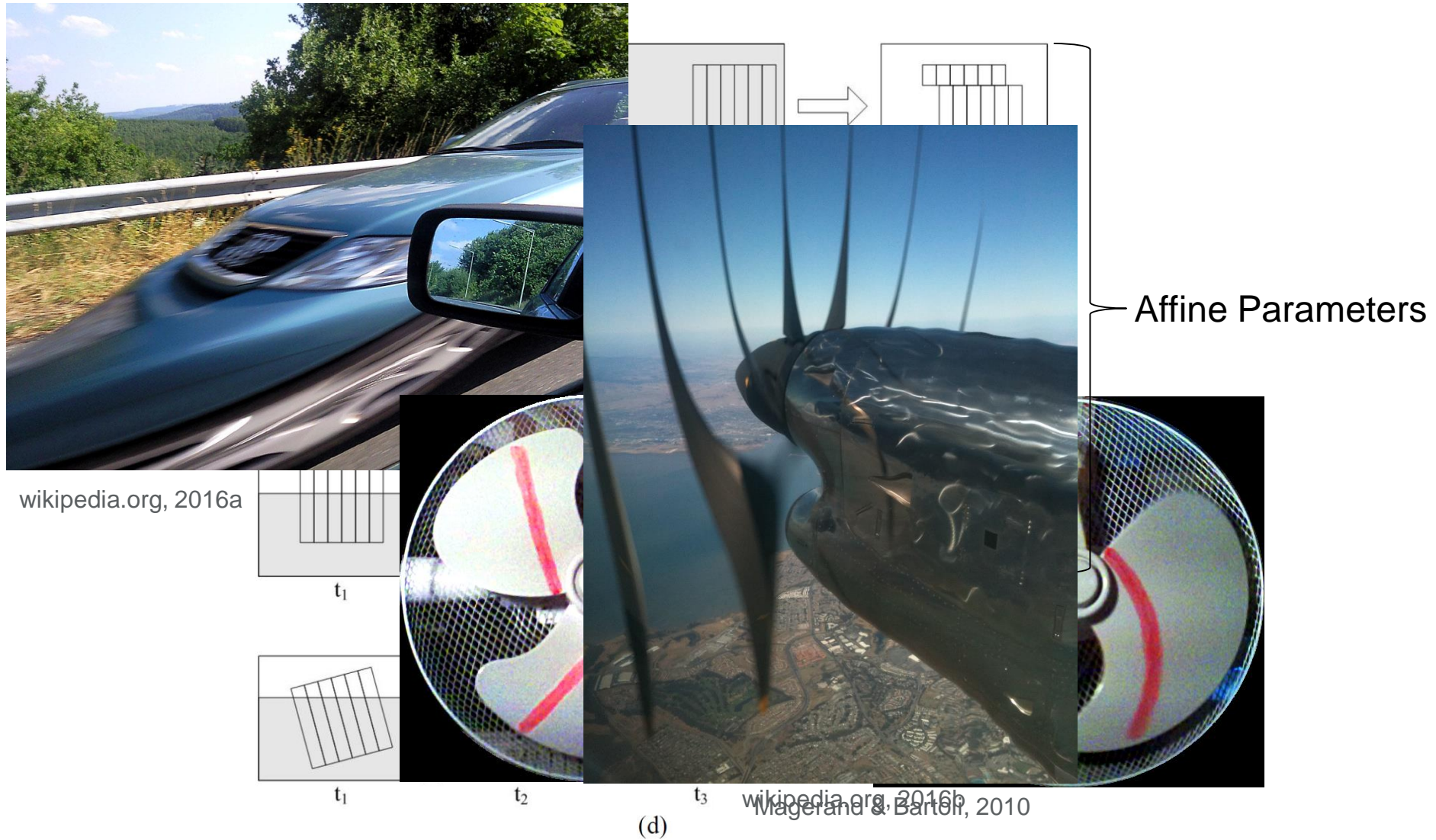
- Photogrammetry – „Information from imagery“
- Basic approach: Taking images that comply with the pinhole camera model
- CMOS technology is standard in many eligible cameras
 - (Usually) unable to save accumulated voltage
- Sensor is integrated and read out sequentially
 - Exposure at many time intervals



according to Ringaby, 2012

- Causing distortions in kinematic applications
 - Rolling shutter distortions

ROLLING SHUTTER DISTORTIONS



- Collinearity equations employ one exterior orientation per image (Global-Shutter-Model)
→ 6 degrees of freedom per image

