



3D METROLOGY
CONFERENCE



3DMC presentation

Autocalibration of complex mechatronic systems: Machine tools and robots

by Brahim Ahmed Check & Unai Mutilba

18/09/2025





Outline

WHO WE ARE - TEKNIKER

INTRODUCTION

MACHINE TOOL CALIBRATION

ROBOT CALIBRATION



Outline

WHO WE ARE - TEKNIKER

INTRODUCTION

MACHINE TOOL CALIBRATION

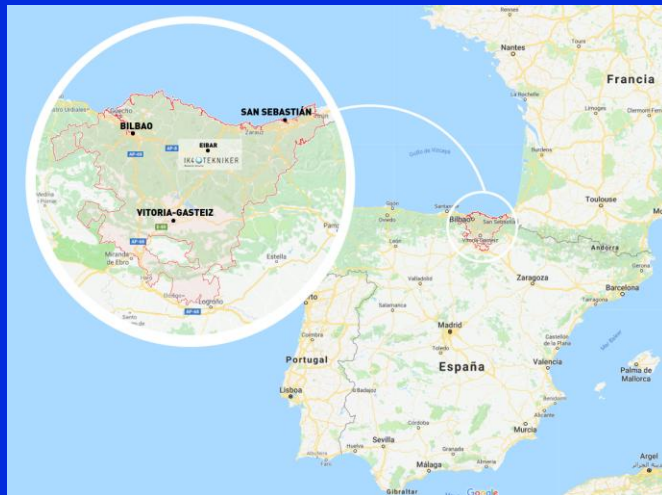
ROBOT CALIBRATION

WHO WE ARE

R&D Centre
(not-for-profit Private Foundation) |
Applied research spanning 45 years

**Our mission is to deliver growth
and wellbeing to society at large
via R&D&I and to further the
competitiveness of the business
fabric in a sustainable manner**

Specialised in Manufacturing





Outline

WHO WE ARE - TEKNIKER

INTRODUCTION

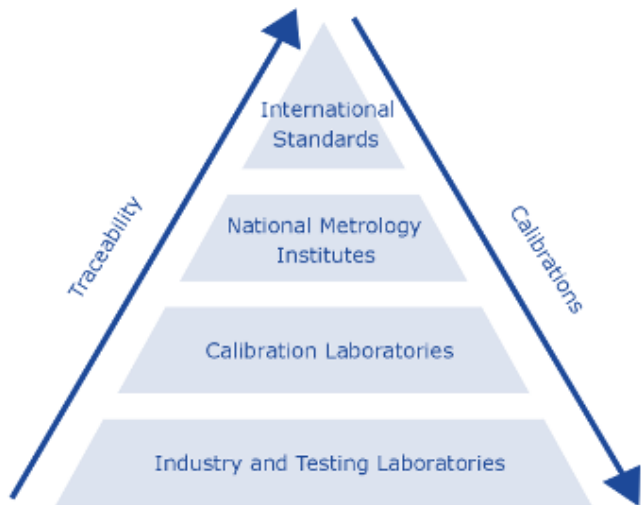
MACHINE TOOL CALIBRATION

ROBOT CALIBRATION



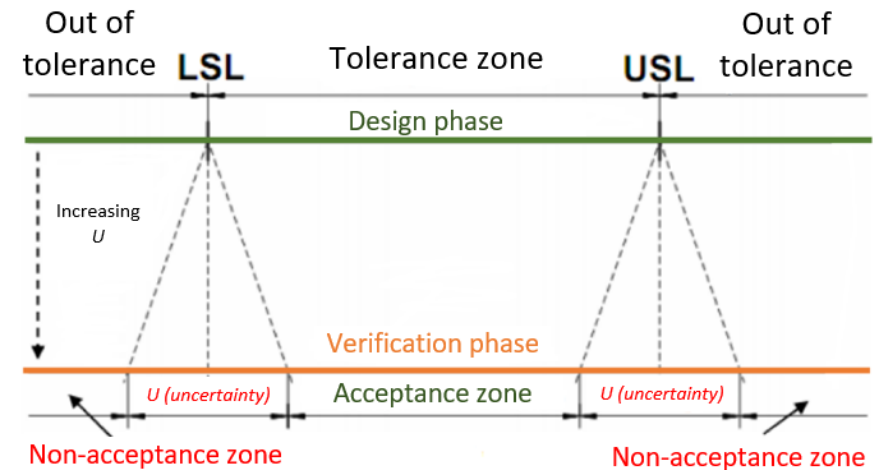
TRACEABILITY

Property of a measurement result whereby the **result can be related to a reference through a documented unbroken chain of calibrations**, each contributing to the measurement uncertainty



UNCERTAINTY

The measurement uncertainty is a **non-negative parameter associated with the result of a measurement**, which characterises the dispersion of values that can be reasonably attributed to that measurement result.



Introduction

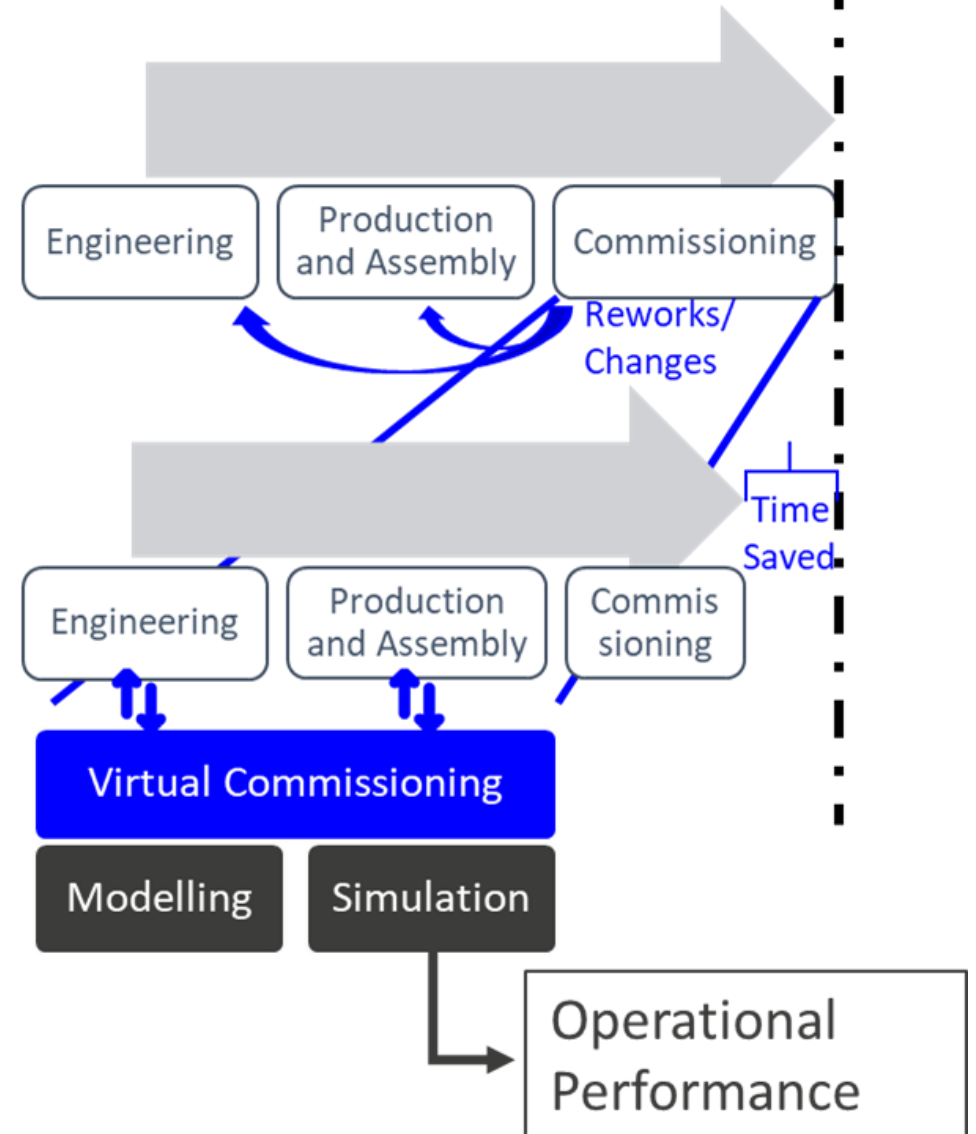
Virtual commissioning

TRADITIONAL

Simulation techniques for validating and optimizing the automation and control systems of machines, robots or industrial plants before physical commissioning.

Errors can be identified and corrected, efficiency improved, and implementation costs and times minimized

Safe virtual environment to test various situations and solutions



Introduction

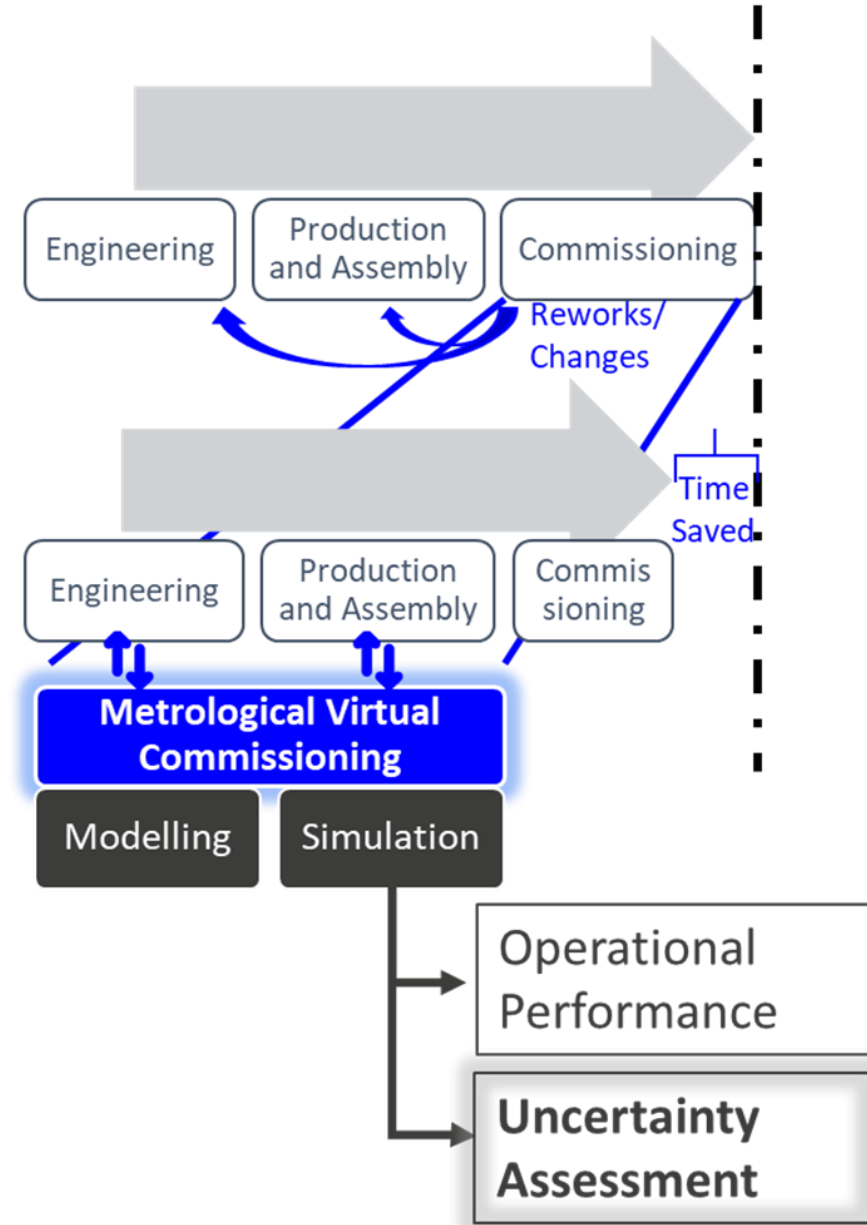
Virtual commissioning + Metrology

METROLOGICAL

Combines virtual commissioning with metrology to ensure models are both functionally accurate and metrologically correct.