$$\overrightarrow{X_T} = [X_0 \ Y_0 \ Z_0]^T \quad \mathbf{R}(a, b, c, d)$$

- Rolling shutter creates one exterior orientation per image row

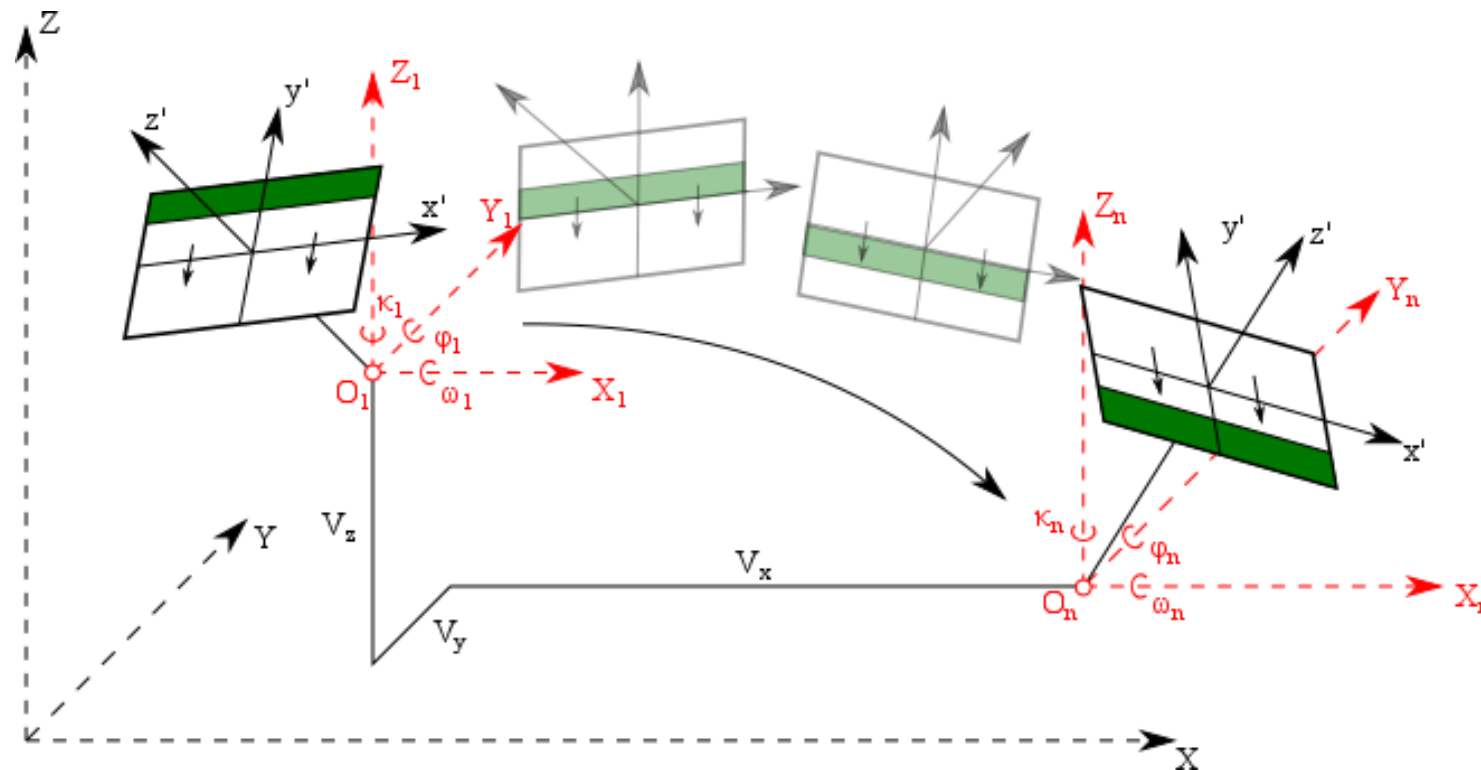
$$\begin{aligned} \overrightarrow{X_{T_1}} &= [X_{0,1} \ Y_{0,1} \ Z_{0,1}]^T & \mathbf{R}_1(a_1, b_1, c_1, d_1) \\ \overrightarrow{X_{T_2}} &= [X_{0,2} \ Y_{0,2} \ Z_{0,2}]^T & \mathbf{R}_2(a_2, b_2, c_2, d_2) \\ & \vdots & \vdots \\ \overrightarrow{X_{T_n}} &= [X_{0,n} \ Y_{0,n} \ Z_{0,n}]^T & \mathbf{R}_n(a_n, b_n, c_n, d_n) \end{aligned}$$