Enables comprehensive validation by testing and optimizing both functionality and measurement accuracy in a virtual environment before physical commissioning

Calibration and measurement systems can be virtually tested and optimized to ensure the actual system meets metrological requirements and standards





Outline

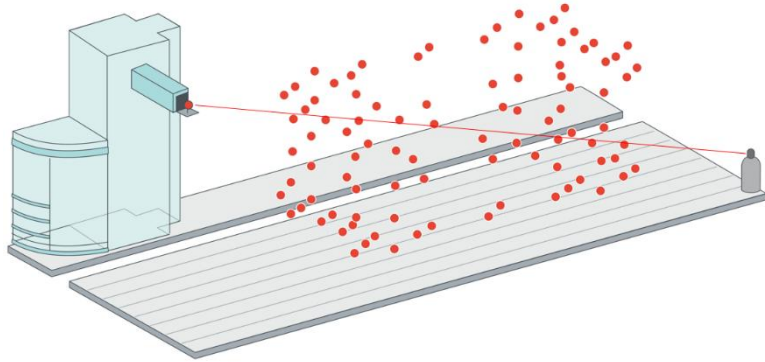
WHO WE ARE - TEKNIKER

INTRODUCTION

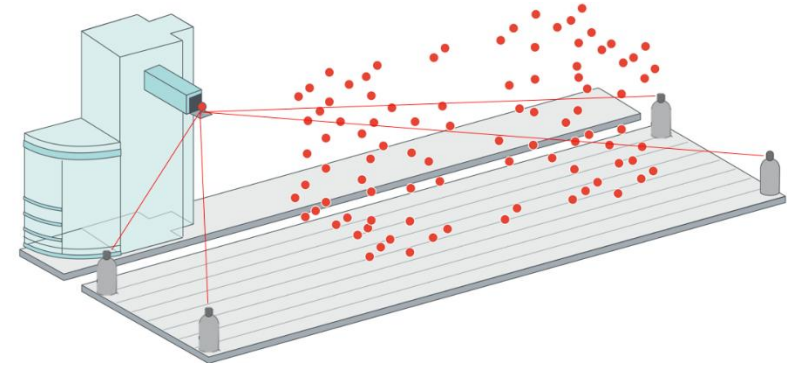
MACHINE TOOL CALIBRATION

ROBOT CALIBRATION

Integrated multilateration - a new approach

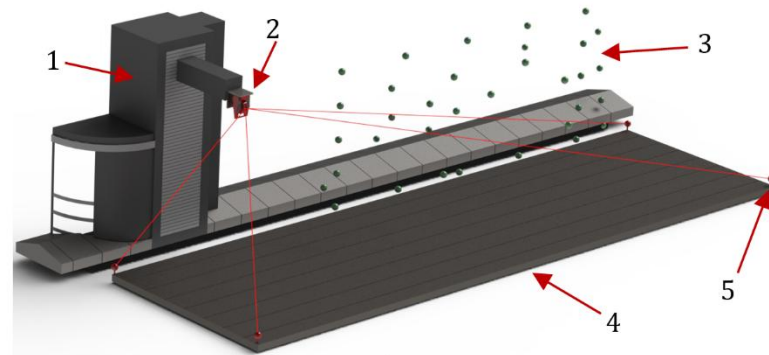


Sequential multilateration approach



Simultaneous multilateration approach

Machine Tool Integrated
Inverse Multilateration
(**MIIM**): Presented in GA
CIRP Tokyo 2018 [1]

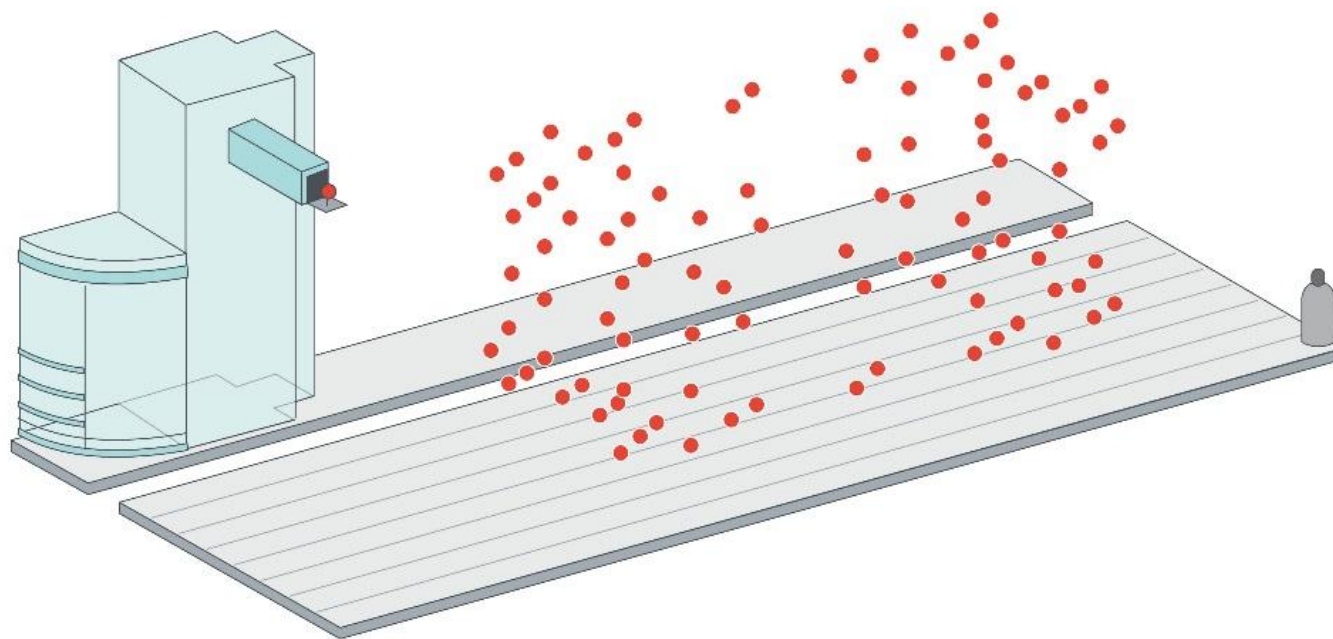


1 Machine tool	4 Machine tool's table
2 Tracking interferometer	5 Fiducial point (x4)
3 Measurement point grid	

MT calibration

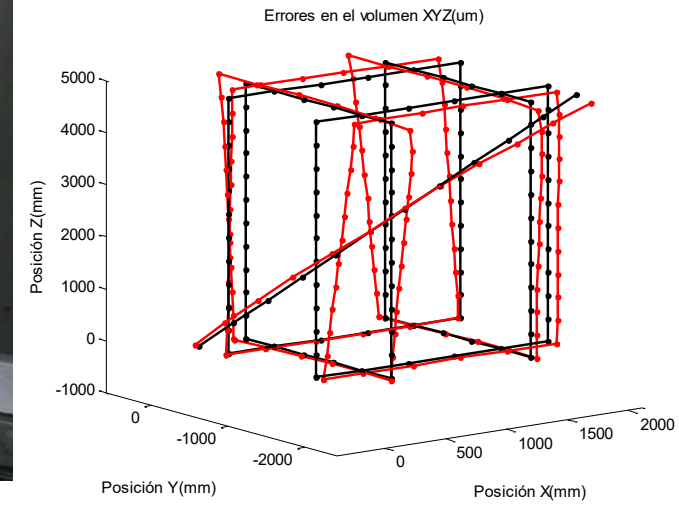
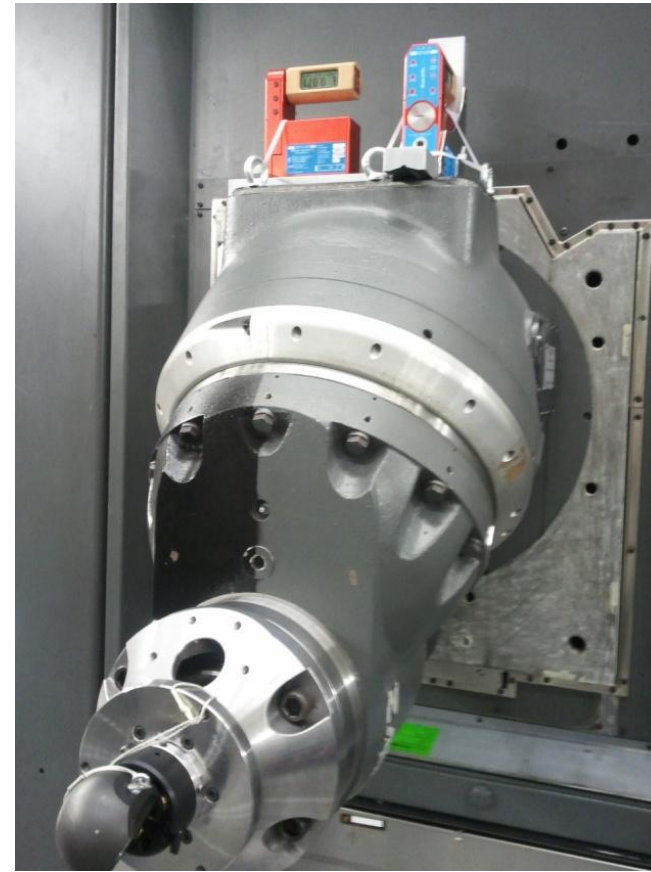
Multilateration based approach for large scale MT error mapping

Interferometric or absolute displacement measurements between tracking interferometers that are fixed to the machine base and a reflector, fixed to the machine spindle, near to the tool centre point (TCP)

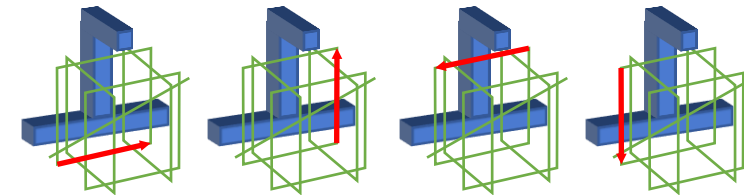
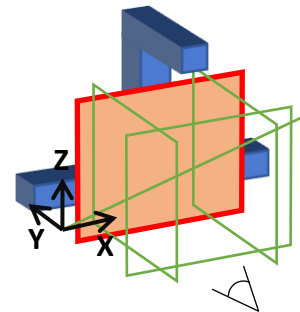




Self-developed solution based on
a AT901 laser tracker and levels



TRADITIONAL
MULTILATERATION –
laser tracker and
electronic levels





Laser tracer technology from ETALON AG



TRADITIONAL
MULTILATERATION –
laser tracer





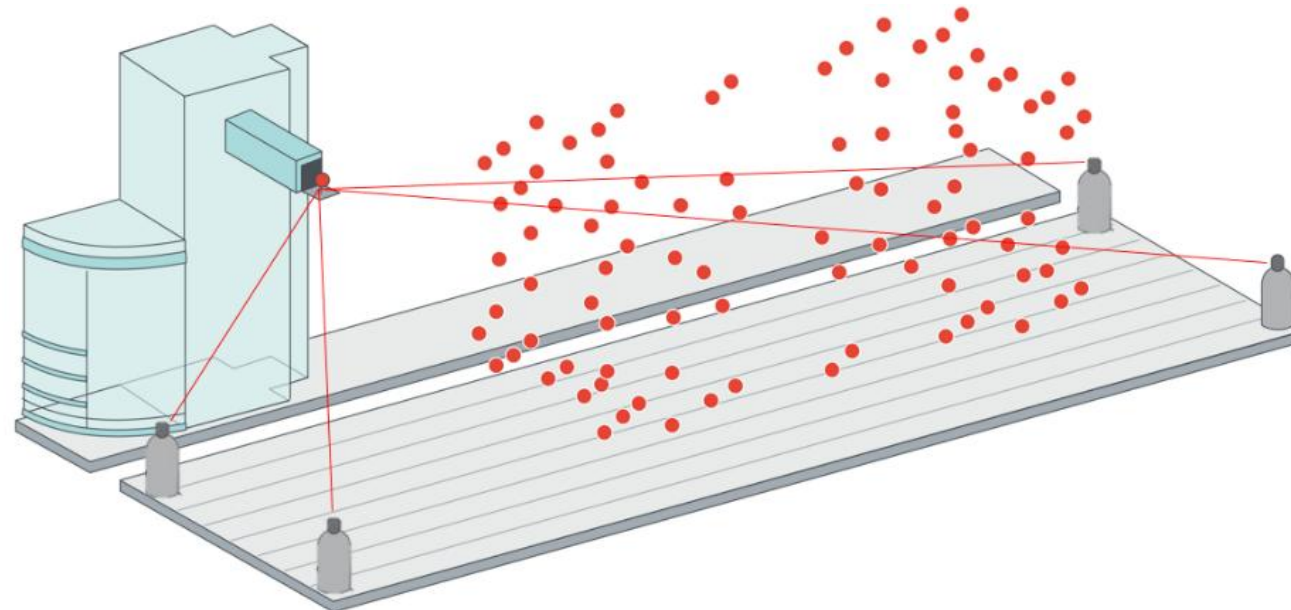
TRADITIONAL
MULTILATERATION –
laser tracer



MT calibration

Simultaneous multilateration approach

Interferometric or absolute displacement measurements between tracking interferometers that are fixed to the machine base and a reflector, fixed to the machine spindle, near to the tool centre point (TCP)

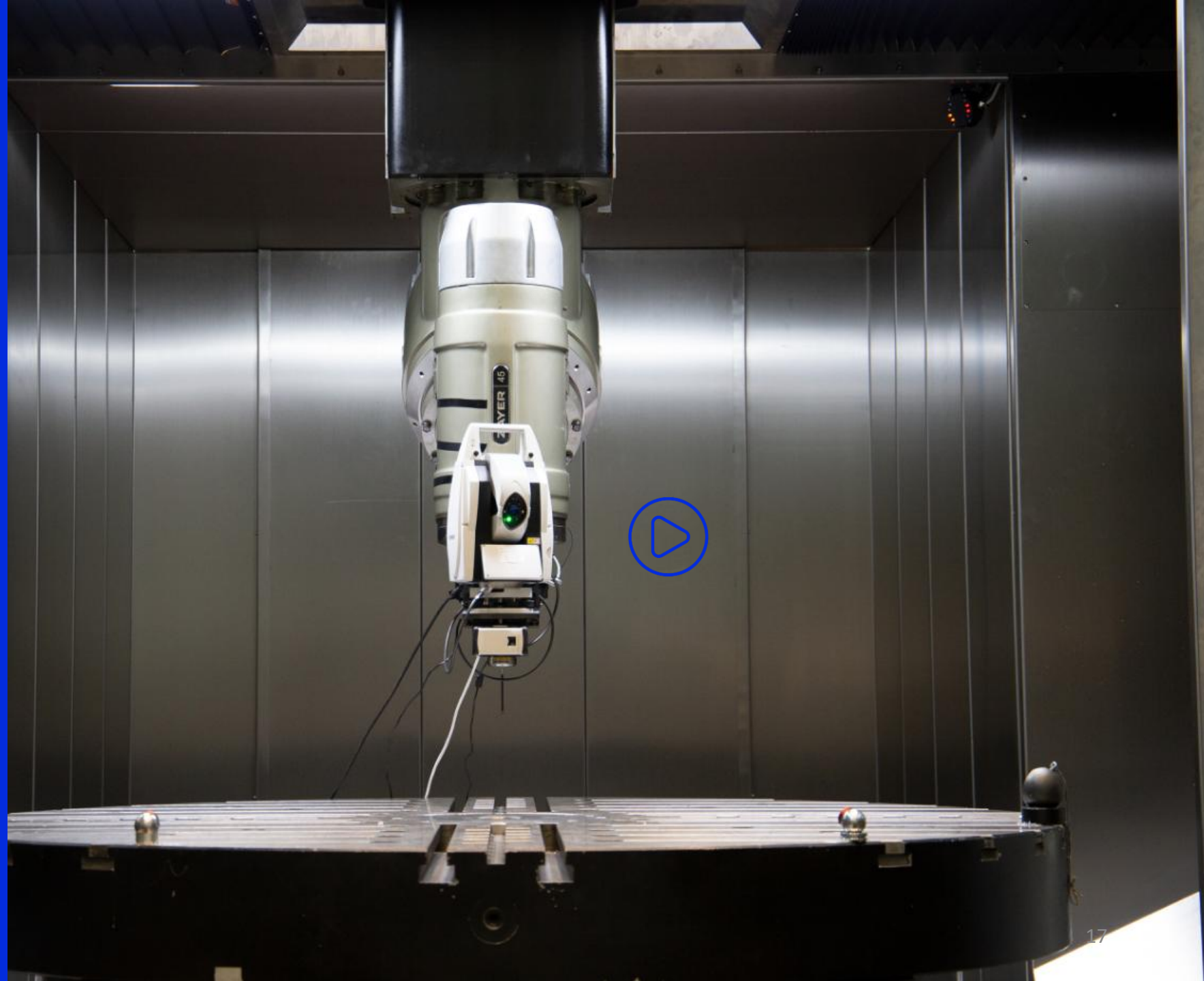




Traditional multilateration has strong limitations:

- **Four tracking interferometers** are needed
 - Sequential multilateration: A unique tracking interferometer is available
 - **Human intervention** is needed for manipulation: Manual intervention to move the tracking interferometer to the next position
 - **MT repeatability**
 - **Time-consuming** approach
 - **Thermal drift**
 - Simultaneous multilateration: Four tracking interferometers are available
 - **High-cost** solution.

SELF-DEVELOPED AND
AUTOMATIC
VOLUMETRIC ERROR
MAPPING APPROACH



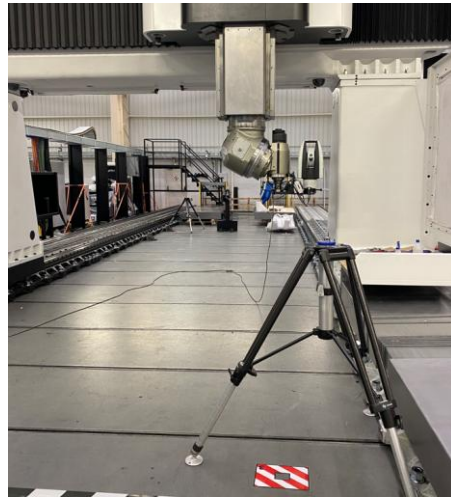
Integrated multilateration - a new approach



Different MT configurations – in collaboration with ZAYER



ZAYER ARION G



ZAYER THERA



ZAYER ARES



ZAYER ZERO

More to come...

Error modelling and compensation of MTs

In MTs, 21 components of error kinematic models

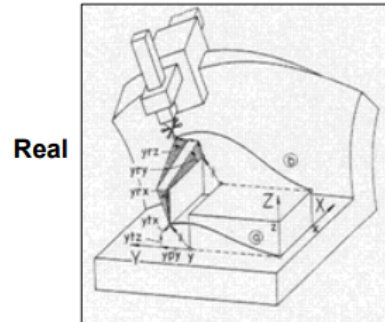
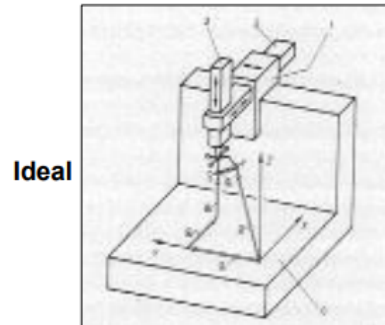
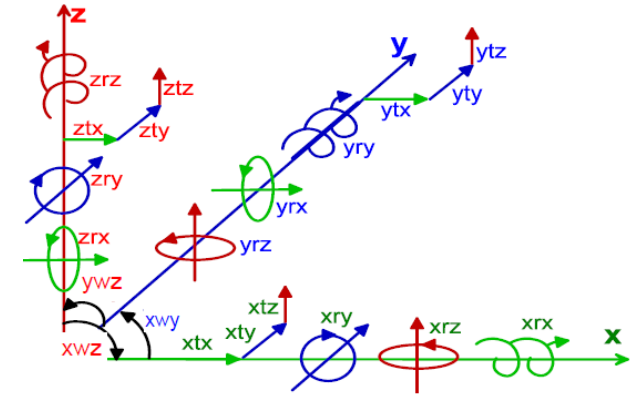
$$E = P + A * X + A_p * X_p$$

error vector at position X+X_p
 translational errors
 rotatorical errors
 probe-offset vector
 position of reference probe

$$A = \begin{bmatrix} 0 & -ywx & -xrz & +zwx & +xry & +yry \\ 0 & 0 & 0 & -zwy & -xrx & -yrx \\ 0 & +xrx & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$A_p = \begin{bmatrix} 0 & -xrz & -yrz & -zrz & +xry & +yry & +zry \\ +xrz & +yry & +zry & 0 & -xrx & -yrx & -zrx \\ -xry & -yry & -zry & +xrx & +yry & +zry & 0 \end{bmatrix}$$

$$X = \begin{bmatrix} x \\ y \\ z \end{bmatrix} \quad X_p = \begin{bmatrix} x_p \\ y_p \\ z_p \end{bmatrix} \quad P = \begin{bmatrix} xtx + ytx + ztx \\ yty + xty + zty \\ ztz + xtz + ytz \end{bmatrix}$$



For each linear axis X, Y and Z in total 6 geometric errors can appear (T: Translatory R: Rotatory) :

- Positioning XTX YTY ZTZ
- Straightness XTY XTZ YTX YTZ ZTX ZTY
- Yaw XRZ YRZ ZRX
- Pitch XRY YRX ZRY
- Roll XRX YRY ZRZ

For 3 linear axes this means 18 error sources in total.

Additionally the 3 squareness errors of the linear axes must be taken into account:

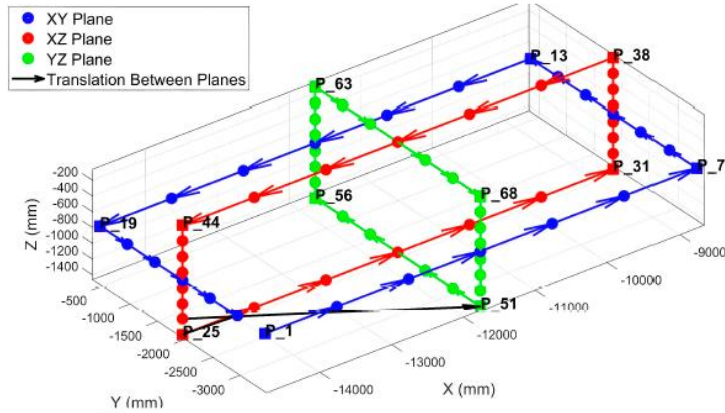
- x ⊥ y XWY
- x ⊥ z XWZ
- y ⊥ z YWZ

In total 21 geometric errors have to be handled for a 3-axes machine tool.

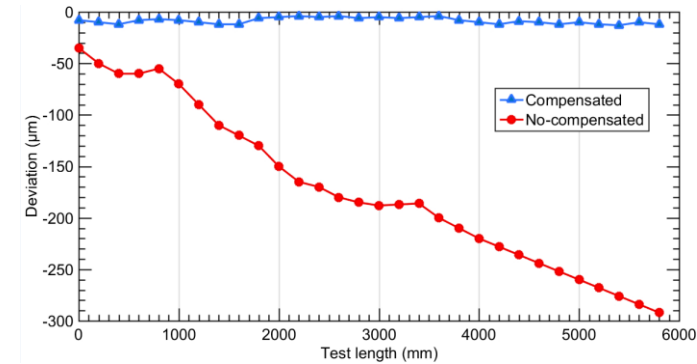
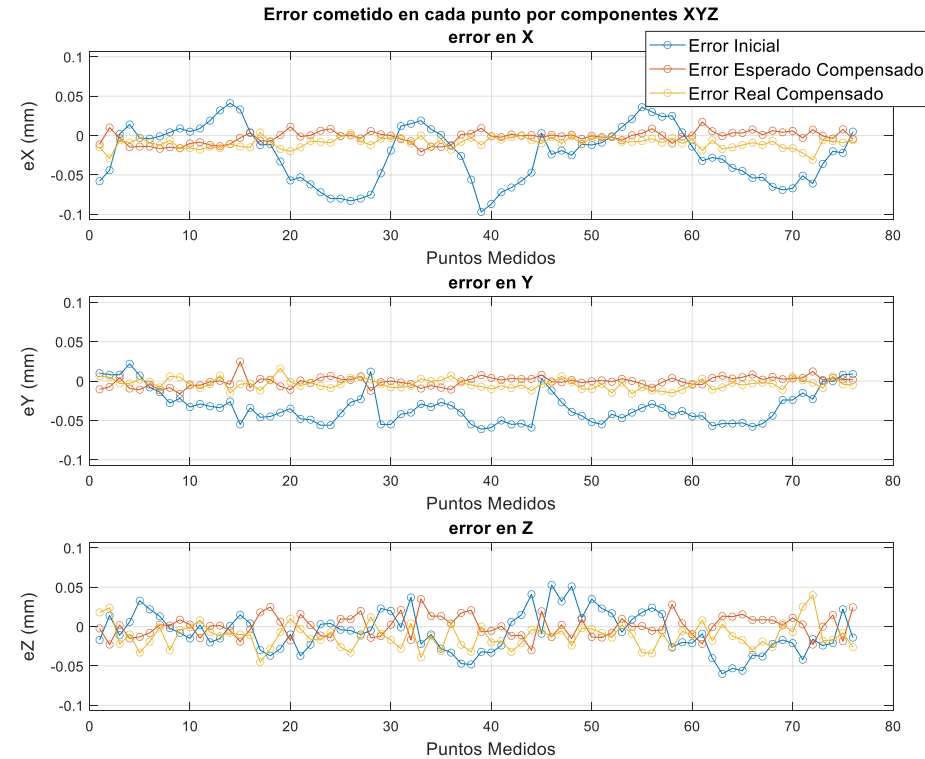