→ 6 degrees of freedom per row → 6n degrees of freedom per image

- Problem: High amount of unknowns causes an underdetermined system of equations

- Solution: Restriction to two exterior orientations and interpolation

$$\begin{aligned} \overrightarrow{X_{0_1}} &= [X_{0,1} \ Y_{0,1} \ Z_{0,1}]^T & \mathbf{R}_1(a_1, b_1, c_1, d_1) \\ \overrightarrow{X_{0_n}} &= [X_{0,n} \ Y_{0,n} \ Z_{0,n}]^T = \overrightarrow{X_{0_1}} + \overrightarrow{V} & \mathbf{R}_n(a_n, b_n, c_n, d_n) \end{aligned}$$



- Collinearity equations for Rolling Shutter

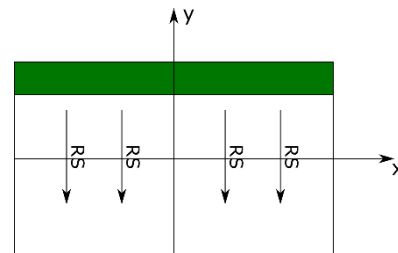
- Additional variables

- V → Translation during image acquisition
- q_1, q_n → Unit quaternions for rotation
→ R_{int} : Interpolated rotation matrix, dependent on τ
- τ → Normalized interpolation factor, dependent on y'

- 12 degrees of freedom → Min. 6 spatially distributed points

$$x' = x'_0 + z' \frac{r_{int}(\tau)_{11}(X - (X_0 + \tau V_x)) + r_{int}(\tau)_{21}(Y - (Y_0 + \tau V_y)) + r_{int}(\tau)_{31}(Z - (Z_0 + \tau V_z))}{r_{int}(\tau)_{13}(X - (X_0 + \tau V_x)) + r_{int}(\tau)_{23}(Y - (Y_0 + \tau V_y)) + r_{int}(\tau)_{33}(Z - (Z_0 + \tau V_z))} + \Delta x'$$

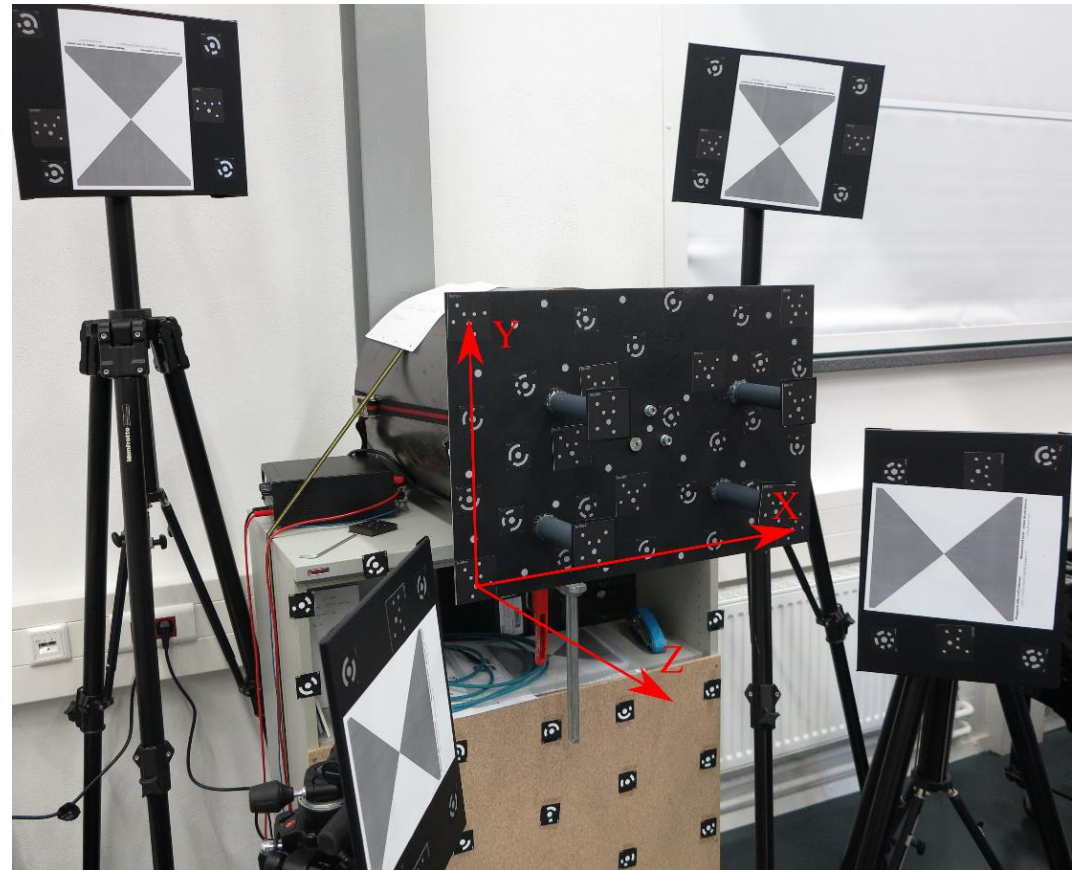
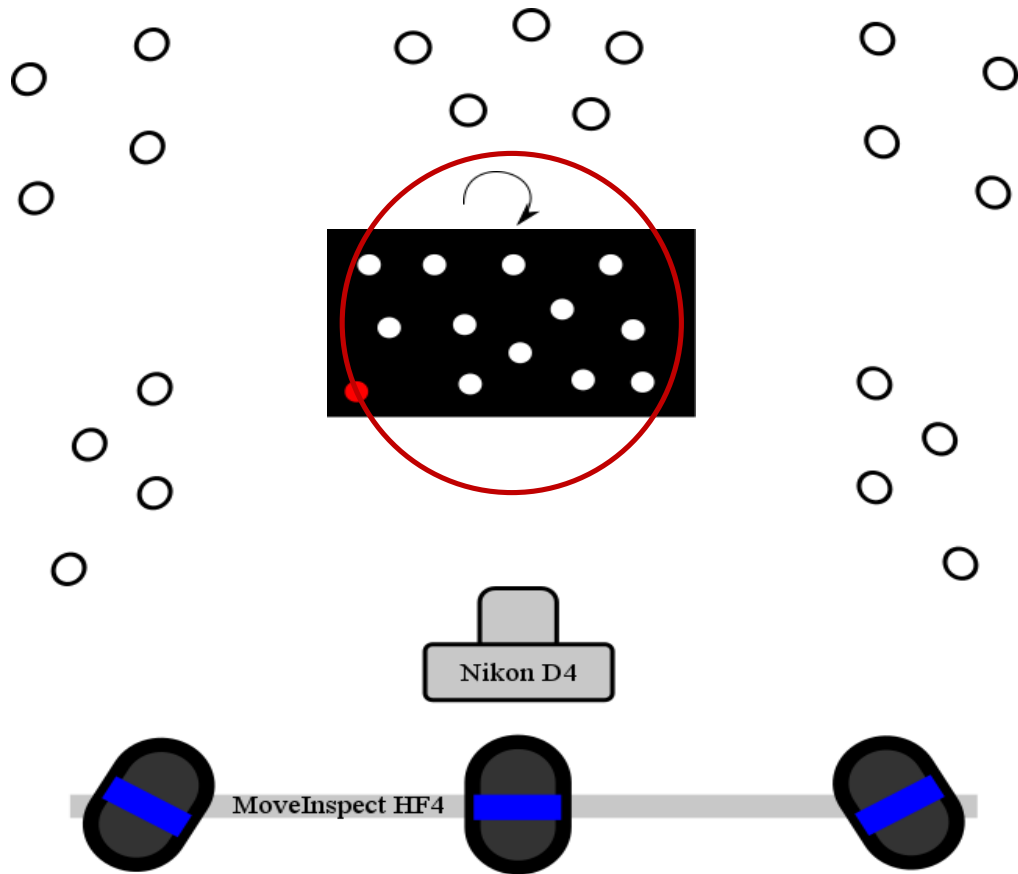
$$y' = y'_0 + z' \frac{r_{int}(\tau)_{12}(X - (X_0 + \tau V_x)) + r_{int}(\tau)_{22}(Y - (Y_0 + \tau V_y)) + r_{int}(\tau)_{32}(Z - (Z_0 + \tau V_z))}{r_{int}(\tau)_{13}(X - (X_0 + \tau V_x)) + r_{int}(\tau)_{23}(Y - (Y_0 + \tau V_y)) + r_{int}(\tau)_{33}(Z - (Z_0 + \tau V_z))} + \Delta y'$$