Error modelling and compensation of MTs

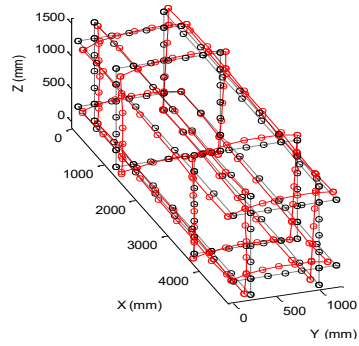
Measurement strategy



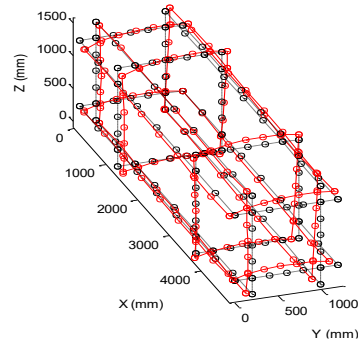
Some results



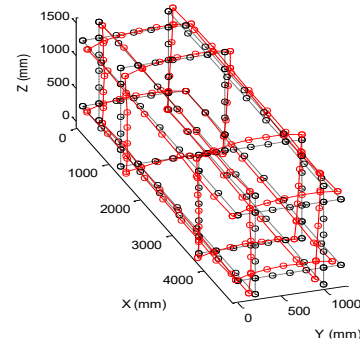
Thermal characterisation of MTs



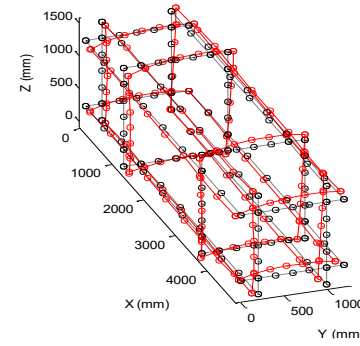
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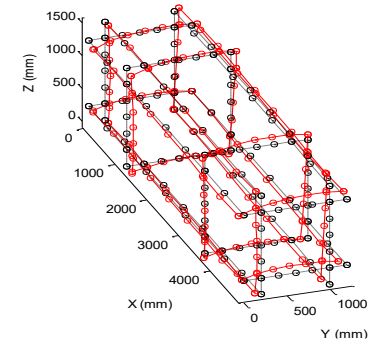
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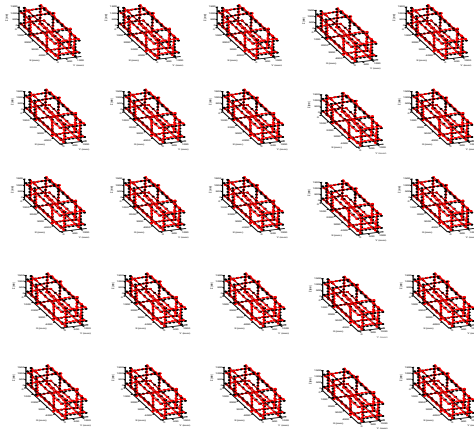
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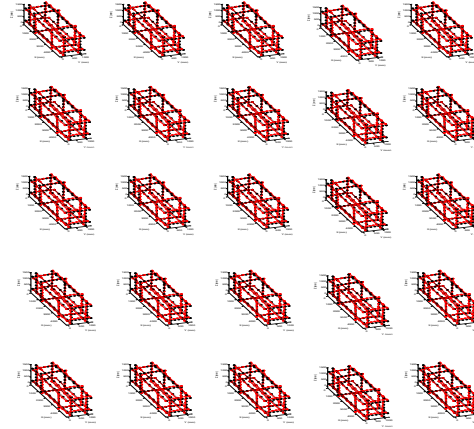
11:15



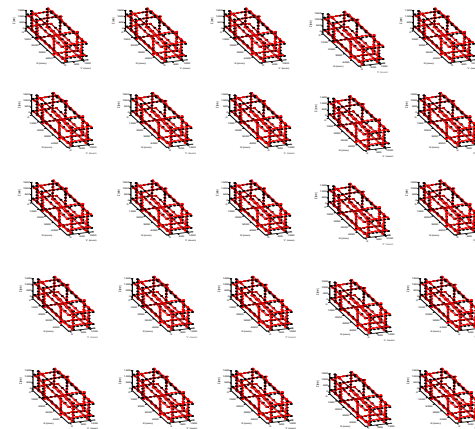
12:00



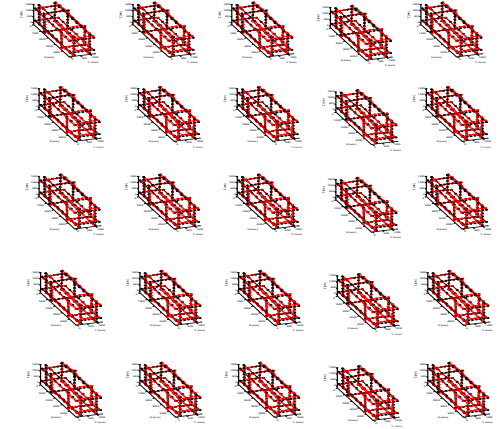
Monday



Tuesday



Wednesday



Thursday

Thermal characterisation of MTs



Measurement setup:

Machine tool: ZAYER ZERO model (non-controlled environment)

CNC: Heidenhain.

MIIM setup:

AT960 LEICA laser tracker integrated on the MT head.

4 wide-angle retro-reflectors: Two on the table and two on a height.

Measurement volume:

X: $-2.650 \div -1.350$ (1.300 mm) step 260 mm.

Y: $-1.300 \div -100$ (1.200 mm) step 240 mm.

Z: $-1.150 \div -50$ (1.100 mm) Step 100 mm.

Point cloud: 84 points

Measurement sequence:

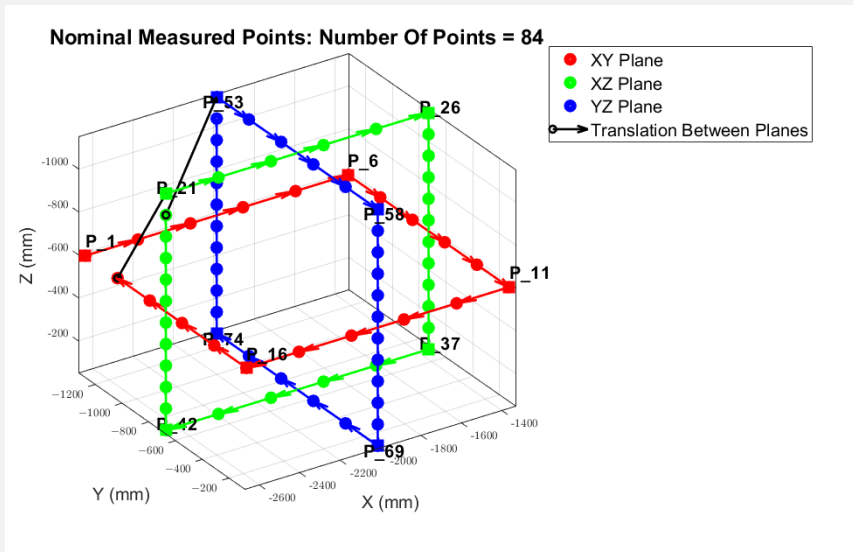
1st: Plane XY : XX↑ YY ↑ XX ↓ YY↓

2nd: Plane XZ : XX↑ ZZ ↑ XX ↓ ZZ↓

3rd: Plano YZ : YY↑ ZZ ↑ YY ↓ ZZ↓

Total measurement time: Aprox. 10 days(300 repetitions)

Time resolution: 45 min/volume.