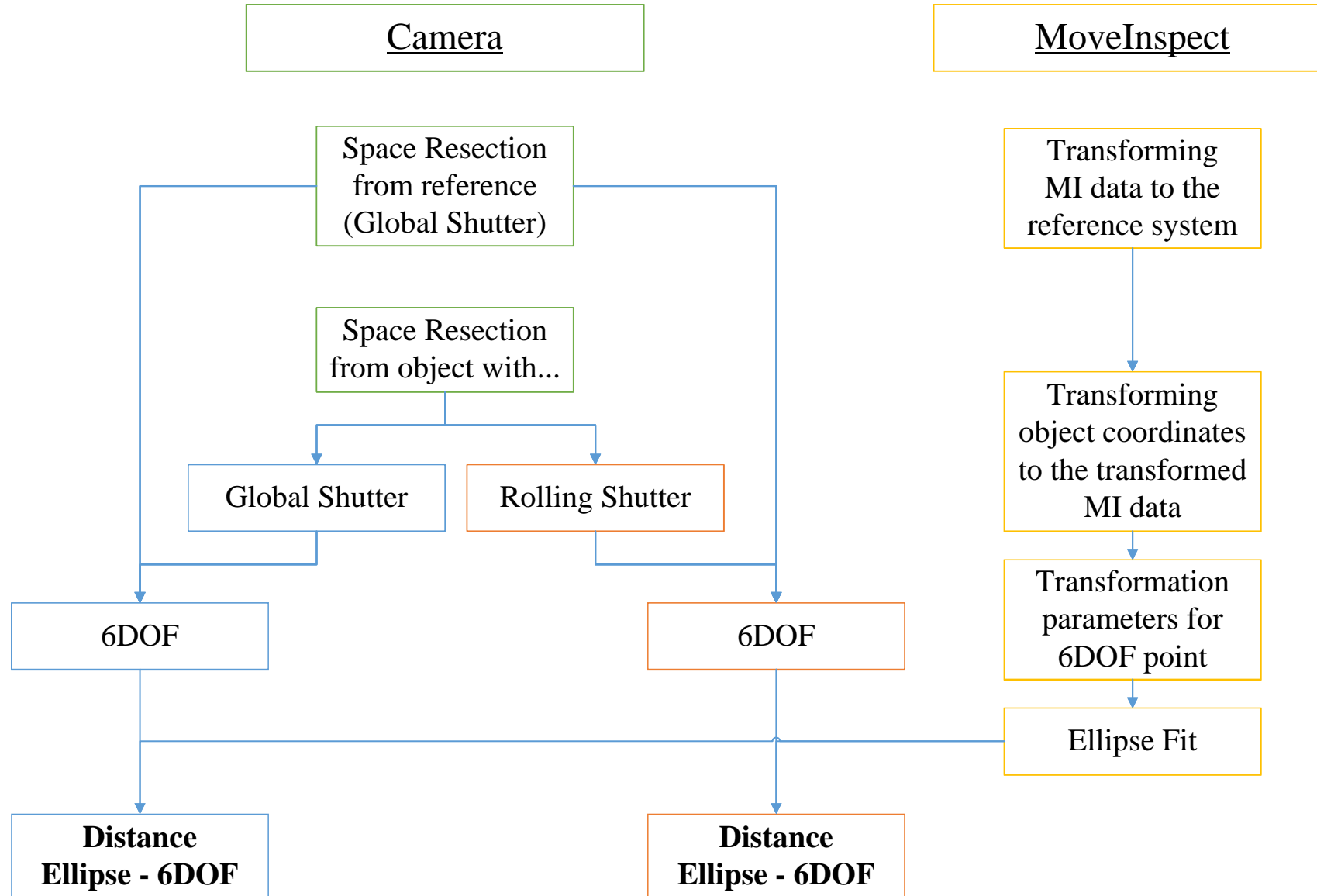


$$\tau = \frac{y_{max} - y'_i}{y_{max} - y_{min}}$$

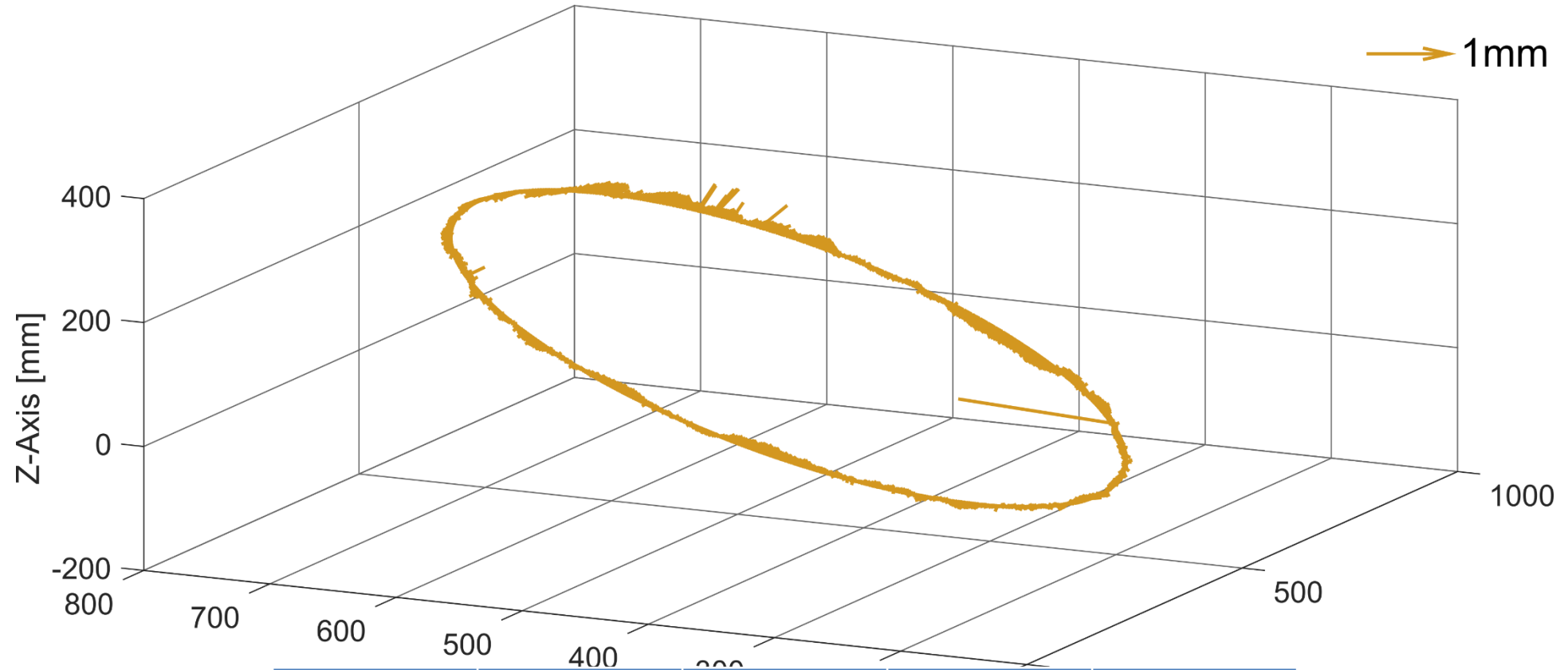
		Camera	
		Static	Kinematic
Object	Static	Global Shutter (Standard) Model	Rolling Shutter (Extended) Model
	Kinematic	Reversed Rolling Shutter Model	Not (yet) investigated