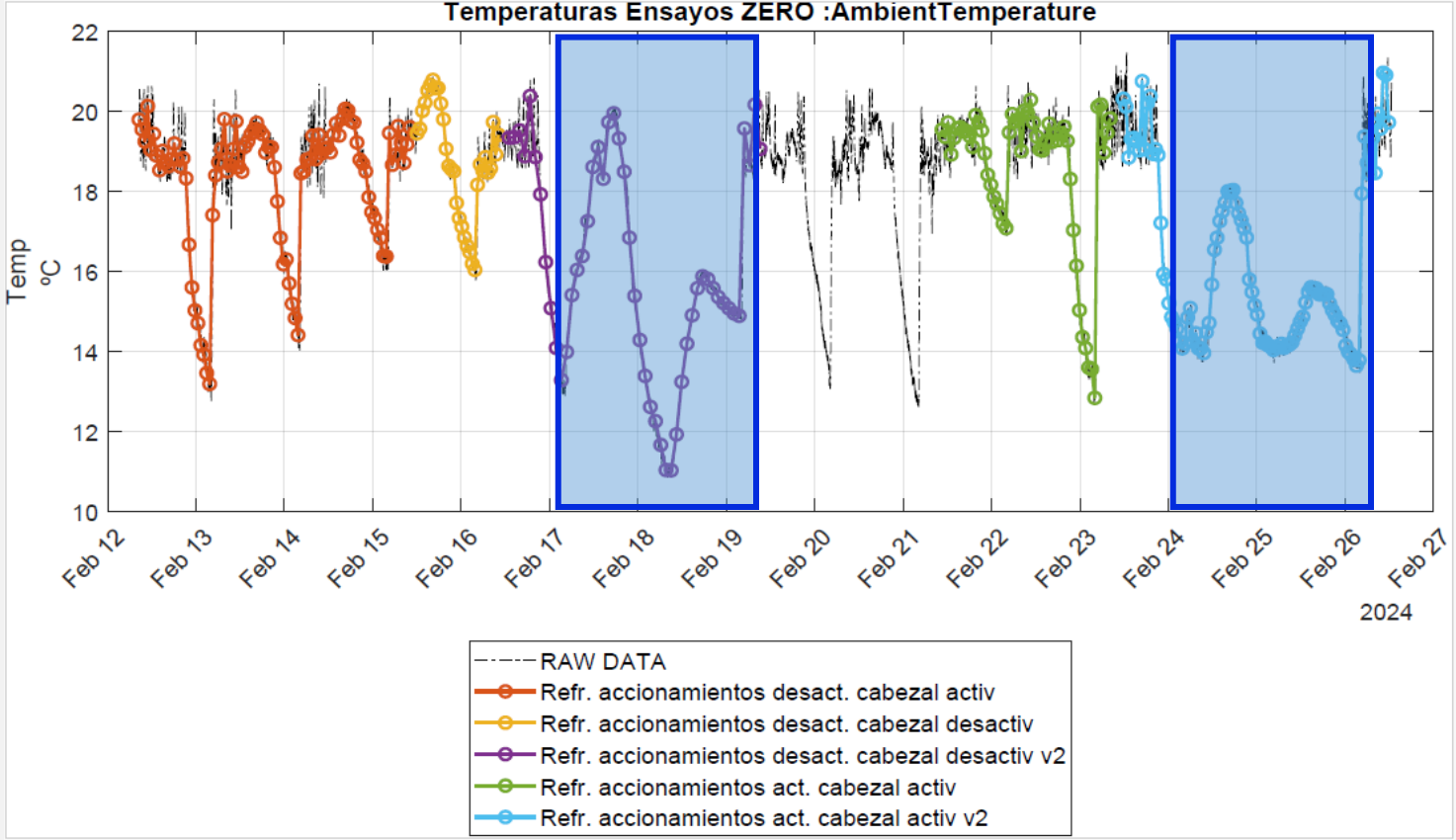
Thermal characterisation of MTs



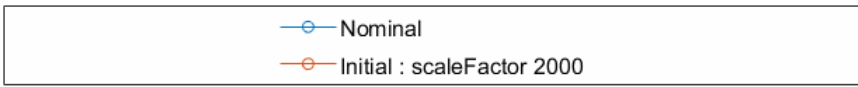
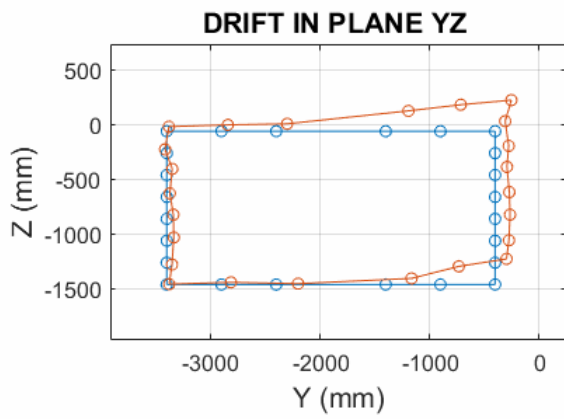
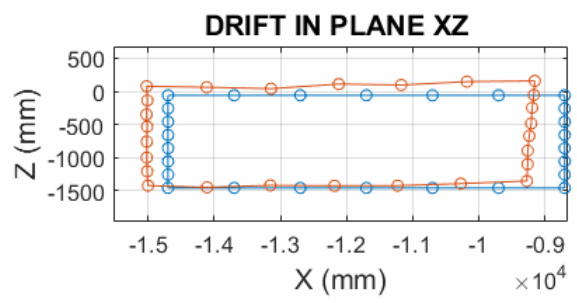
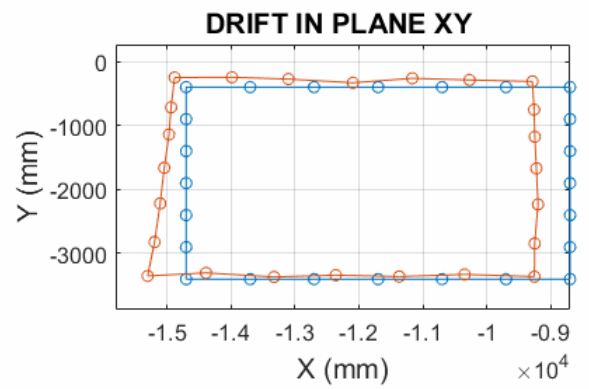
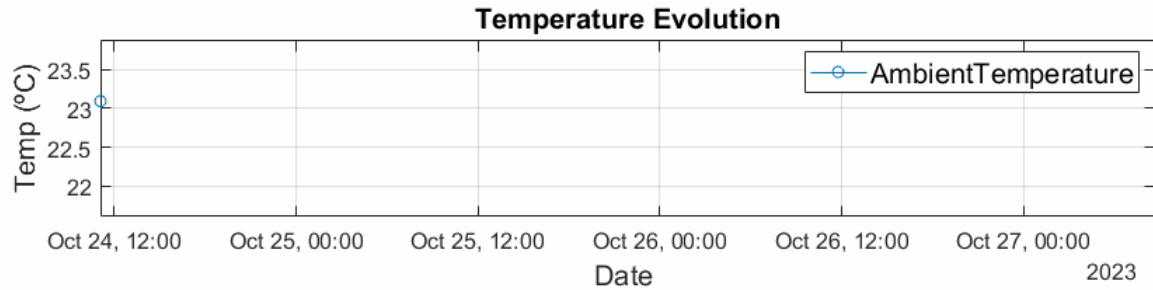
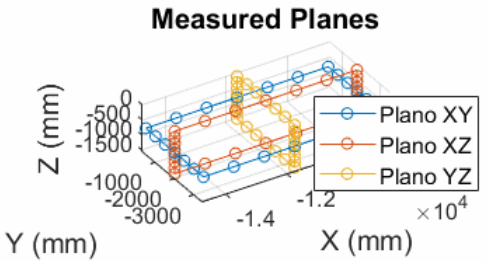
Measurement data:
Temperature: Ambient
temperature variation 7°C
(non-controlled environment)



Weekend



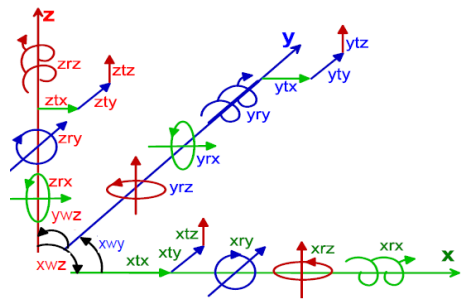
Thermal characterisation of MTs



Thermal characterisation of MTs – coordinate measurements



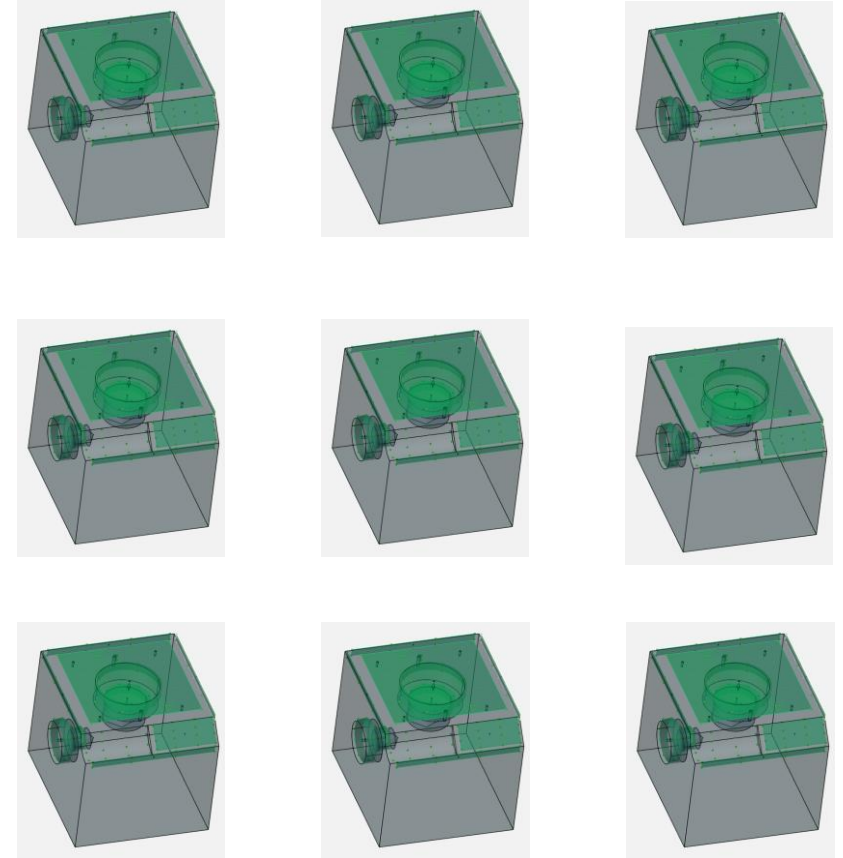
GD&T sensibility to the ambient temperature variation – Ongoing research...




ZEISS Quality Suite



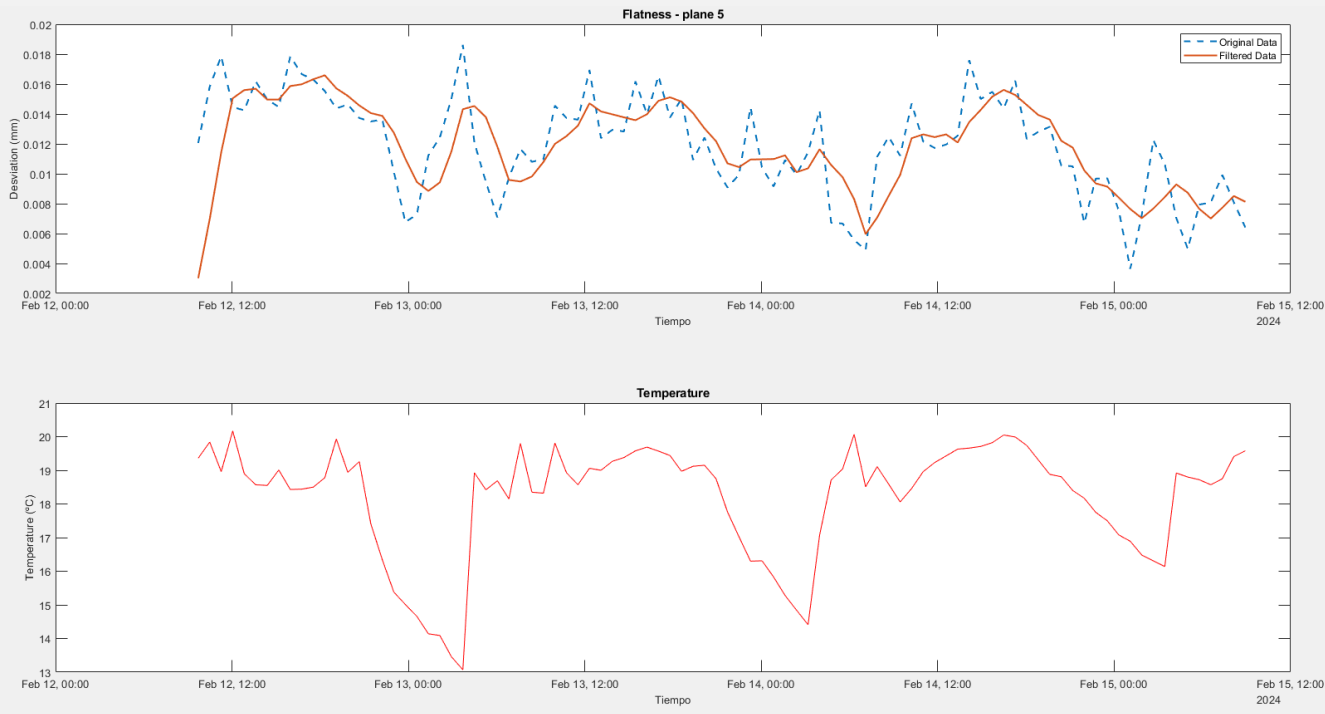
```
Automatic_processing_GDT.py
1 # -*- coding: utf-8 -*-
2
3 import glob
4 import os
5
6
7 # Funcion para obtener los archivos txt en el directorio seleccionado
8 def get_rot_count(dir):
9     num_file = 0
10
11     # Get all files in folder dir
12     array_files = os.fsencode(dir)
13
14     # Definir una lista vacia
15     array_files_txt = []
16
17     # Create selected txt file list and number of files
18     for file in os.listdir(array_files):
19         filename = os.fsdecode(file)
20         if filename.endswith(".txt") :
21             num_file +=1
22             array_files_txt.append(filename)
23             continue
24         else:
25             continue
26
27 # Verify data of the function
28 print('Numero archivos .txt = ')
29 print("\t",num_file,"\n")
30
31 print('Lista de los archivos .txt seleccionados')
32 print("\t",array_files_txt,"\n")
33
34 print('Numero de elementos en la lista de archivos.txt seleccionados = ')
35 print("\t",len(array_files_txt),"\n")
36
37 return array_files_txt, num_file
38
39
```



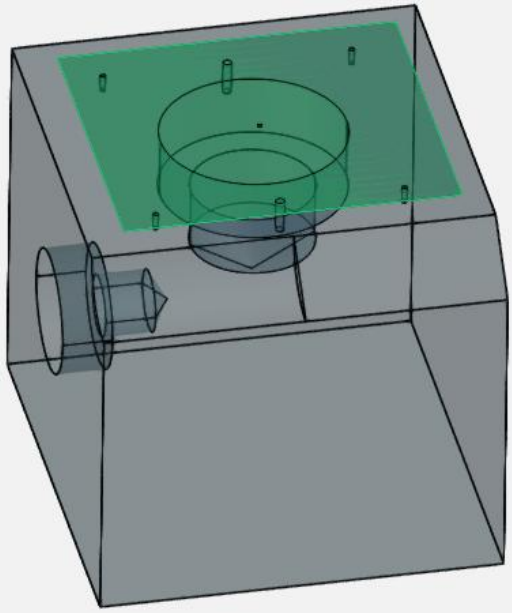
Thermal characterisation of MTs – coordinate measurements



Some preliminary results:



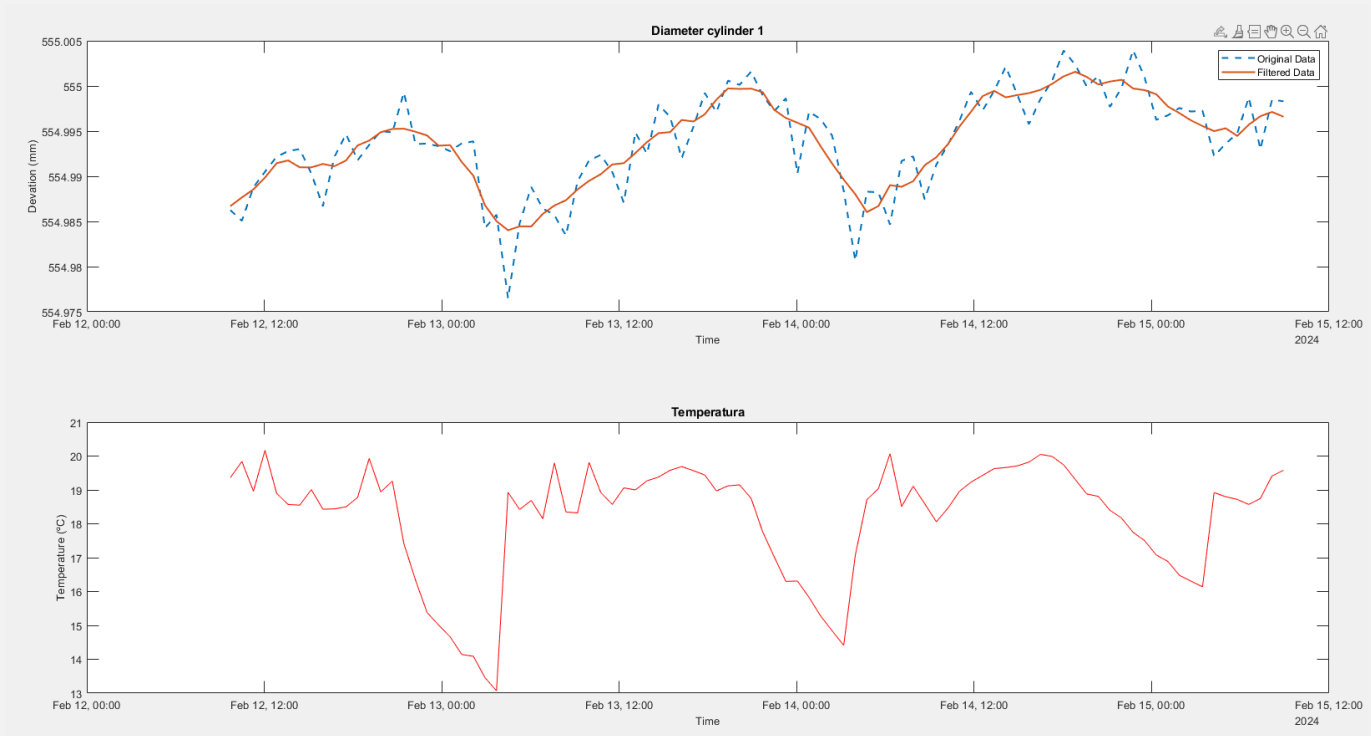
Flatness upper plane



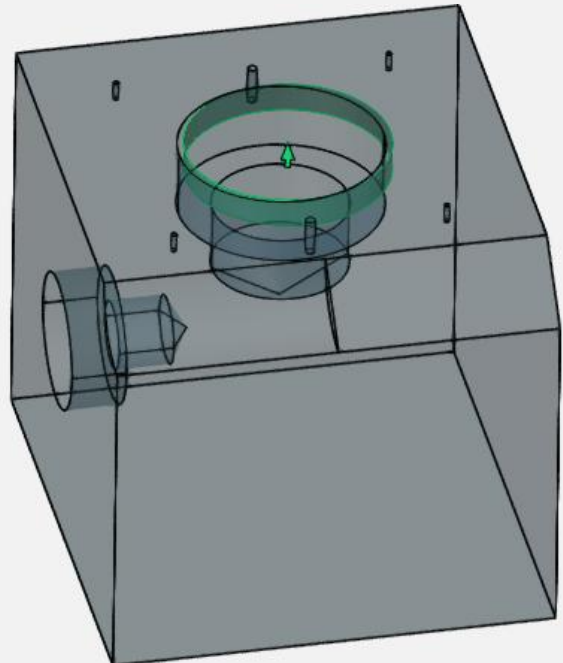
Thermal characterisation of MTs – coordinate measurements



Some preliminary results:



Diameter – upper plane





Outline

WHO WE ARE - TEKNIKER

INTRODUCTION

MACHINE TOOL CALIBRATION

ROBOT CALIBRATION

ROBOT CALIBRATION

WHAT IS IT ABOUT?

Determination of the real DH kinematic parameters and elastic model

Defined by theoretical values

Not ensured during component manufacturing

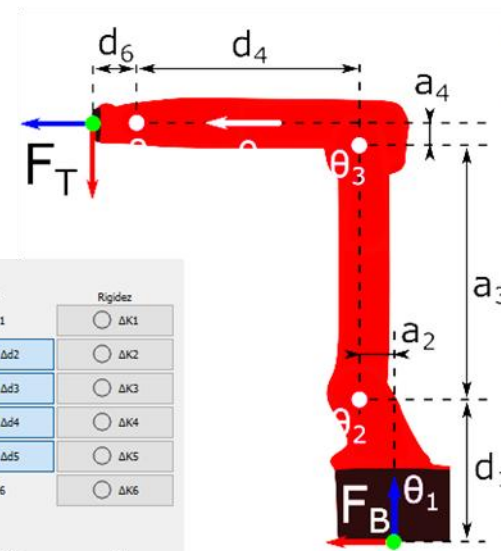
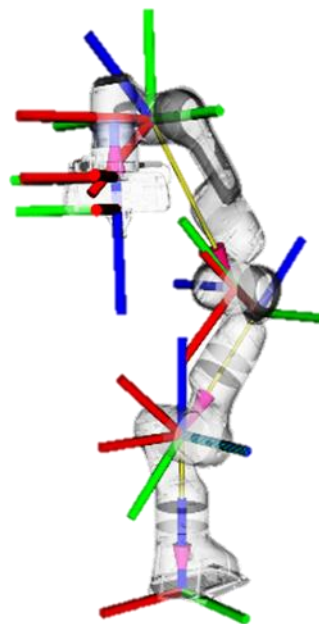


Tabla D-H M

	α	a	θ	d	Rigidez
31	$\Delta\alpha_1$	Δa_1	$\Delta\theta_1$	Δd_1	<input type="radio"/> ΔK_1
32	<input checked="" type="radio"/> $\Delta\alpha_2$	<input checked="" type="radio"/> Δa_2	<input checked="" type="radio"/> $\Delta\theta_2$	<input checked="" type="radio"/> Δd_2	<input type="radio"/> ΔK_2
33	<input checked="" type="radio"/> $\Delta\alpha_3$	<input checked="" type="radio"/> Δa_3	<input checked="" type="radio"/> $\Delta\theta_3$	<input checked="" type="radio"/> Δd_3	<input type="radio"/> ΔK_3
34	<input checked="" type="radio"/> $\Delta\alpha_4$	<input checked="" type="radio"/> Δa_4	<input checked="" type="radio"/> $\Delta\theta_4$	<input checked="" type="radio"/> Δd_4	<input type="radio"/> ΔK_4
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	X	Y	Z	Rx	Ry	Rz
Base	<input checked="" type="radio"/> ΔB_x	<input checked="" type="radio"/> ΔB_y	<input checked="" type="radio"/> ΔB_z	<input checked="" type="radio"/> ΔB_{rx}	<input checked="" type="radio"/> ΔB_{ry}	<input checked="" type="radio"/> ΔB_{rz}
Herramienta	<input checked="" type="radio"/> ΔT_x	<input checked="" type="radio"/> ΔT_y	<input checked="" type="radio"/> ΔT_z	<input checked="" type="radio"/> ΔT_{rx}	<input checked="" type="radio"/> ΔT_{ry}	<input checked="" type="radio"/> ΔT_{rz}

ROBOT CALIBRATION

HOW IT WORKS?

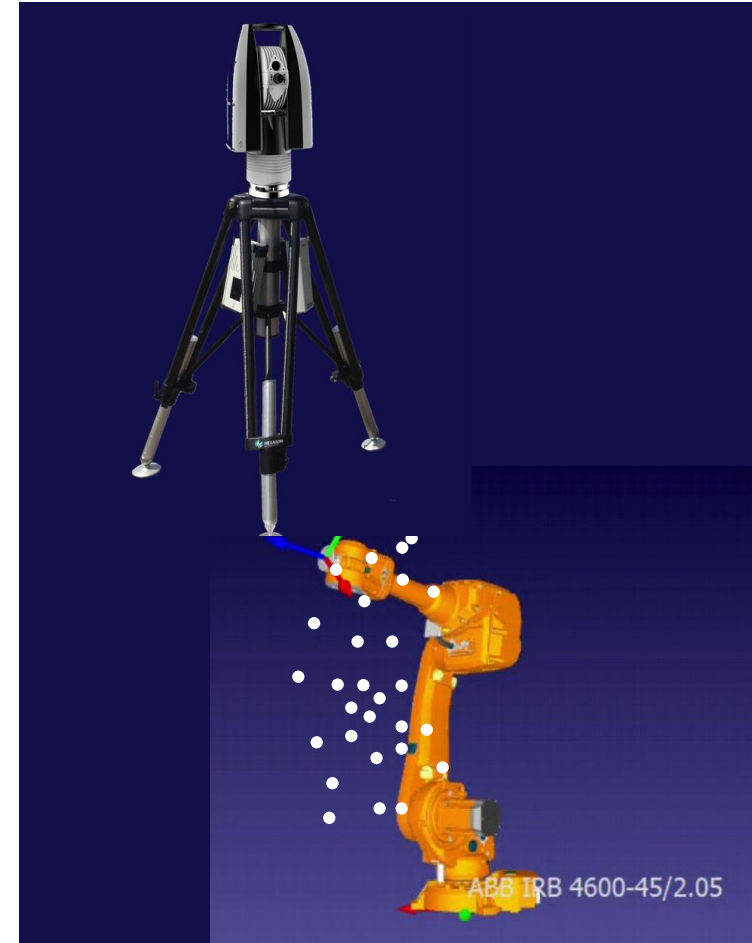
Using an internal or external metrology framework (ISO 9283)



Measurement of the points in the region of interest



Adjustment of the DH parameters minimizing robot error positioning



ROBOT CALIBRATION

WHY IS IT NEEDED?

Demanding robot-based manufacturing applications

Improvement of the robot absolute accuracy

Robot repeatability 20-50 μm ,

Absolute accuracy before calibration 1-2mm

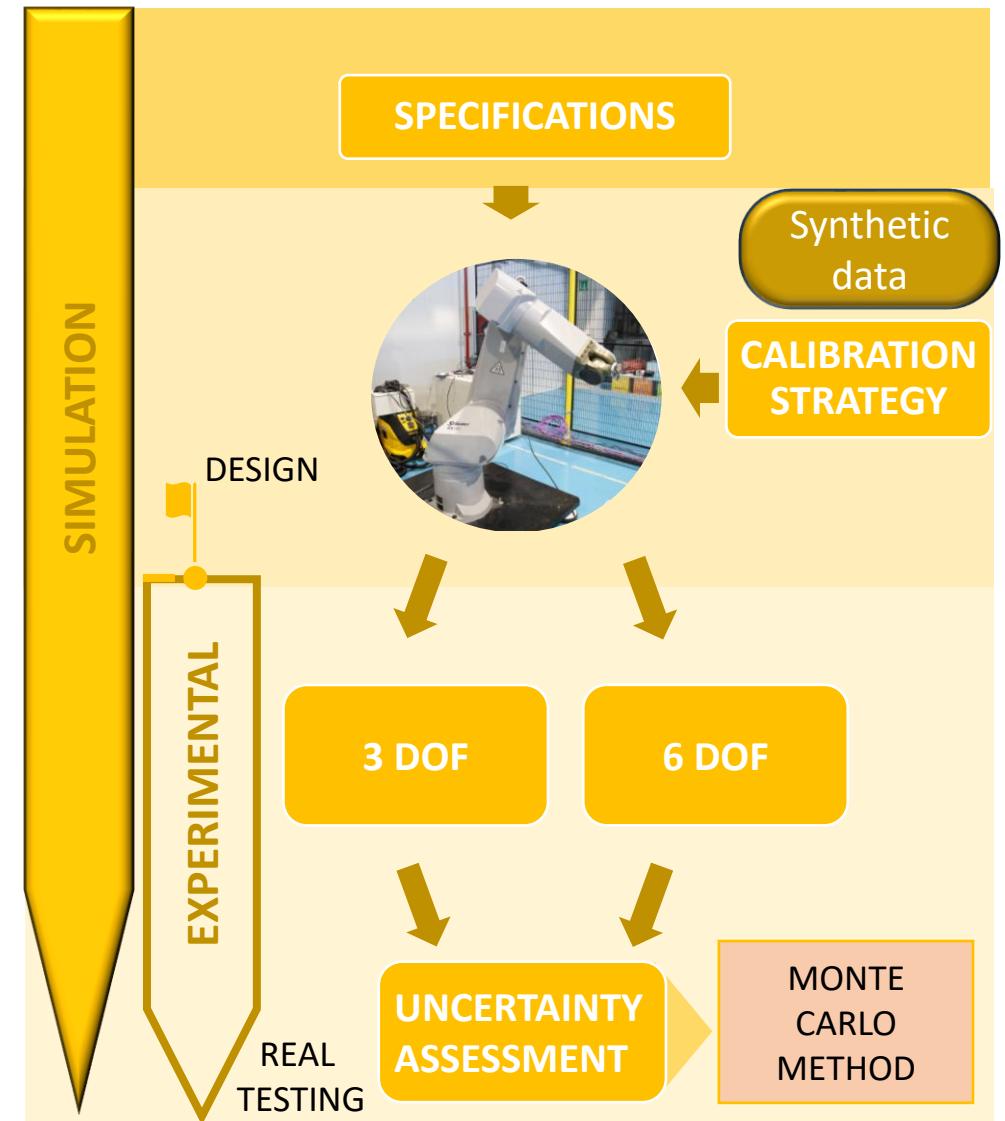
Absolute accuracy improvement after calibration up to 10x



WORKFLOW DIAGRAM

Simulation stages:

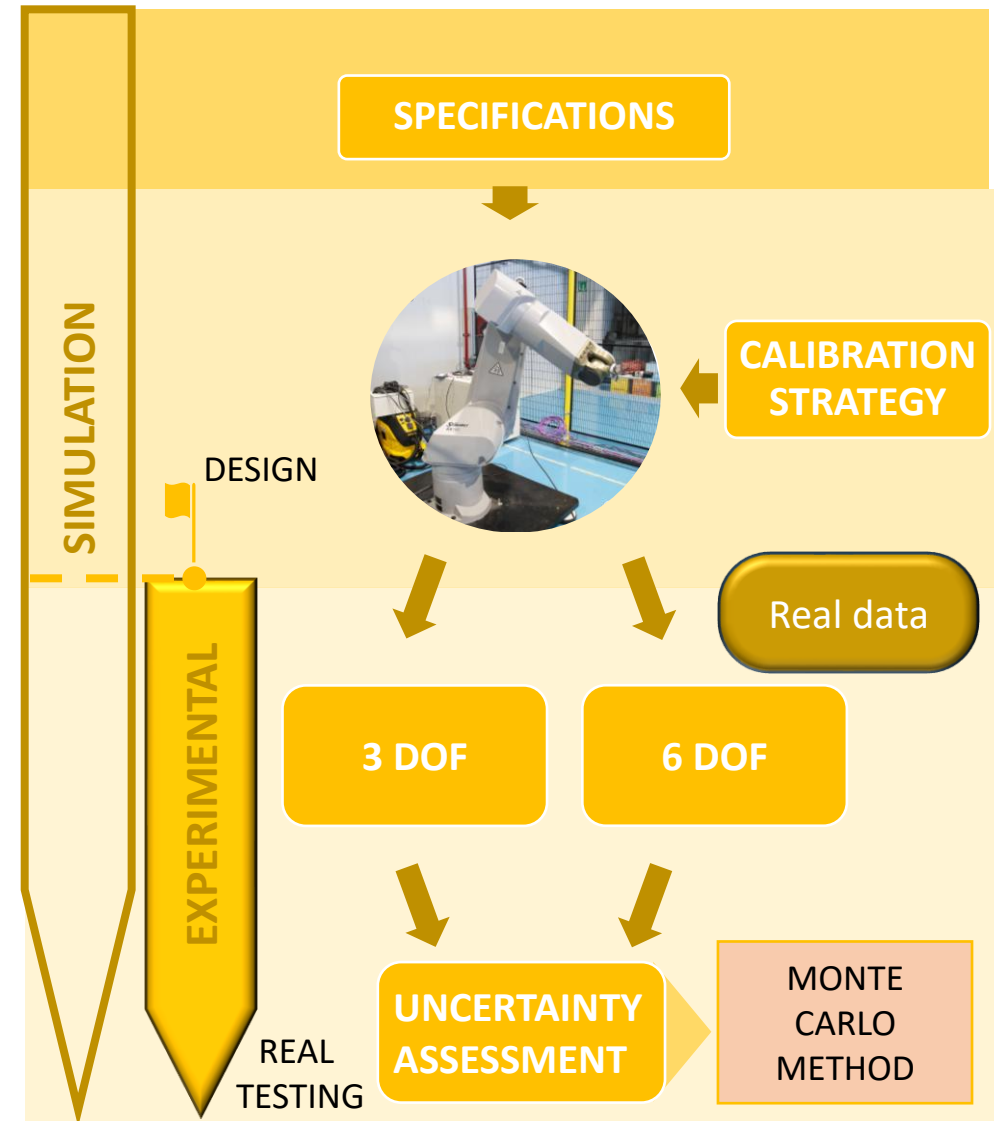
- Develop a dynamic digital twin to simulate real-world behaviors for metrological analysis and optimization.
- Use existing equipment data to generate synthetic data, including uncertainties, for realistic system evaluation.
- Assess overall system uncertainty with synthetic data to ensure compliance with specifications and standards prior to physical deployment.



WORKFLOW DIAGRAM

Experimental stages:

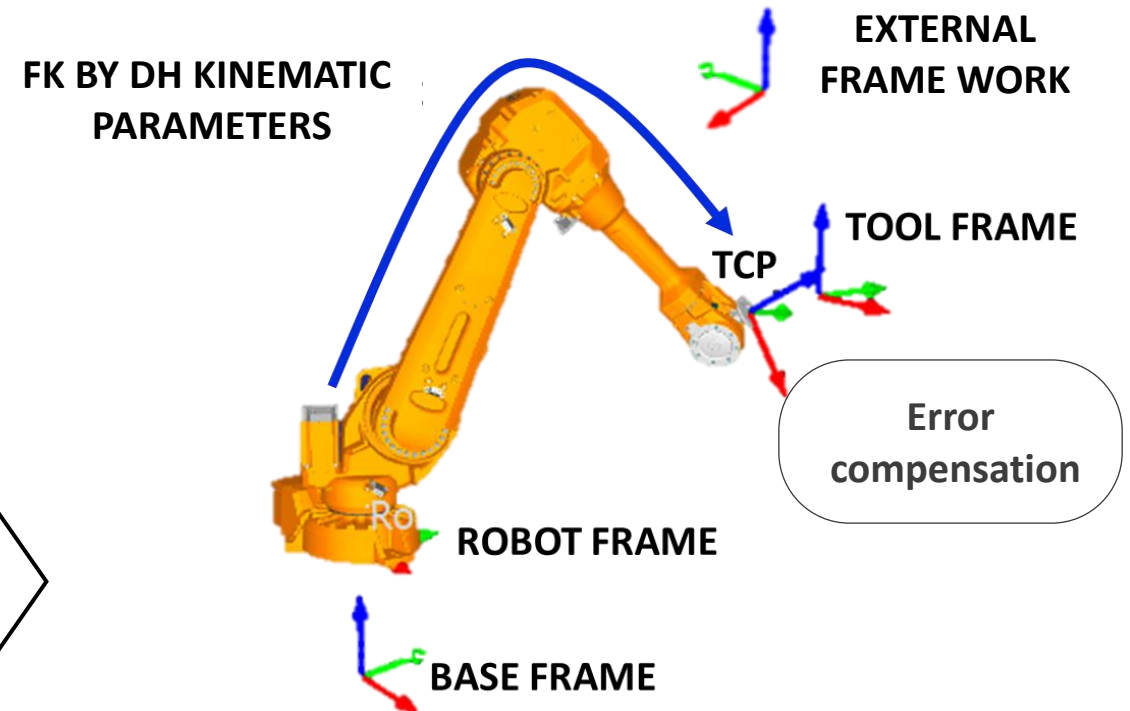
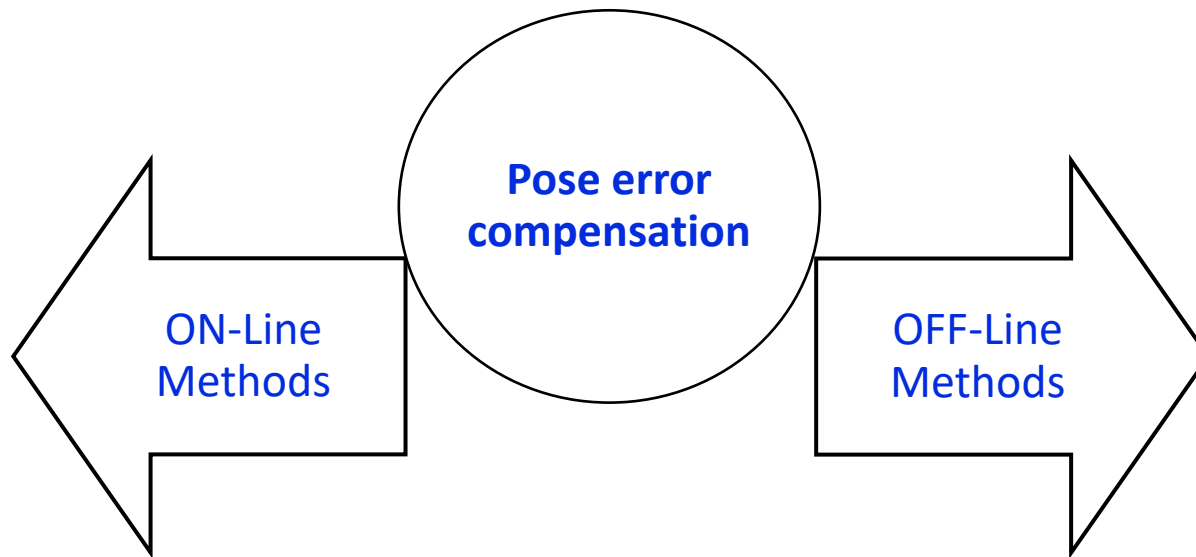
- Transition from virtual optimization to real-world implementation of the auto-calibration solution, using actual data to improve accuracy
- Continuously update the digital twin with operational data to simulate true system performance and uncertainties.
- Integrate real data into the digital twin for precise assessment and refinement, ensuring compliance with metrological standards.





ROBOT COMPENSATION STRATEGIES

CURRENT APPROACHES

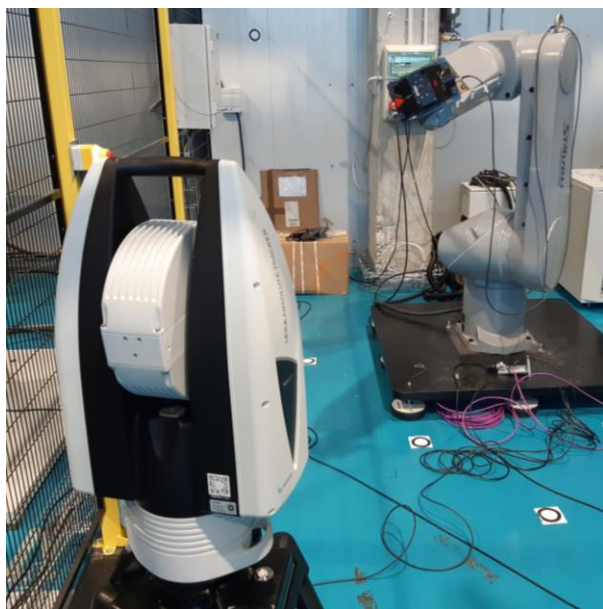


ROBOT COMPENSATION STRATEGIES

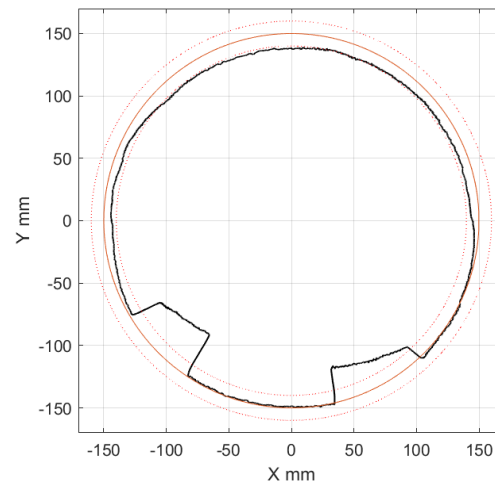
REAL CASE 1 TEKNIKER

- RTFP compensation
- Laser tracker
- 1000 Hz
- Error in robot repeatability order

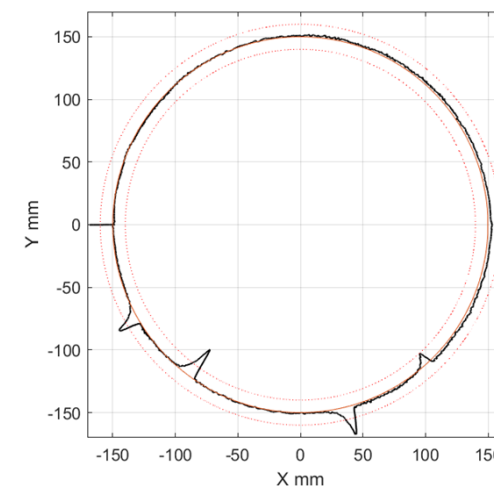
ON-LINE METHODS



Without Compensation



With Compensation



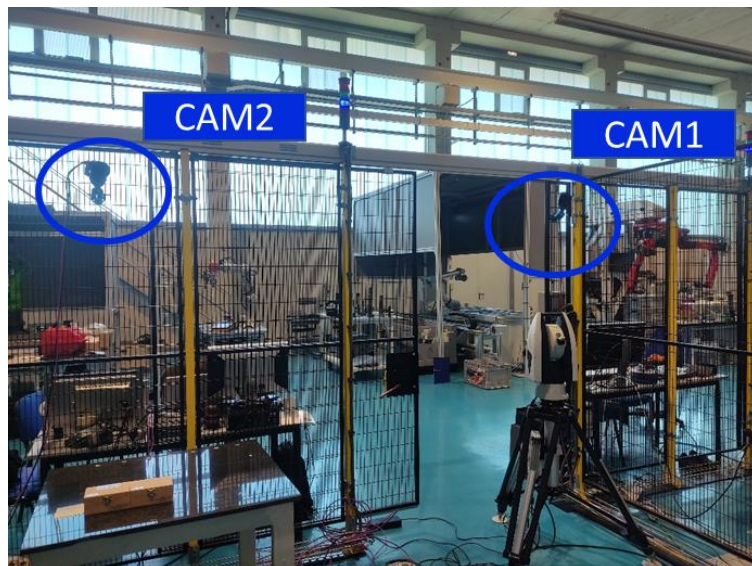
Robot trajectory
Commanded trajectory
200 μ m range error