EXPERIMENTAL CONFIGURATION



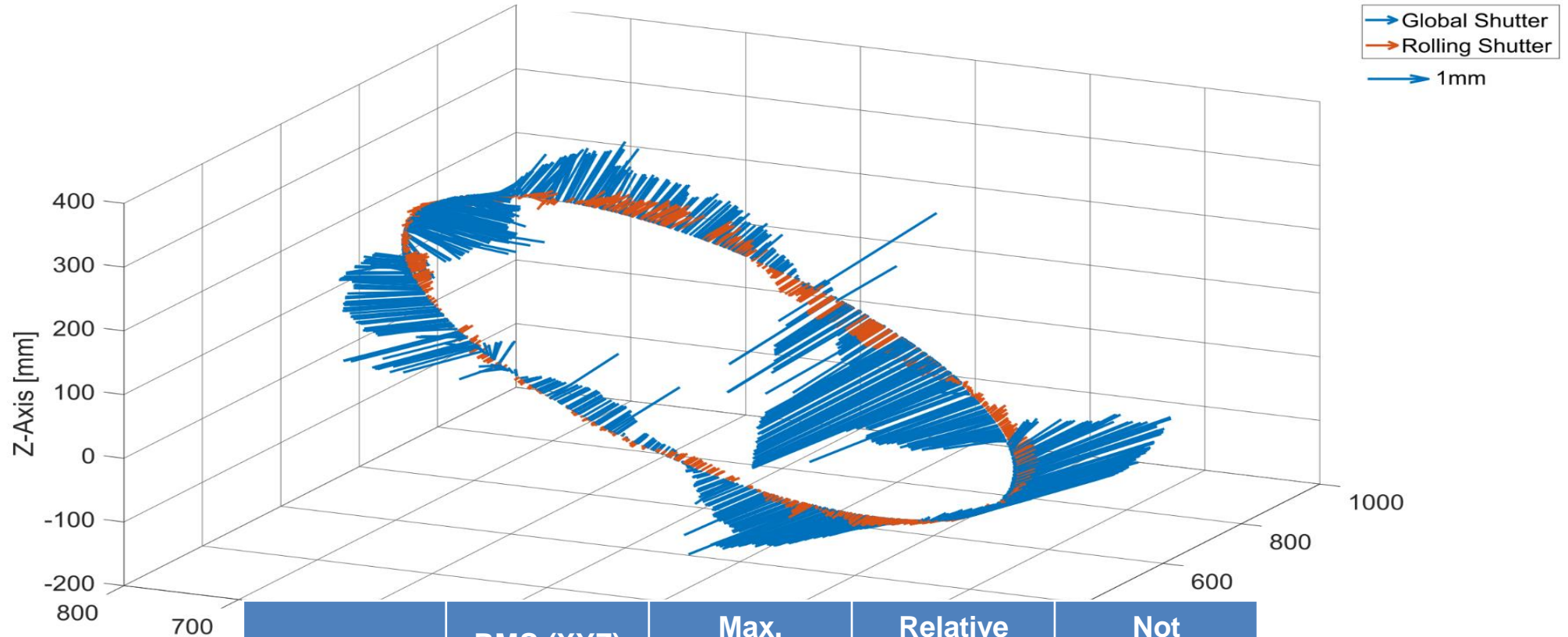


ELLIPSE FIT MI DATA - RESIDUALS



Standard Deviation	X	Y	Z	XYZ	Axis [mm]
Ellipse	0.031 mm	0.072 mm	0.079 mm	0.111 mm	

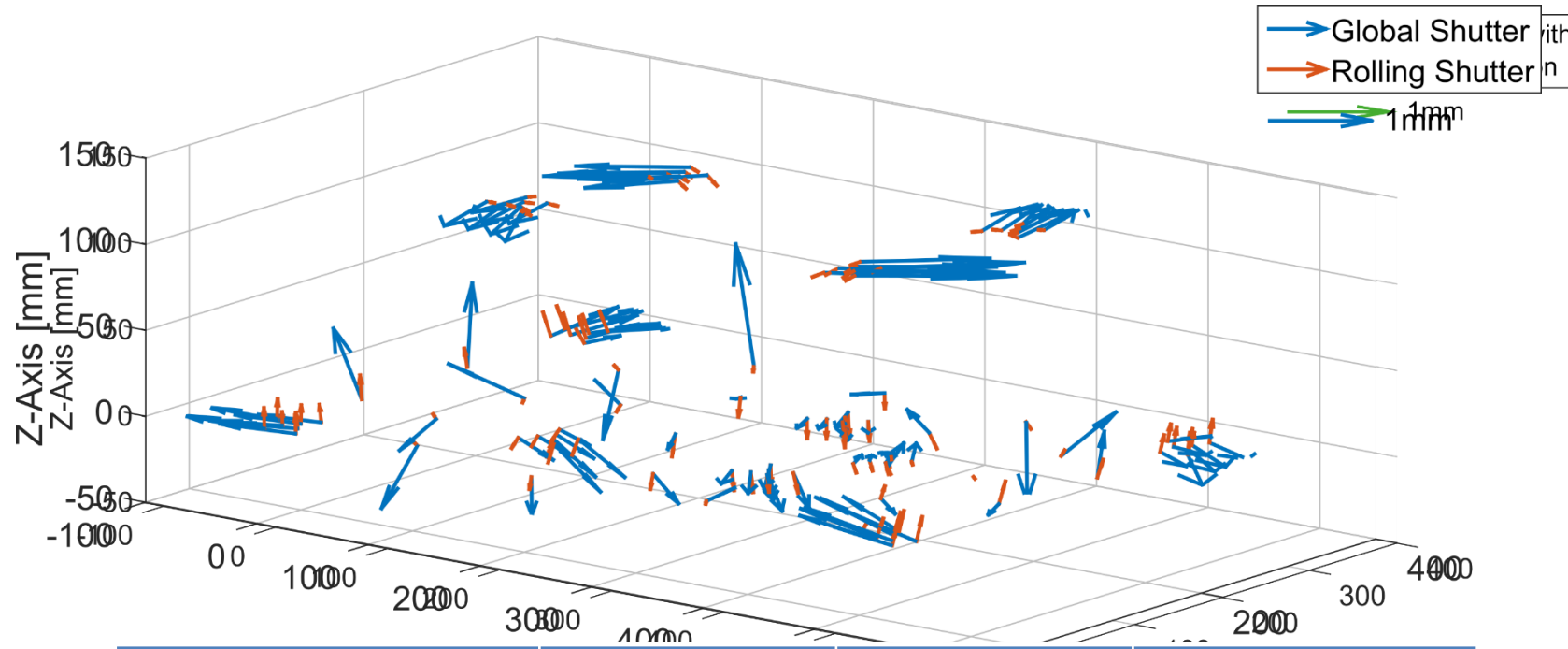
SINGLE IMAGE ANALYSIS - RESULTS



	RMS (XYZ)	Max. Deviation	Relative Accuracy	Not Converged
Global Shutter	1.302 mm	6.072 mm	1:260	0.0 %
Rolling Shutter	0.246 mm	0.920 mm	1:1715	2.7 %