ROBOT COMPENSATION STRATEGIES

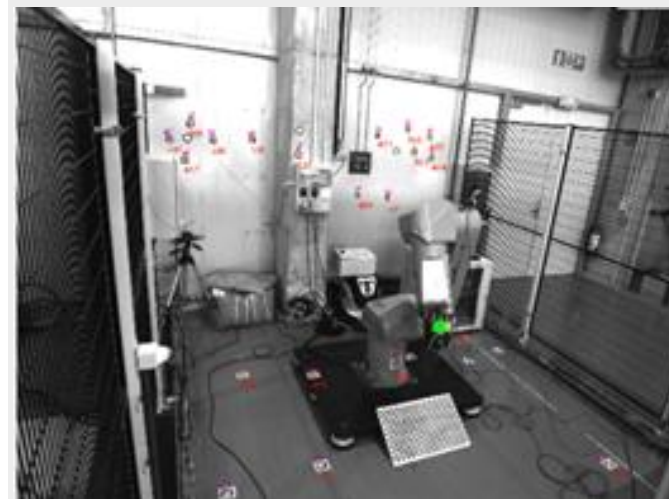
REAL CASE 2 TEKNIKER

- Stereovision system compensation
- 1 Hz
- Reduction of robot error by an order of magnitude

ON-LINE METHODS



Camera 1



Camera 2



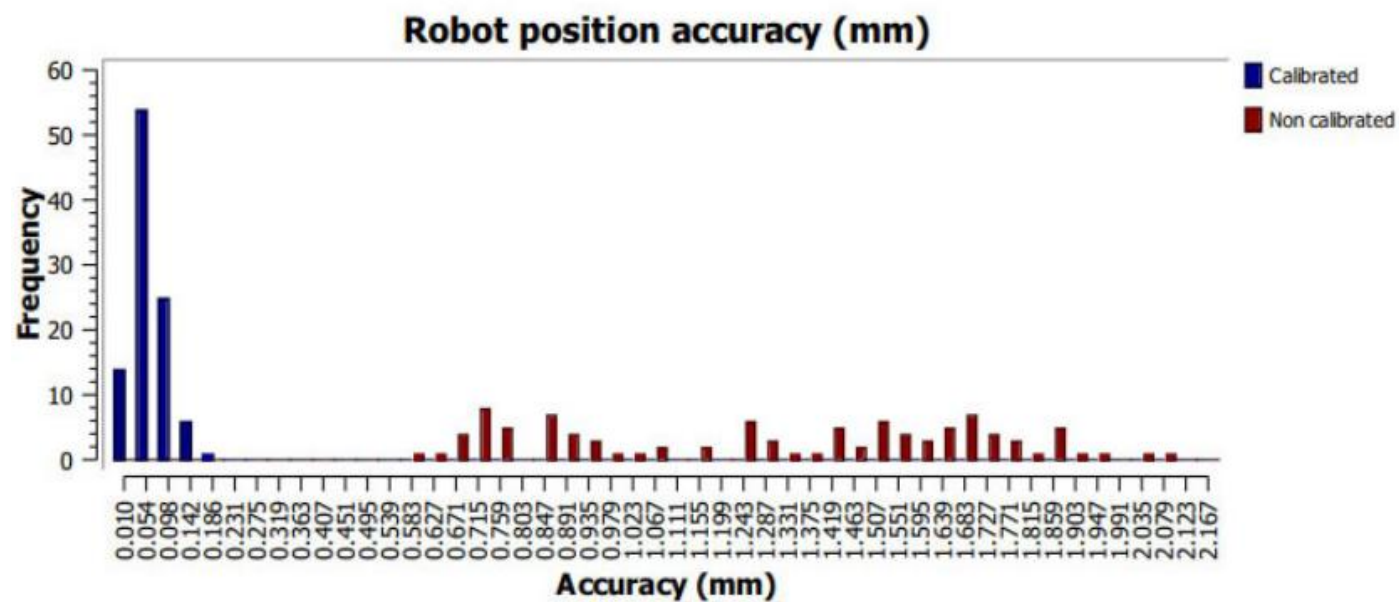
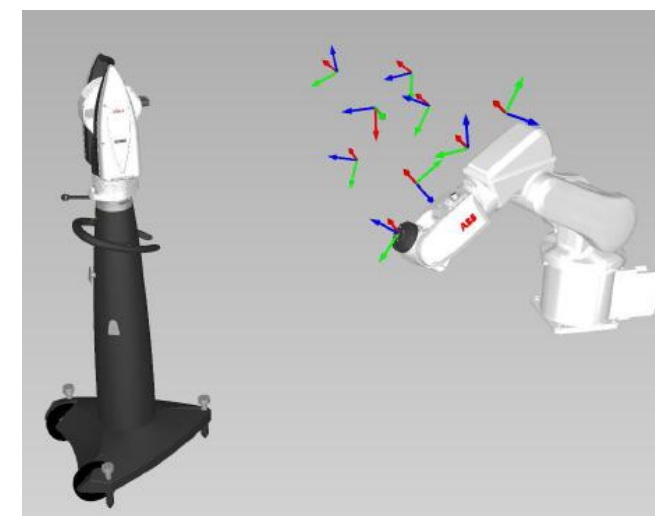


ROBOT COMPENSATION STRATEGIES

REAL CASE 1 TEKNIKER

- Laser Tracker calibration
- More than 500 robot compatibility
- Reduction of robot error by an order of magnitude

OFF-LINE METHODS

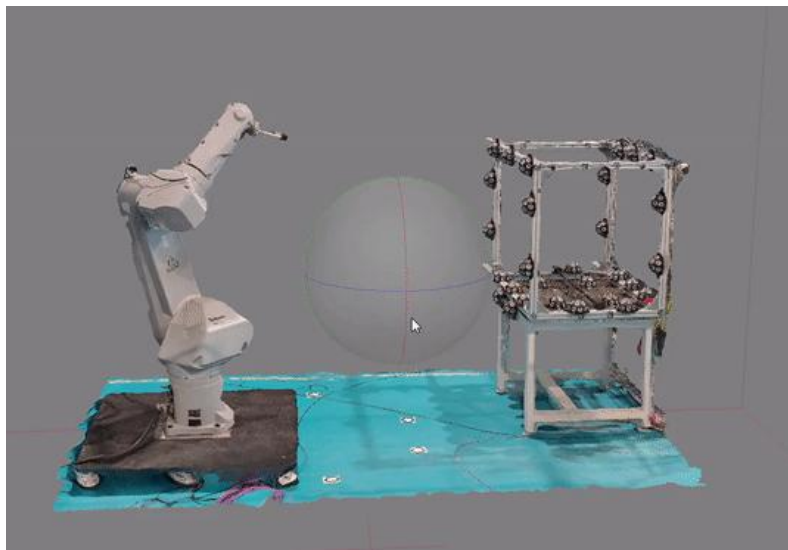


ROBOT COMPENSATION STRATEGIES

REAL CASE 2 TEKNIKER

- On-board self-calibration by vision system
- Reduction of robot error by an order of magnitude
- Fast self-calibration <20min

OFF-LINE METHODS



CAMERA ROBOT
INTERFACE

3D ARTIFACT
CONFIGURABLE
SOLUTION



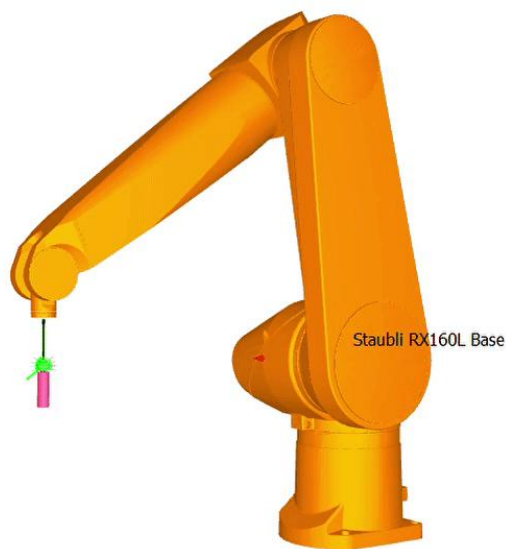
2D ARTIFACT
CHESS BOARD





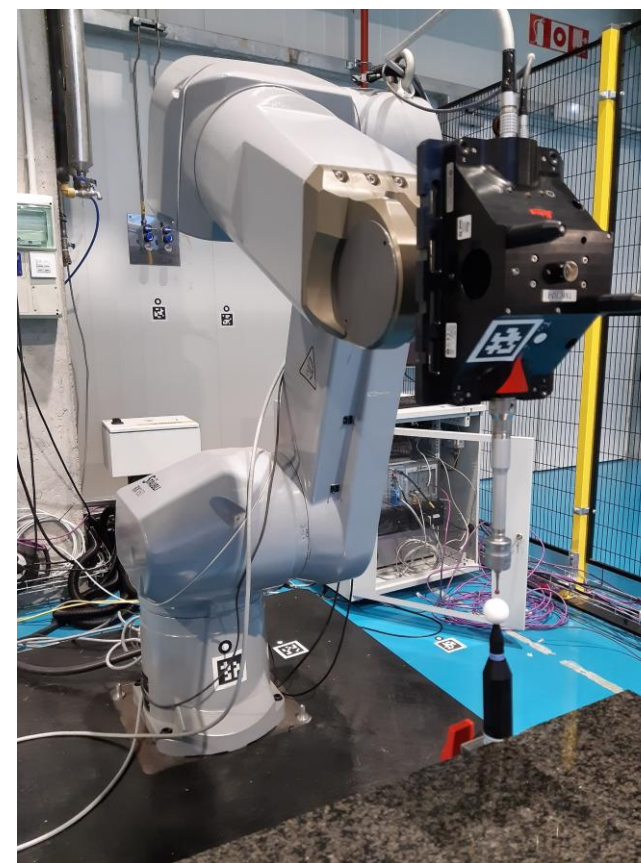
ROBOT COMPENSATION STRATEGIES

OFF-LINE METHODS



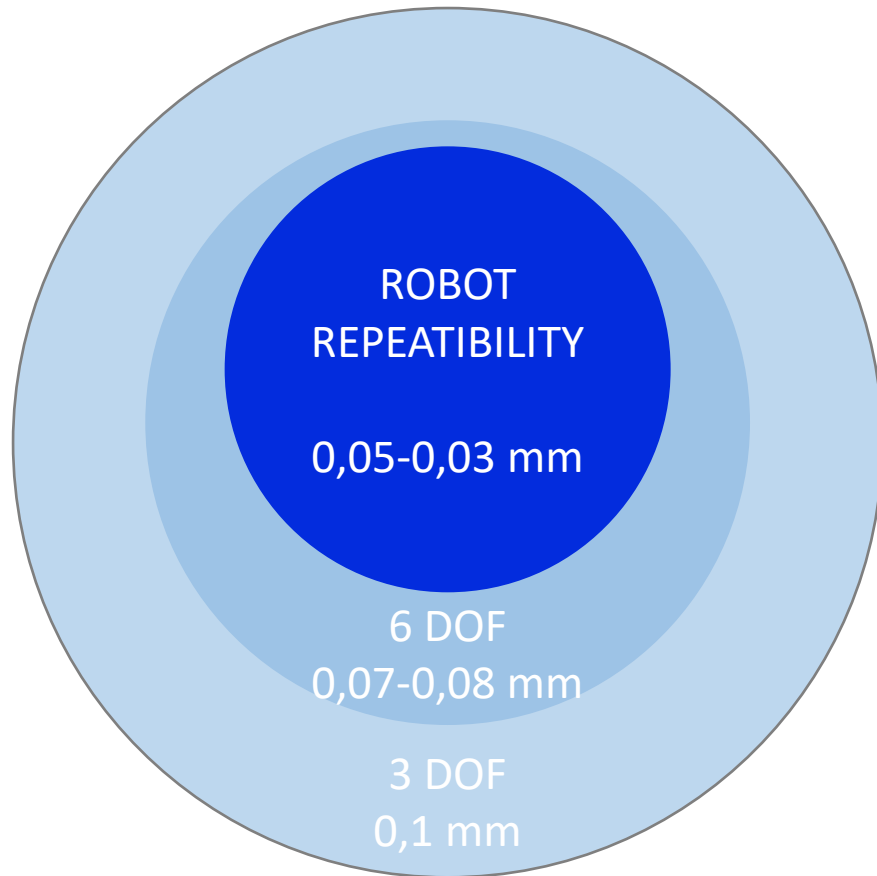
REAL CASE 3 TEKNIKER

- Probing strategy
- Robot error verification
- Robot self-recalibration
- CNC controller open interaction



EXPECTED ACCURACY

Depending types of calibration





FINAL REMINDERS



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- **VIDIT PROJECT**

- *“The project (22DIT01 ViDiT) has received funding from the European Partnership on Metrology, co-financed from the European Union’s Horizon Europe Research and Innovation”*

- **ADAM PROJECT**

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- **WORLD DAY OF METROLOGY**

- **MAY 20**



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