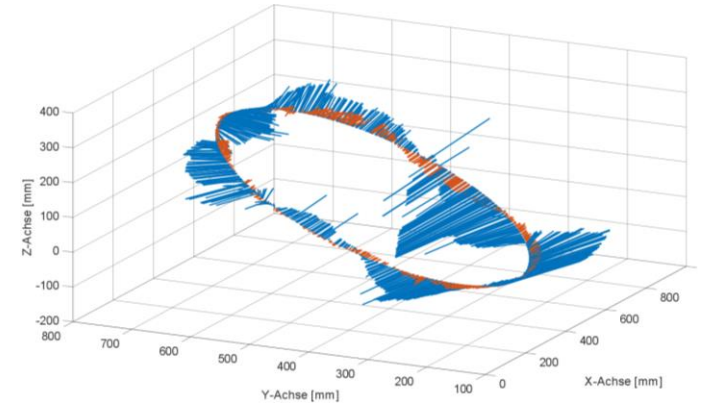
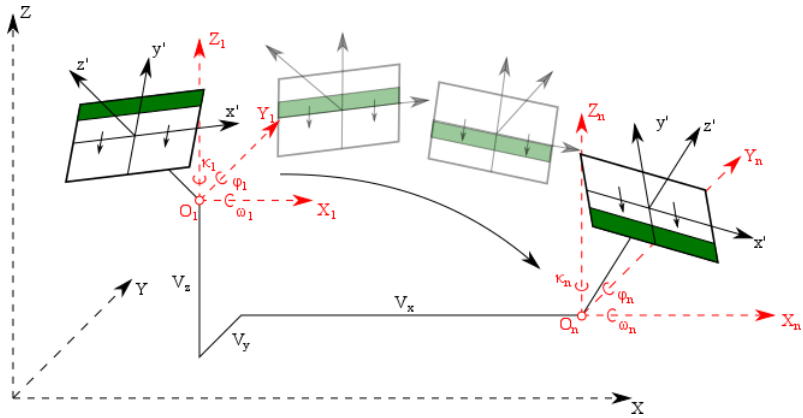


BUNDLE ADJUSTMENT - RESULTS



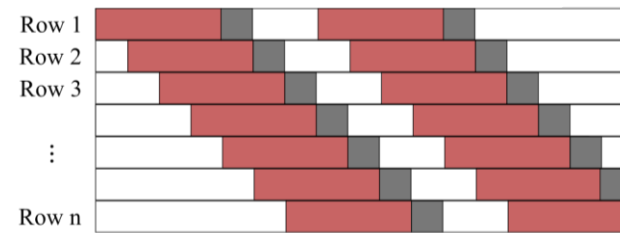
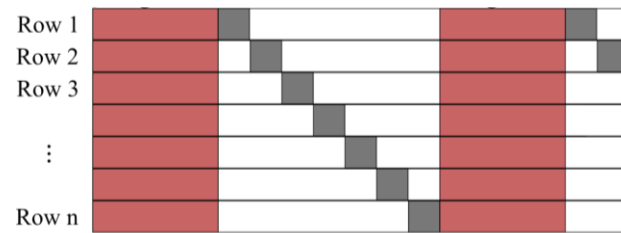
	RMS (XYZ)	Max. Deviation	Relative Accuracy
Global Shutter	0.864 mm	1.910 mm	1:383
Rolling Shutter	0.101 mm	0.183 mm	1:3992
Rolling Shutter with GS-approximation	0.490 mm	1.139 mm	1:642

- The model describes the real conditions
 - Accuracy improvement > factor 5
- Parameters of exterior orientation(s) are highly correlated
 - Singular systems of equations
 - Inaccurate parameter estimation
 - Depth is crucial for a robust estimation
 - Approximate values have high impact on the results of a bundle adjustment
- Outlook
 - Improvement of approximate values/robustness
 - Influence on image measurements
 - Precorrect distorted image for Global Shutter analysis
 - High-speed applications for low cost cameras



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